ARTICLE OPEN Prediction of BiS₂-type pnictogen dichalcogenide monolayers for optoelectronics

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In this work, we introduce a 2D materials family with chemical formula MX_2 (M={As, Sb, Bi} and X={S, Se, Te}) having a rectangular 2D lattice. This materials family has been predicted by systematic ab-initio structure search calculations in two dimensions. Using density-functional theory and many-body perturbation theory, we study the structural, vibrational, electronic, optical, and excitonic properties of the predicted MX_2 family. Our calculations reveal that the predicted SbX_2 and BiX_2 monolayers are stable while the AsX_2 layers exhibit an in-plane ferroelectric instability. All materials display strong excitonic effects and good optical absorption within the infrared-to-visible range. Hence, these monolayers can harvest solar energy and serve in optoelectronics applications. Furthermore, our results indicate that exfoliation of the predicted MX_2 monolayers from their bulk counterparts is experimentally viable.

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INTRODUCTION

In the last two decades, a remarkable array of two-dimensional (2D) materials has been successfully exfoliated from their bulk counterparts, including notable examples such as graphene¹, transition-metal dichalcogenides (TMDCs)², and MXenes³. These materials exhibit extraordinary properties^{4–6}, positioning themselves as promising candidates for future optical, electronic, and mechanical devices. Consequently, the quest for 2D materials with a broad range of applications is at the forefront of materials design.

Recently, computational search methods have emerged as a viable approach for exploring archetypes of 2D materials^{7–11}. Usually, the search starts with an existing material, with chemical combinatorics employed to design materials with the same prototype. This allows us to control the physical and chemical properties of the designed materials by tuning their composition. In addition, systematic exploration of different configurations (with a given stoichiometry) often leads to discovery of structures with lower energy than that of the starting configuration.

One of the most promising applications of the discovered 2D materials is the development of advanced optoelectronic devices⁴. Due to weak dielectric screening and confinement of electrons in two dimensions, the optical properties of 2D materials are often governed by strongly bound electron-hole pairs known as excitons¹². These excitons can be harnessed and utilized for practical applications in next-generation optoelectronic and photonic devices such as light-emitting diodes¹², solar cells and photodetectors¹³.

TMDCs¹⁴ and black phosphorus (BP)¹⁵ are among the most attractive 2D materials. They both display pronounced excitonic effects but have quite different optical properties otherwise. The

absence of inversion symmetry in monolayer TMDCs leads to nonlinear optical properties and the presence of strong spinorbit interactions. Locking of spin within the inequivalent K valleys leads to the ability to manipulate the valley degree of freedom using circularly polarized light¹⁴. Unlike TMDCs, BP is centrosymmetric and possesses a rectangular unit cell displaying in-plane anisotropy which results in an anisotropic optical absorption and emission spectrum¹⁵. Given the potential wideranging applications of 2D excitonic materials in next-generation optoelectronic devices, the search of 2D materials exhibiting strongly bound excitons and exceptional optical absorption across the infrared-to-visible range of the solar spectrum is very important.

In this paper, we predict a family of 2D materials based on firstprinciples density-functional theory (DFT) calculations, with stoichiometry MX_2 , where $M = \{As, Sb, Bi\}$ and $X = \{S, Se, Te\}$, for promising applications in optoelectronic devices. Our state-ofthe-art DFT and many-body perturbation theory calculations reveal that most of the predicted rectangular MX₂ (r-MX₂) monolayers are stable and absorb light within the infrared-tovisible range of the solar-energy spectrum and hence can harvest solar energy for optoelectronics applications. Furthermore, these monolayers possess inversion symmetry. They exhibit an indirect bandgap, a strong in-plane anisotropy, and strong excitonic effects. Since these monolayers have smaller exfoliation energy compared to the 1H-MoS₂ monolayer (between 8-50% of the energy needed to exfoliate 1H-MoS₂), and since their bulk counterparts have already been synthesized¹⁶⁻¹⁸, the twodimensional exfoliation of the predicted r-MX₂ monolayers seems experimentally viable.

