

A wireframe bear is superimposed on a blue server room background. The bear is composed of a mesh of white lines forming its shape. The server room features rows of server racks with glowing blue light strips and vertical beams of light. In the background, there are faint, glowing binary code patterns (0s and 1s) scattered across the scene.

Workload Estimation and Load-Balancing of Discrete Element Method

**EUROHPC
USER DAY
2023** Brussels
11.12.23



Project: Workload Estimation and Load-Balancing of
Discrete Element Method
EuroHPC used: MeluXina

Speaker: Xavier BESSERON (*Uni. of Luxembourg*)

Workload Estimation and Load-Balancing of Discrete Element Method

Outline

Extended Discrete Element Method

- What is XDEM?

Parallelization of XDEM

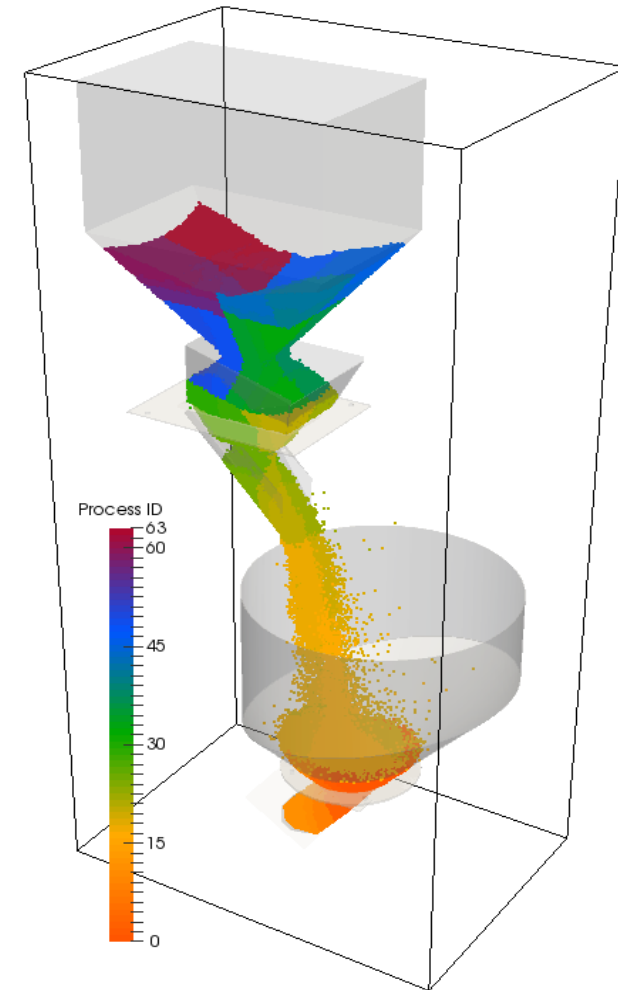
- Domain Decomposition with MPI
- Load-Balancing

Workload Estimation for XDEM

- Toward better Load-Balancing

Preliminary Results

- Load Estimation and Imbalance



Extended Discrete Element Method

What is XDEM?

eXtended Discrete Element Method

What is XDEM?

