

## CHOOSING THE MOVIE FOR A MOVIE NIGHT

The students of your school choose a movie for a movie night among three possibilities: *All for love* (a romantic comedy), *Boulevard police* (action movie), *Creepy night* (horror movie). For short, we call these movies  $A$ ,  $B$ , and  $C$  respectively. The students vote by ordering the movies in their order of preference (first choice, second choice, third choice). For example, they write  $B > C > A$  to mean that  $B$  is the first choice,  $C$  the second choice, and  $A$  the third choice. Suppose that the result of this ranking are as follows:

$A > B > C$	38%
$A > C > B$	2%
$B > C > A$	18%
$B > A > C$	7%
$C > A > B$	3%
$C > B > A$	32%

**Which movie should be selected in your opinion?**

- Movie  $A$  has a clear win. Indeed, consider the first choice of the students: 40% choose  $A$ , 25% choose  $B$  and 35% choose  $C$ .
- Movie  $B$  has a clear win. Indeed, let's compare the movies two by two. 57% of the students prefer  $B$  to  $A$ , so  $B$  wins over  $A$ . Moreover, 63% of the students prefer  $B$  to  $C$ , so  $B$  wins over  $C$ .
- Movie  $C$  has a clear win. Indeed,  $B$  is the least favorite first option, so we can discard it. Removing  $B$  from the rankings and reconsidering which movie is the first choice, we see that 47% of the students choose  $A$  and 53% of the students choose  $C$ .

Movie  $B$  is the compromise solution because it is the second choice for 70% of the students. Since 95% of the students rank movie  $B$  as first or second choice, it would be reasonable to suggest to select movie  $B$ .

**Conclusion:** The outcome of a vote depends on the rule with which the outcome is determined. Indeed, as we see in the above example, according to the chosen rule, it's either movie  $A$  or  $B$  or  $C$  that gets selected. Before the voting it is necessary to agree on the rule. This may depend, for example, on whether compromise solutions are well-accepted or not. For example, is avoiding the third choice more important than selecting the first choice?

**A different example:** Replace  $B$  by a movie that is very similar to  $A$  (say,  $B$  is the movie *Best friends in love*). Then distributing the first choice between  $A$  and  $B$  would favor  $C$ . For example, if 64% of the students love the options  $A$  and  $B$  and detest the horror movie  $C$ , the most common first choice would be  $C$  (in case the votes of the romantic comedy fans are evenly split between  $A$  and  $B$ ). This example shows that similar choices take vote away from one another and that while casting a vote one should keep this in mind.