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RESULTS AND DISCUSSION

Motivation, structure, and stability

Motivation. We decided to study MX_2 chalcogenides (M = {As, Sb, Bi} and X = {S, Se, Te}) because the whole set of materials should have similar properties (e.g., similar bonding patterns, electronic band structures, phonon dispersions, etc.), but offering the possibility to control them by changing the composition. For instance, the electronegativity decreases for the heavier elements in the MX_2 series. Also, the heavier elements have more significant spin-orbit coupling (SOC), which usually plays a substantial role in tuning the bandgap.

The ratio M/X can provide considerable information about the exfoliation possibility in three-dimensional systems. Compounds of elements of the group V and VI of the periodic table, such as Bi₂Se₃ (M/X = 2/3), have an exfoliable bulk structure, consisting of sets of the so-called quintuple layers that are stacked together *via* vdW interactions. By increasing the ratio M/X = 1, a layered bulk phase is likely to be obtained, but it may no longer be exfoliable^{16,18}. In contrast, for M/X = 0 (i.e., the bulk of pure S, Se, or Te, the system is no longer layered; it is composed of open or closed chains joined by vdW forces¹⁹. Therefore, we expected to find exfoliable 2D materials for a ratio of M/X = 1/2 and that we could use this MX₂ stoichiometry to push our structural-search algorithm to a yet unexplored "playground" (we were unaware of the experimental identification of the reported BiS₂ bulk phase^{16,18} when we started our structure search).

Ab-initio structure prediction. The predicted structure in this work was obtained by systematic ab-initio structure search calculations performed using the constrained minima hopping method (cMHM)^{20,21}. This method employs an efficient dynamical algorithm, which couples DFT with short molecular dynamics simulations to explore the multidimensional potential energy surface (PES) of guasi-2D materials, intending to discover local and global minima on the PES²²⁻²⁷ (see Ref. ²¹ for technical details). In a previous work²¹, the cMHM successfully predicted several phases and reproduced the known 2D crystal phases of Bi monolayer. In this work, we perform similar structure search calculations as reported in Ref. ²¹ but for the BiS₂ composition. In our structure search calculations, we considered one (3 atoms/cell) to eight (24 atoms/cell) formula units of BiS₂. The obtained lowenergy structures corresponding to local minima on PES were further optimized using tighter convergence criteria of k-mesh sampling and plane-wave energy cutoff (see Methods section) with the inclusion of SOC. The obtained lowest energy configuration was considered the ground state structure of BiS₂ monolayer. This inference was further supported by a comparative energetics study of other candidate phases of BiS₂ monolayers as discussed below.

Structural properties and crystallographic details. The obtained ground state configuration of the BiS₂ monolayer, shown in Fig. 1, is centrosymmetric and belongs to the 2D layer group cm11 (no. 13); the 3D supercell containing vacuum along c axis belongs to the space group C2/m (no. 12). The conventional unit cell (shown in blue in Fig. 1) has a rectangular shape, whereas the primitive cell (shown in red in Fig. 1) has a rhombic shape. Following the conventional cell, the 2D Bravais lattice is rectangular and we refer to this system as the r-BiS₂ monolayer. We have also calculated the relaxed geometries of the other rectangular pnictogen dichalcogenides to which we will refer as r-MX₂ in the following.

The primitive lattice vectors of r-MX₂ are $\mathbf{a}_1 = (a/2, -b/2, 0)$ and $\mathbf{a}_2 = (a/2, b/2, 0)$, as marked using red arrows in Fig. 1. The *a* lattice parameter varies from 14.5 Å for AsS₂ to 16.7 Å for BiTe₂. The values of *b* ranges between 3.7 Å for AsS₂ and 5.5 Å for BiTe₂. The angle between both vectors is ~ 28°. Naturally, the heavier the constituent atoms are, the larger are the lattice parameters



Fig. 1 Rhombic structure of $r-MX_2$ monolayer. a Top and (b) side views of the studied $r-MX_2$ monolayer. The conventional (blue) and primitive (red) unit cells are drawn in panel (a).