Simulation software for

Particles Dynamics

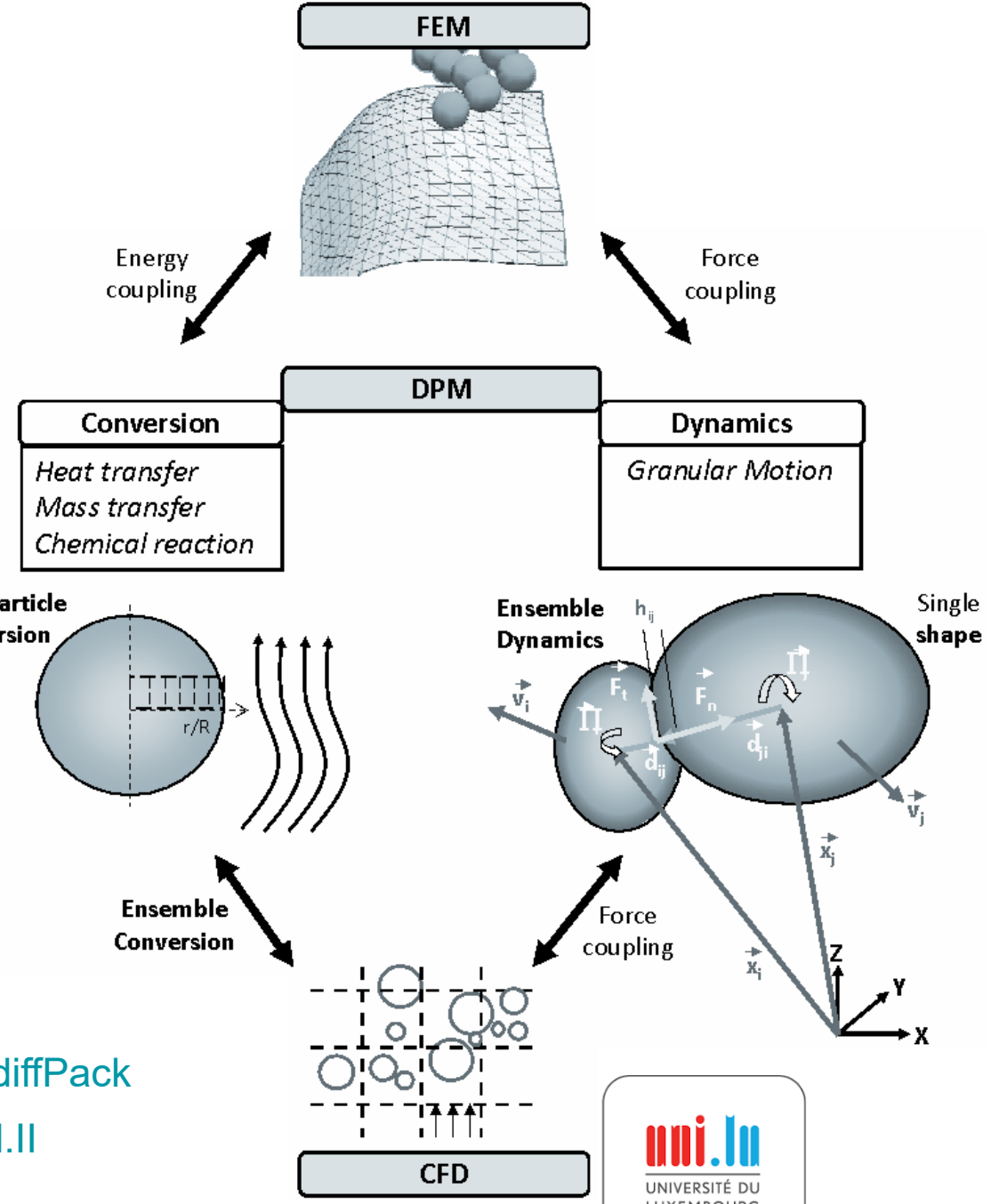
- Force and torques
- Particle motion

Particles Conversion

- Heat and mass transfer
- Chemical reactions

Coupled with

- Computational Fluid Dynamics (CFD)
- Finite Element Method (FEM)

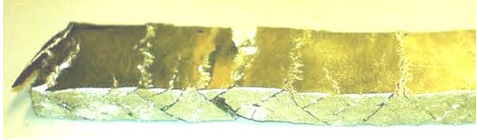
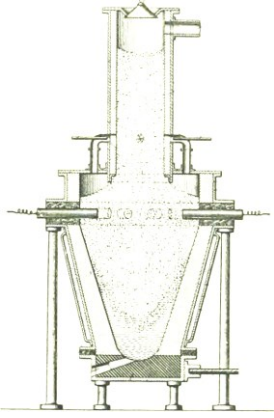