(see Fig. 2), but the effect is considerably more pronounced for the chalcogen atoms than for the pnictogen atoms.

Stability of r-MX₂ monolayers. The calculation of elastic constants helps to verify the elastic and mechanical stability of the r-BiS₂ monolayer^{28,29}. Our calculated elastic constants (with SOC) are: $C_{11} = 17.5, C_{12} = 6.9, C_{22} = 28.9$, and $C_{66} = 7.3$ N/m. These elastic constants are of the same order of magnitude as in the buckledhexagonal BiSb monolayer ($C_{11} = C_{22} = 24.4$, and $C_{12} = 5.8 \text{ N/m}$)³⁰. Dynamical stability of r-BiS₂ and the other compounds has been checked by calculating the phonon dispersions which will be discussed in the section on vibrational properties below. Altogether, our calculations suggest that the predicted r-BiS₂ monolayer is energetically, elastically, mechanically, and dynamically stable, providing support to the notion that it could be experimentally realized. The results on elastic constants and phonon dispersions of all r-MX₂ monolayers studies in this manuscript are given in the Supplementary Table 1 and Supplementary Fig. 2.

In addition to the monolayer r-MX₂ geometry predicted in this work, for the sake of comparison, we explicitly considered the two hexagonal TMDC-like structures, 1H-MX₂ (trigonal prismatic) and 1T-MX₂ (octahedral) geometries². Our calculations reveal that the predicted r-MX₂ structure is indeed the lowest-energy ground state geometry among all the studied geometries for the MX₂ family; see Supplementary Fig. 2, which shows a systematic comparison of the relative energy among the three MX₂ phases (1H, 1T, and rectangular). It is not surprising that the 1T- and 1H-MX₂ geometries have relatively high energy: they both are highly-coordinated structures, and the MX₂ compounds studied here seem to have an "incorrect" stoichiometry³¹ due to mixing of elements from the group V and VI in a proportion 1 to 2. Atoms S, Se, and Te already have 6 valence electrons, very close to reaching



Fig. 2 Relevant energies and parameters of all r-MX₂ compounds. a Calculated formation energy (E_{form}) of each r-MX₂ monolayer (see Eq. (3)). **b** G_0W_0 (solid black line) and HSE06 band gap with (solid red line) and without (dashed line) spin-orbit coupling, and (**c**) lattice parameters *a* and *b* as defined in the text. In all panels the lines are a guide to the eye for systems with the same M (As, Sb, or Bi) atom.

the octet¹⁹. Although this rule is not expected to be strictly followed, a significant deviation from it has to be energetically unfavorable which is manifested here in the relatively high energies of the hexagonal structures.

The SbS₂, SbSe₂, BiS₂, and BiSe₂ monolayers are already present in the Computational 2D Materials Database (C2DB)⁷ but only in the 1T-MX₂ phase. The stability of these materials is labeled as "high", except for the thermodynamic stability of BiSe₂, which is "medium" (it lies relatively high in the minimum energy convex hull). As we mentioned before, the family of r-MX₂ compounds has The possibility of synthesizing the r-MX₂ monolayer also requires a low formation energy E_{form} (see Eq. (3)). For instance, the 1H-MoS₂ monolayer has been successfully exfoliated by micromechanical methods³² and has formation energy $E_{form} \approx 80$ meV/atom³³. Compared with all predicted r-MX₂ monolayers, all formation energies are $E_{form} \lesssim 40$ meV/atom, as shown in Fig. 2a. Since E_{form} is lower for all the orthorhombic MX₂ compounds, its exfoliation from its bulk phase seems viable. In general, 2D materials with $E_{form} < 200$ meV/atom do not need a stabilizing substrate, and they are regarded stable as free-standing or suspended flakes³⁴.

Experimentally, the bulk phase of r-BiS₂ and r-BiSe₂ (a layered monoclinic structure in space group C2/m) has been synthesized at ~ 5.5 GPa pressure^{16,17}. The experimental atomic positions and lattice parameters are consistent with our calculations. There exist two other reports on bulk BiS₂ obtained in similar growth conditions, but the crystal geometry was not specified^{18,35}. Likely, it is the same monoclinic phase, which is the only phase of BiS₂ reported so far. One of these studies indicates that bulk BiS₂ is stable in water¹⁸. Overall, these studies suggest the possibility of synthesizing the two-dimensional r-BiS₂ and r-BiSe₂ through exfoliation, and a similar synthesis approach may be possible for the other r-MX₂ monolayers.

Vibrational properties

Since the primitive unit cell of $r-BiS_2$ monolayer contains six atoms (2 Bi and 4 S), there are 15 allowed optical phonon modes, which can be described by the following irreducible representation at the zone center

$$\Gamma_{\text{optic}} = 6A_{\text{g}} \oplus 2A_{\text{u}} \oplus 3B_{\text{g}} \oplus 4B_{\text{u}}.$$
(1)

Here A_g and B_g modes are Raman active, whereas A_u and B_u modes are infrared active. The predicted frequencies of these modes at the zone center are as follows: $A_g = 34$, 92, 173, 238, 282, and 469 cm⁻¹; $A_u = 52$ and 172 cm⁻¹; $B_g = 48$, 103, and 215 cm⁻¹; $B_u = 92$, 156, 210, and 291 cm⁻¹.

It is worthwhile to have a closer look at the phonon dispersion of r-BiS₂ shown in Fig. 3a. The dispersion has been calculated with a 2D Coulomb cutoff³⁶ in order to prevent an LO/TO splitting which, otherwise, would occur at the Γ point for some of the phonon modes³⁷. Instead of the LO/TO splitting, we observe an overbending at Γ of some of the infrared active modes. In particular the A_u mode at 52 cm⁻¹ displays an ultra-strong overbending in the $\Gamma \rightarrow C_2$ and the $\Gamma \rightarrow V_2$ directions (but not in the ΓY_2 direction where the phonon displacement is perpendicular to the phonon wave vector). The origin of this overbending, marked by the red line in the dispersion, becomes clear when looking at the displacement pattern in panel (b): the mode is strongly polar with all sulfur atoms moving in one direction and all bismuth atoms moving in the opposite direction.

The extreme overbending is actually connected to incipient ferroelectric behaviour. Actually, in the AsX_2 compounds, this mode is soft (see Supplementary Fig. 2). Geometry relaxation along this mode leads to a polar structure of lower energy, displaying a dipole moment in the plane. The polar structures, along with the unit-cell parameters and the energy gain with respect to the non-polar structure are shown in the Supplementary Fig. 4. This adds the predicted materials to the recently published list of 2D ferroelectric materials, found by a computational high-throughput search³⁸.

The highest phonon branch at 469 cm^{-1} is almost flat. This mode consist of bond-stretching of the (only) S-S bond in the structure as displayed in panel (b). All other atoms are at rest. The relatively large distance between neighboring S-S bonds explains the flatness of the band. Likewise, the second highest mode (291 cm⁻¹ at Γ) is also very flat, because only sulfur atoms outside



Fig. 3 Vibrational properties of r-BiS₂ **monolayer. a** Phonon dispersion of r-BiS₂ monolayer calculated using density-functional perturbation theory with a 2D coulomb cutoff (see Supplementary Fig. 1 for calculated phonons of all r-MX₂ monolayers studied in this work). Black circles denote the Raman active phonon modes and red lines depict the infrared active mode with overbending. **b** Vibration pattern for over-bending A_u mode and for the two highest frequency Raman modes at Γ . **c** Off-resonant Raman spectrum at 300 K computed within DFPT.

the S-S bond are participating, interacting only very loosely with the neighboring cluster of vibrating atoms.