OpenFOAM
ANSYS Fluent

diffPack
deal.II
CalculiX

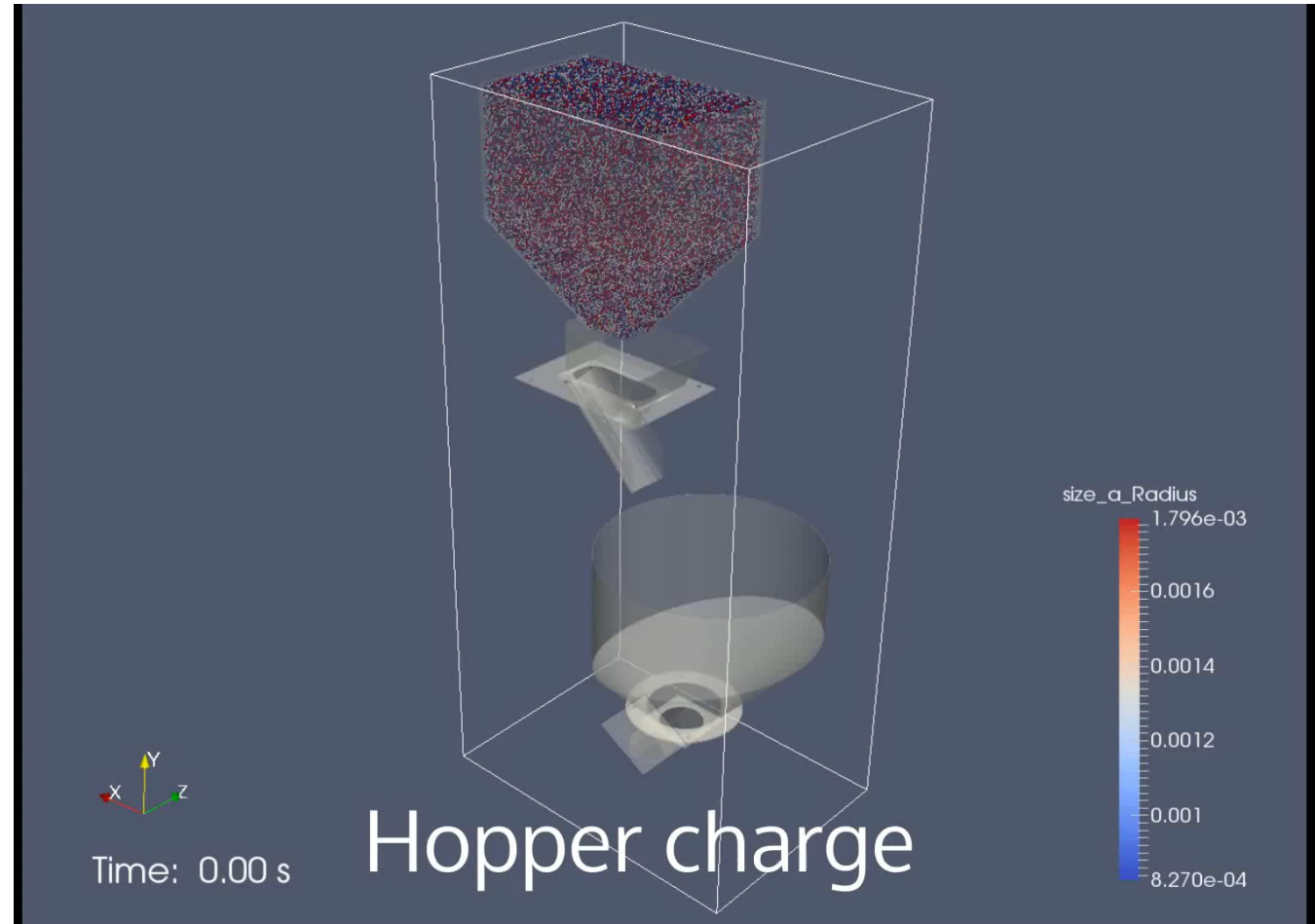
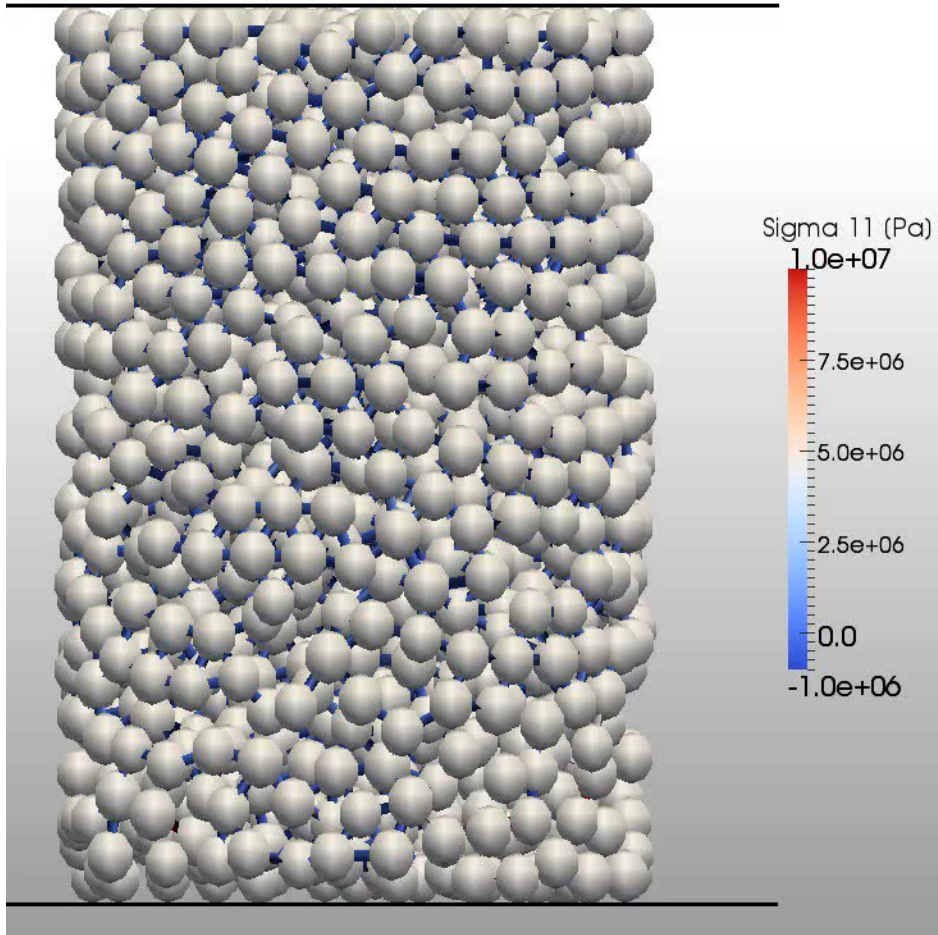