The phonon dispersion of r-BiS₂ does not have any soft modes and thus demonstrates the dynamical stability of this monolayer. The presence of minor imaginary phonon frequencies in the parabolic acoustic ZA branch near the zone center is ascribed to the numerical inaccuracies in the long-wavelength limit $(q \rightarrow 0)^{39,40}$ and can be observed in the calculated dispersion of many 2D materials. The calculated phonon dispersions of most of the r-MX₂ family members (See Supplementary Fig. 2) are similar to that shown in Fig. 3, except for the r-AsX₂ monolayers that exhibit a ferroelectric instability. Figure 3c shows the computed non-resonant Raman spectrum of r-BiS₂. It demonstrates that 7 out of the total of 9 Raman active modes are clearly visible in the spectrum. We thus expect that Raman spectroscopy will be a very useful tool to identify $r-MX_2$ monolayers and to distinguish them from hexagonal phases of 2D materials (which only have two Raman active modes at high energy and the layer shear mode at very low energy⁴¹).

Electronic properties

Before showing electronic band structure results from our DFT calculations, let us briefly discuss what could be expected from the predicted r-MX₂ monolayers, in contrast to the 1H- and 1T-MX₂ monolayers. The 1H- and 1T-MX₂ monolayer structures proposed so far are metallic⁷ – and hence are not suitable for optoelectronics applications – for a straightforward reason: they have an odd number of electrons per unit cell. In our case, the rhombic lattice of r-MX₂ (Fig. 1) doubles the unit cell, removing that band-filling constraint and, thus, allowing a bandgap at the Fermi energy.

Figure 4 shows the electronic band structures of all $r-MX_2$ monolayers calculated using $G_0W_0^{42-44}$ (solid lines) and PBE⁴⁵ (dashed lines) methods with the inclusion of SOC effects. We notice that the overall dispersion of bands does not change substantially as a function of the employed exchange-correlation (XC) functional. However, the bandgap varies considerably for different employed XC functionals (see Table 1). While the effect of SOC is almost negligible for the lighter elements considered, it can be substantial for the heavier constituent elements, especially for the BiX₂ series. Note, there is no SOC-induced spin splitting of bands owing to the centrosymmetric structure of the r-MX₂ monolayers.

Figure 2b and Table 1 show the bandgap calculated using different theoretical methods. Most of the $r-MX_2$ monolayers are predicted to absorb light within the visible range of the solar spectrum. An indirect bandgap is observed in As and Sb monolayers while a direct gap is seen in Bi monolayers. This could be a significant advantage compared to the traditional TMDCs as it strongly suppresses the electron-hole recombination (luminescence) during the optoelectronic applications. Recent works on TMDCs report that non-radiative electron-hole recombination channels can be further suppressed by electrostatic doping⁴⁶ and strain⁴⁷. We anticipate that similar approaches can be applied to enhance the optoelectronic performance of the predicted r-MX₂ monolayers.

Optical properties and many-body effects

In order to obtain the absorption spectrum, including electronhole interactions, we solve the Bethe-Salpeter equation (BSE)⁴⁸ on top of the G₀W₀ calculations within the Tamm-Dancoff approximation⁴² using the YAMBO code⁴³. The optical absorption spectrum along the polarization direction μ is described by the imaginary part of the 2D polarizability tensor and is given by⁴⁸

$$\operatorname{Im}\left\{a_{2D}^{\mu}(\omega)\right\} = \frac{2\pi e^{2}}{A\omega^{2}} \sum_{S} \left|\sum_{vc\mathbf{k}} A_{vc\mathbf{k}}^{S} \langle v\mathbf{k} | v^{\mu} | c\mathbf{k} \rangle\right|^{2} \delta(\omega - E_{S})$$
(2)

where A is the area of the unit cell, v^{μ} is component of the velocity operator along the direction μ , A_{vck}^{S} are the expansion coefficients of the exciton eigenstate S in the electron-hole basis and E_{S} is the exciton energy.