Application Examples: XDEM

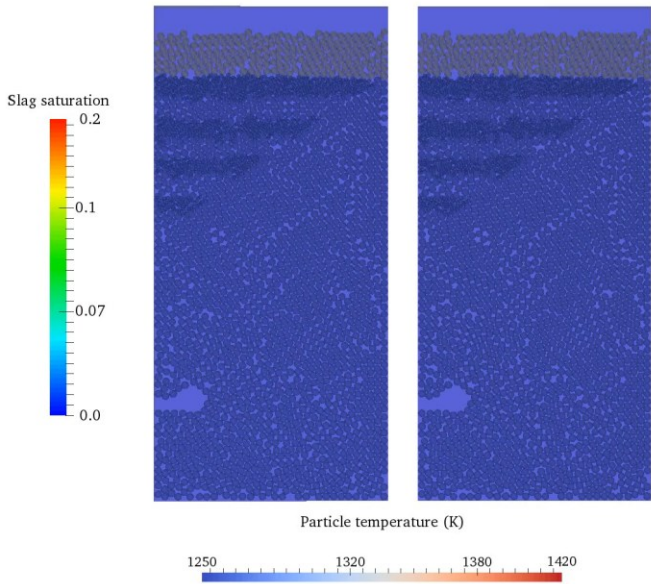


Brittle Failure

Hopper charge and discharge



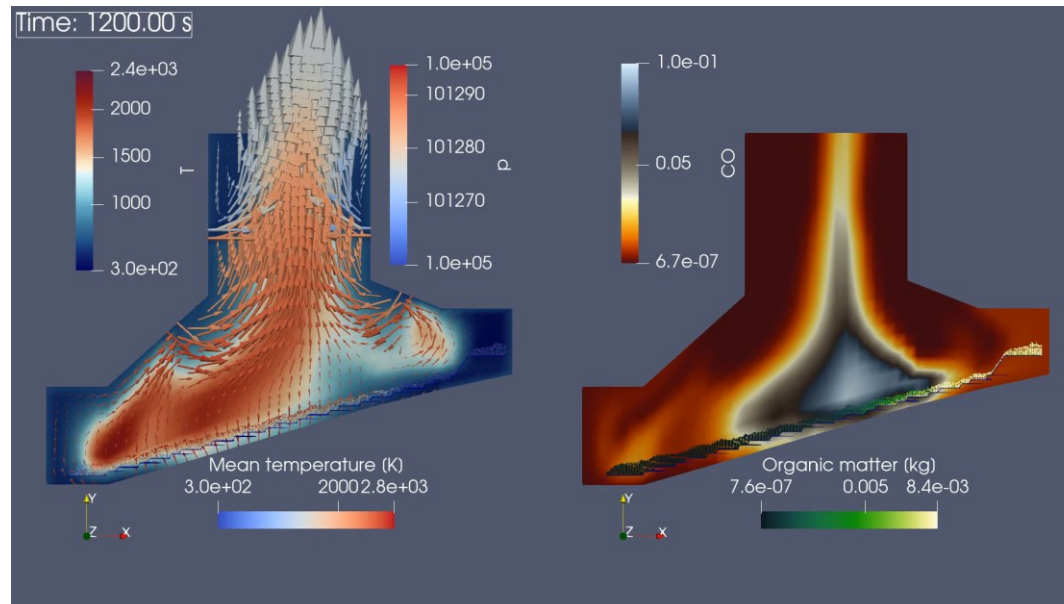
Application Examples: XDEM coupled with CFD



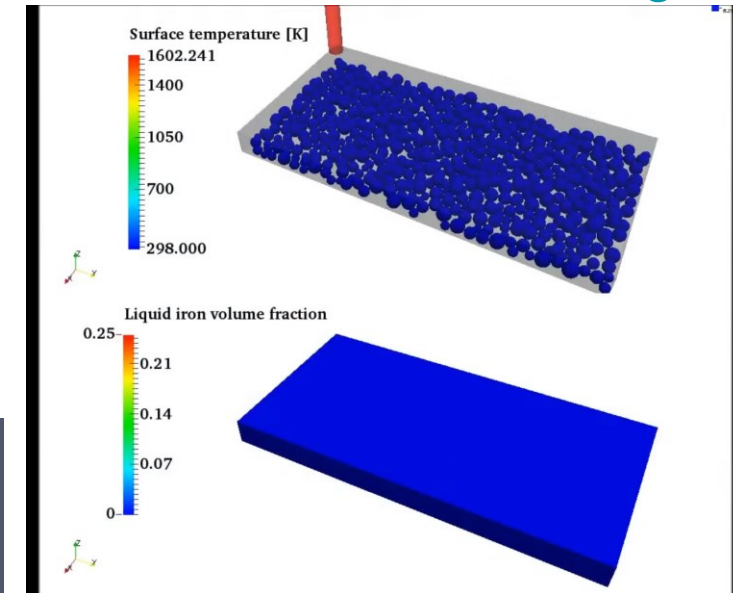
Iron & Slag production in a Blast Furnace