The optical absorption spectra for $r-MX_2$ monolayers obtained by solving the BSE are shown in Fig. 5. The solid and dashed colored lines show the absorption spectrum computed with and without including electron-hole interactions. The onset of direct optical absorption occurs within the infrared-to-visible range of the solar spectrum. Moreover, for all the monolayers, the absorption onset starts before the indirect gap. The double peak



Fig. 4 Electronic properties. Electronic band structure of r-MX₂ monolayers calculated using G_0W_0 (solid lines) and PBE (dashed lines) including the effects of spin-orbit coupling. The *k*-path for BiS₂ is formed by Γ (0.0, 0.0), C (-0.268, 0.268), C₂ (0.268, 0.732), Y₂ (0.5, 0.5), and V₂ (0.0, 0.5). The coordinates for C, C₂, and Y₂ depend on the cell parameters and were determined by the materialscloud's SeeK-path tool⁶⁴. The Fermi energy (E_{*F*}) is set at the valence band maximum.

Table 1. Bandgap (eV units) of r-MX2 monolayers calculated usingPBE, PBE+SOC, HSE06, HSE06+SOC, and G_0W_0 +SOC.							
r-MX ₂ monolayer	PBE	PBE +SOC	HSE06	HSE06 +SOC	$G_0W_0 + SOC$		
AsS ₂	1.25	1.17	1.92	1.91	2.01		
AsSe ₂	0.96	0.88	1.54	1.51	2.06		
AsTe ₂	0.52	0.48	0.98	0.83	1.38		
SbS ₂	1.42	1.35	2.12	2.08	2.24		
SbSe ₂	1.09	1.03	1.69	1.62	2.23		
SbTe ₂	0.65	0.63	1.10	1.00	1.57		
BiS ₂	1.47	1.04	2.20	1.87	1.84		
BiSe ₂	1.17	0.76	1.81	1.45	1.82		
BiTe ₂	0.70	0.26	1.19	0.73	0.83		

structure (A/B excitons) observed in 2H-Mo(W) X_2 monolayers² due to spin-orbit splitting of the top valence band is absent in these materials due to the inversion symmetry of the crystal.

In Fig. 5, we also observe that strongly bound excitons dominate the optical absorption spectrum for all $r-MX_2$ monolayers. We find that for all the studied monolayers, the absorption onset shifts by a few hundred meV when excitonic effects are included, which indicates that excitons possess large exciton binding energies. Similar to the case of excitons in MoS₂ and other transition metal dichalcogenides^{14,41}, these large binding energies are due to the reduced environmental screening in monolayers and the quasi-2D nature of the excitons.

The dielectric screening increases when going down the periodic table for the chalcogen atoms, which is in line with a decrease in direct bandgap, as shown in Fig. 5. The lowering of direct bandgap results in a red shift of absorption onset with an increase in the atomic number of the chalcogen atom, as shown in Table 2. In contrast, we do not observe a clear trend with the pnictogen atomic number. The bandgaps and the first exciton energies are highest for the Sb-based compounds.

Finally, we look at the anisotropic optical absorption of these materials. We start by comparing the excitons in MX₂ monolayers with monolayer BP as both materials exhibit anisotropy and possess inversion symmetry. Due to the difference in crystal symmetries for MX_2 monolayer (C_{2h}) and monolayer BP (D_{2h}), we observe different optical selection rules. In monolayer BP, the bright excitons transform under two different representations $(B_{2\mu})$ and B_{3u} , which results in selective coupling of excitons to either x or y polarized light⁴⁹. In contrast, the bright excitons in r-MX₂ monolayers transform according to the single representation (B_u) which can couple to both x or y polarized light (yet, with different intensities as the calculations show). In Fig. 5, we present the absorption spectra for all the monolayers along the x and y directions. (The x and y directions are shown in Fig. 1). The first few bound excitons in all monolayers exhibit a greater oscillator strength along the y direction than the x direction. This anisotropy in the optical absorption spectrum arises from the in-plane geometric anisotropy within the crystal structure.