Wood Conversion in a Biomass Furnace



Selective Laser Melting in Additive Manufacturing



Parallelization of XDEM

Domain Decomposition with MPI and Load-Balancing

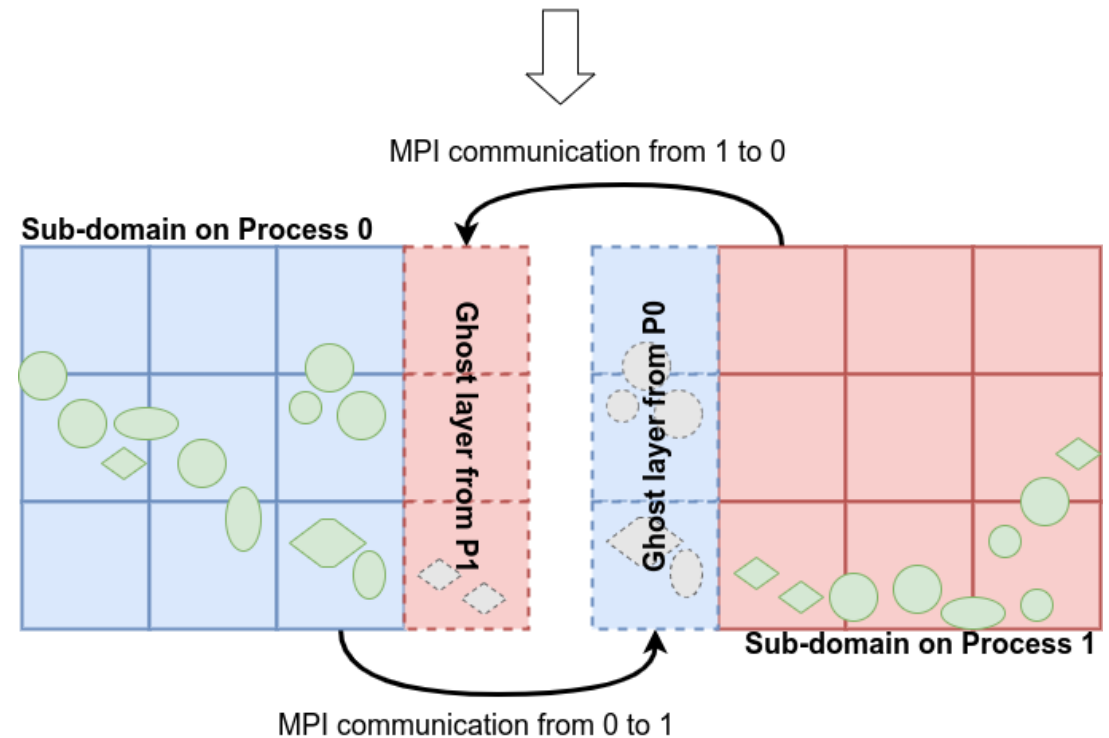
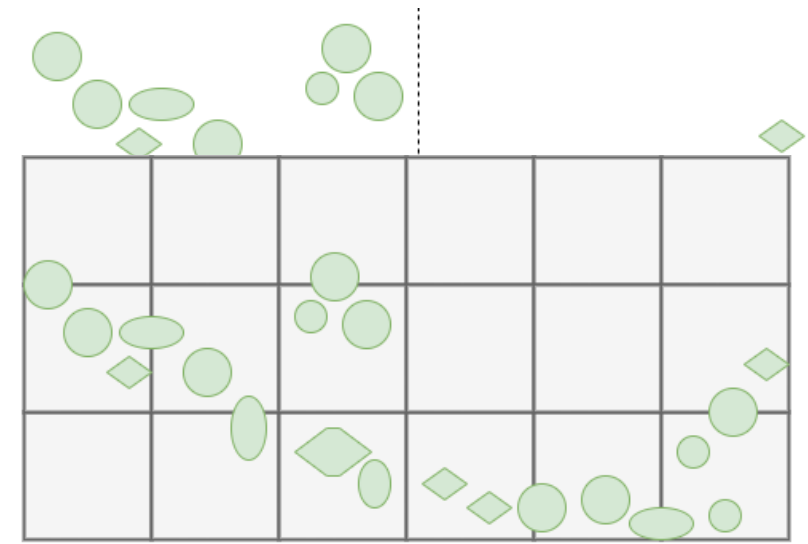
Domain Decomposition in XDEM

Decomposing the set of particles?

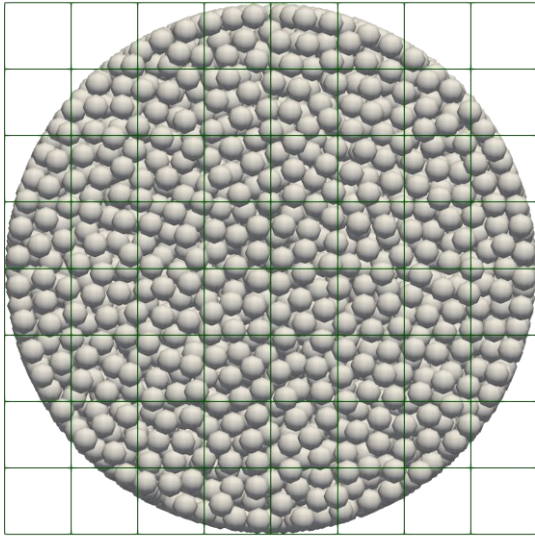
- Particles move during the simulation
 - Neighborhood relations change
 - Create undetected dependencies
- Would require frequent re-partitioning

Use a static regular grid to 'store' particles

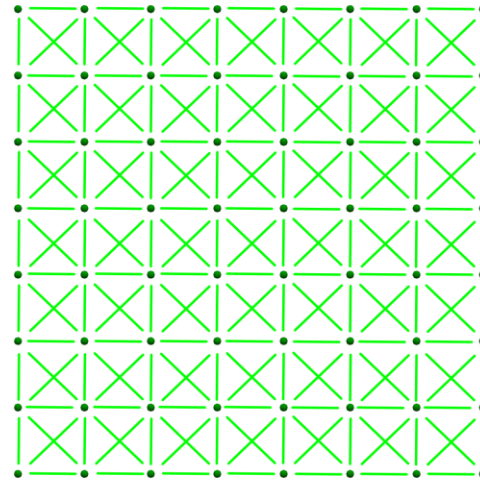
- Find location of a particle in constant time
 - Size of grid cells adapted for collision detection
 - No missing communication
- Re-partitioning only required in case of imbalance