Role of temperature

In general, an increase in temperature leads to a decrease in the band gap of semiconductors, primarily due to electron-phonon interactions. This effect is observed not only in traditional semiconductors but also in two-dimensional systems like MX₂ compounds, which include materials such as MoS₂, WSe₂, and WS₂^{50,51}. These changes in the band gap result in a slight redshift ($k_BT \sim 26$ meV) in the optical absorption spectra, including the energy peaks associated with excitons (as depicted in Fig. 5). Similar to the band gap, the size of the exciton peaks diminishes with increasing temperature, although they remain experimentally detectable in materials like MoSe₂.

 $MoSe_2$, with its comparable electronic band gap (~2 eV) and optical properties⁵⁰, provides a valuable point of reference for comparing and extrapolating the temperature-induced effects observed in our compounds. Consequently, at room temperature, we anticipate only minor or negligible perturbations in the band gap and, consequently, in the optical and exciton properties.



Energy (eV)

Fig. 5 Optical properties. Optical absorption spectra for different $r-MX_2$ monolayers. The solid and dashed lines correspond to the optical absorption spectrum calculated with and without considering electron-hole interactions. The red and blue lines in each subplot represent the absorption spectrum calculated along x and y polarization directions, respectively. The x and y directions are shown in Fig. 1. All spectra are plotted with a linear broadening ranging from 10 meV to 100 meV with the minimum and maximum energy. The solid and dashed vertical lines in each subplot denote the computed energies (with SOC effects) of the direct gap and the bandgap, respectively.

Table 2. First bright exciton energies of MX_2 monolayers (in eV)calculated using BSE+G0W0+SOC.					
MX ₂	S	Se	Те		
As	1.97	1.91	1.07		
Sb	2.00	2.01	1.34		
Bi	1.20	1.26	0.45		

Outlook

Compared to other known phases of MX₂ monolayers, such as the 1H- and 1T-MX₂ geometries, our predicted r-MX₂ monolayers exhibit the highest stability, as indicated by their lowest formation energy. These materials can be easily exfoliated from their bulk counterparts, requiring only a tiny amount of energy (8-50% of the energy needed to exfoliate 1H-MoS₂ monolayer). Some of the r-MX₂ monolayers in our study are indirect bandgap semiconductors. The bandgaps predicted by the G_0W_0 method range from 0.83 eV in BiTe₂ to 2.24 eV in SbS₂. Importantly, all the r-MX₂ monolayers absorb light within the infrared-to-visible range of the solar spectrum and exhibit significant excitonic effects with large exciton binding energies. Our findings suggest promising applications of r-MX₂ monolayers in optoelectronic devices operating in the solar-energy range. Furthermore, considering that the three-dimensional counterpart of r-BiS₂ has already been experimentally synthesized, and the formation energy of r-MX₂ monolayers is lower than half that of 1H-MoS₂ monolayers, the exfoliation of r-MX₂ monolayers appears to be a feasible experimental approach.

METHODS

DFT details

All DFT calculations were performed using the Vienna ab initio simulation package (vAsp)⁵² and the QUANTUM ESPRESSO (QE) package⁵³ with the Perdew-Burke-Ernzerhof (PBE) exchange-correlation (XC)

functional⁴⁵. We used fully relativistic projector augmented wave^{54,55} for VASP calculations and norm-conserving pseudopotentials from the PSEUDODOJO project⁵⁶ for the QE calculations. Spinorbit coupling (SOC) was included in all DFT calculations unless specified otherwise.

In order to obtain the equilibrium lattice parameters, we first performed structural relaxation with the VASP code. We later performed self-consistent calculations to obtain the ground state charge densities. A plane wave energy cutoff of 400 eV and a uniform Γ centred k-point sampling of $24 \times 24 \times 1$ was employed for all the VASP calculations. We calculated the electronic band structures using screened-hybrid functional of Heyd-Scurseria-Ernzerhof (HSE06)⁵⁷ as PBE-XC functional⁴⁵ generally underestimates the bandgap. <code>PYPROCAR⁵⁸</code> and <code>MECHELASTIC²⁹</code> packages were used for further analysis of the electronic and elastic properties, respectively.

Formation energies for all the materials were computed using the following expression

$$E_{form} = \frac{E_{2D}}{N_{2D}} - \frac{E_{3D}}{N_{3D}},$$
 (3)

where $E_{2D/3D}$ are monolayer and bulk energies of MX₂ and $N_{2D/3D}$ are the number of atoms in the unit cell^{33,34,59}. This energy compares the energetics of the monolayer and bulk structures, which allows us to judge the possible experimental realization by means of exfoliation.

We employed density-functional perturbation theory (DFPT)⁶⁰ for phonon calculations as implemented within the QE code. All the structures were relaxed again using the QE code with a convergence threshold of 10^{-6} Ry and 10^{-5} Ry/Bohr for total energy and forces, respectively. To obtain the ground state charge densities, we used a plane wave cutoff of 100 Ry and a uniform Γ centred $9 \times 9 \times 1$ k-point grid. We set a vacuum spacing of 16\AA for all materials and employed a 2D Coulomb cutoff technique³⁶ to remove spurious interactions along the out-of-plane direction. In order to obtain phonon dispersions, we computed dynamical matrices on a coarse $4 \times 4 \times 1$ Γ centred q-point grid. These dynamical matrices were Fourier interpolated to obtain the

force-constant matrix in real space, which in turn is employed to calculate the phonon dispersion on a fine q-point path.

For the *GW* calculations, we first obtained the Kohn-Sham energies and wave functions on a uniform $9 \times 9 \times 1$ k-point grid by performing a non self-consistent calculation with a plane wave cutoff of 80 Ry using the QE code. In order to construct the microscopic dielectric tensor, we used a plane wave cutoff of 8 Ry and performed the summation with 1000 Kohn-Sham states. The frequency dependence of the dielectric tensor was described within a plasmon-pole approximation⁶¹. A 2D Coulomb cutoff along the out-of-plane was employed to remove the interactions with periodic images. In order to speed up the convergence of G_0W_0 calculations with respect to bands and kpoints, we used a G-terminator⁶² and RIM-W⁶³ technique, respectively.

To obtain well-converged absorption spectra, we used a uniform Γ -centred $30 \times 30 \times 1$ k-point grid for all r-MX₂ monolayers. A total of 250 bands and a cut-off of 4 Ry were used to build the static dielectric tensor. We included the top eight valence and the bottom eight conduction bands to construct the BSE interaction kernel. A plane-wave cutoff of 60 Ry and 4 Ry was used in the construction of bare exchange and screened Coulomb blocks, respectively.

Reporting summary

Further information on research design is available in the Nature Research Reporting Summary linked to this article.

DATA AVAILABILITY

Additional data on elastic constants and stability in comparison to hexagonal phases, as well as all calculated phonon dispersions are available in the Supplementary Table 1 and Supplementary Fig. 2 accompanying this paper. Input and output files of our DFT, GW, and BSE calculations on band-structures, optical spectra and phonon dispersions are available in the NOMAD repository with identifier https://doi.org/10.17172/NOMAD/2024.01.03-1. All relevant data is also available from the authors upon reasonable request.

CODE AVAILABILITY

The first-principles DFT calculations were performed using the privately-licensed VASP, and the open-source Quantum ESPRESSO software.

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AUTHOR CONTRIBUTIONS

This project was conceived by S.S. and the reported 2D materials family were predicted by structure search calculations conducted by S.S. J.D.M., F.M., K.M.R., and A.H.R. studied the electronic structure and stability of the reported monolayers. M.N. and L.W. performed calculations to study the optical and vibrational properties. All authors discussed the findings. The manuscript was written by J.D.M., M.N., F.M., L.W., and S.S. All authors read and commented on the manuscript. J.D.M. and M.N. equally contributed to this work.

COMPETING INTERESTS

The authors declare no competing interests.

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