Partitioning and Load-Balancing for XDEM

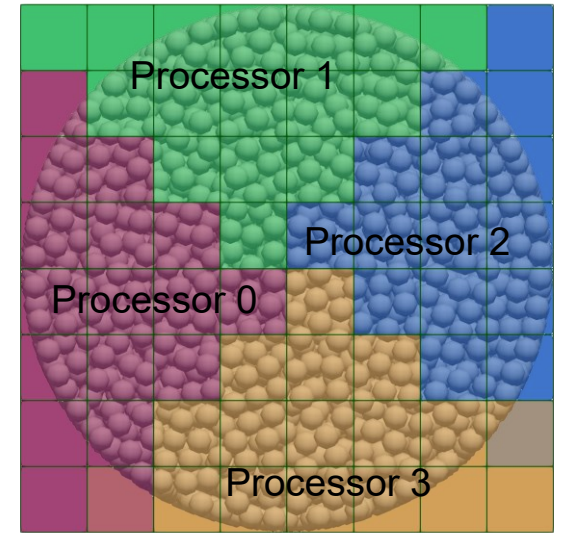


Particles in the cell grid



From grid to graph

- Node \leftarrow Cell
- Node weight $\leftarrow f(\text{nb particles})$
~ Computation cost
- Edge \leftarrow Neighborhood relation
- Edge weight $\leftarrow g(\text{nb particles})$
~ Communication cost
- Node Coordinates (topologic approaches)



Partitioning algorithm

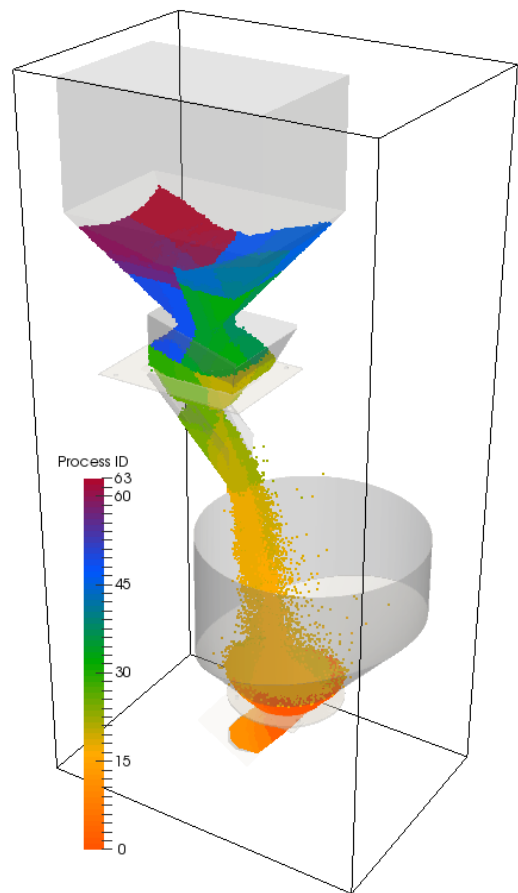
- Orthogonal Recursive Bisection
- METIS
- SCOTCH
- Zoltan PHG, RCB, RIB, ...
- etc.

Objectives

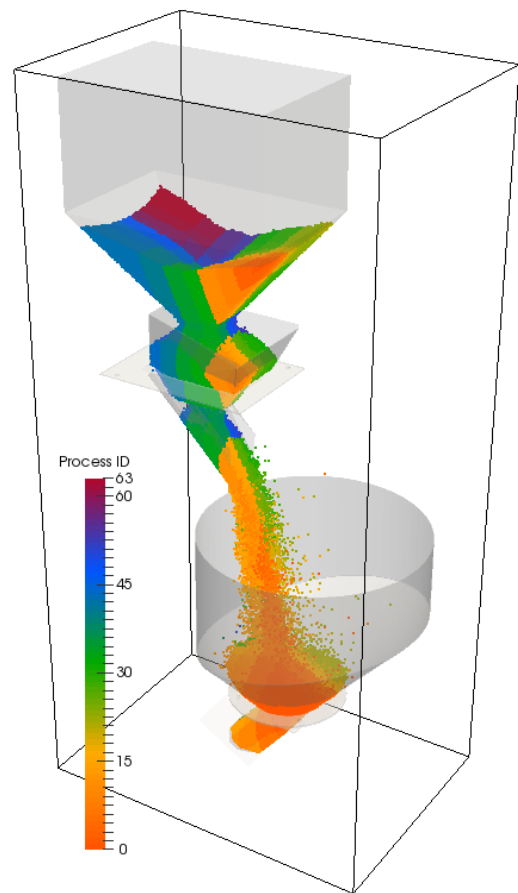
- Balance the computation cost
- Minimize the communication cuts



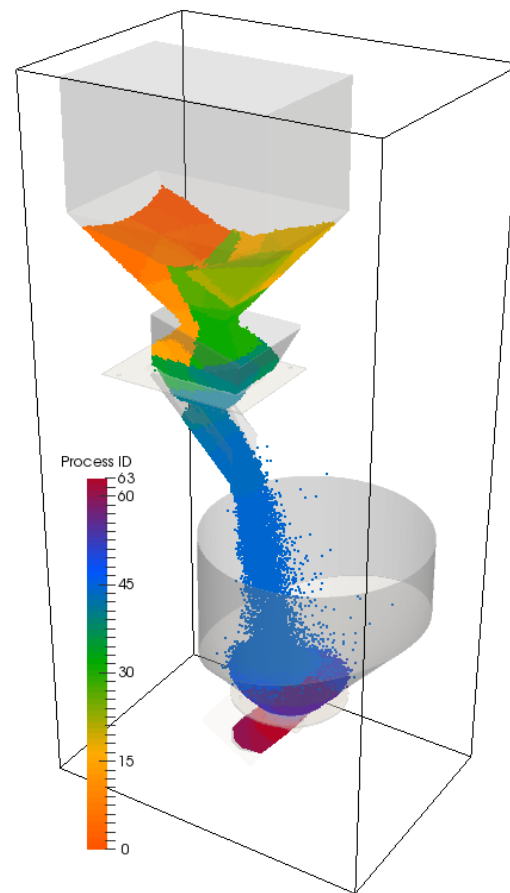
Example of Load-Balancing



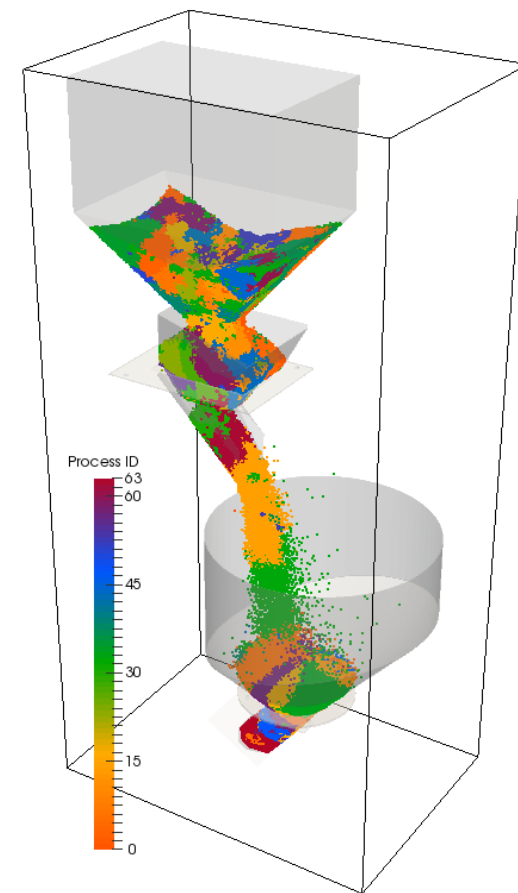
Zoltan RCB
(Recursive Coordinate Bisection)



ORB
(Orthogonal Recursive Bisection)



Zoltan RIB
(Recursive Inertial Bisection)



SCOTCH K-way



Workload Estimation for XDEM

Toward better Load-Balancing

Main Computations Phases in XDEM

Broad Phase: Fast but approximate scan to identify the pairs of particles that *could* interact

- uses an approximate shape (bounding volume)

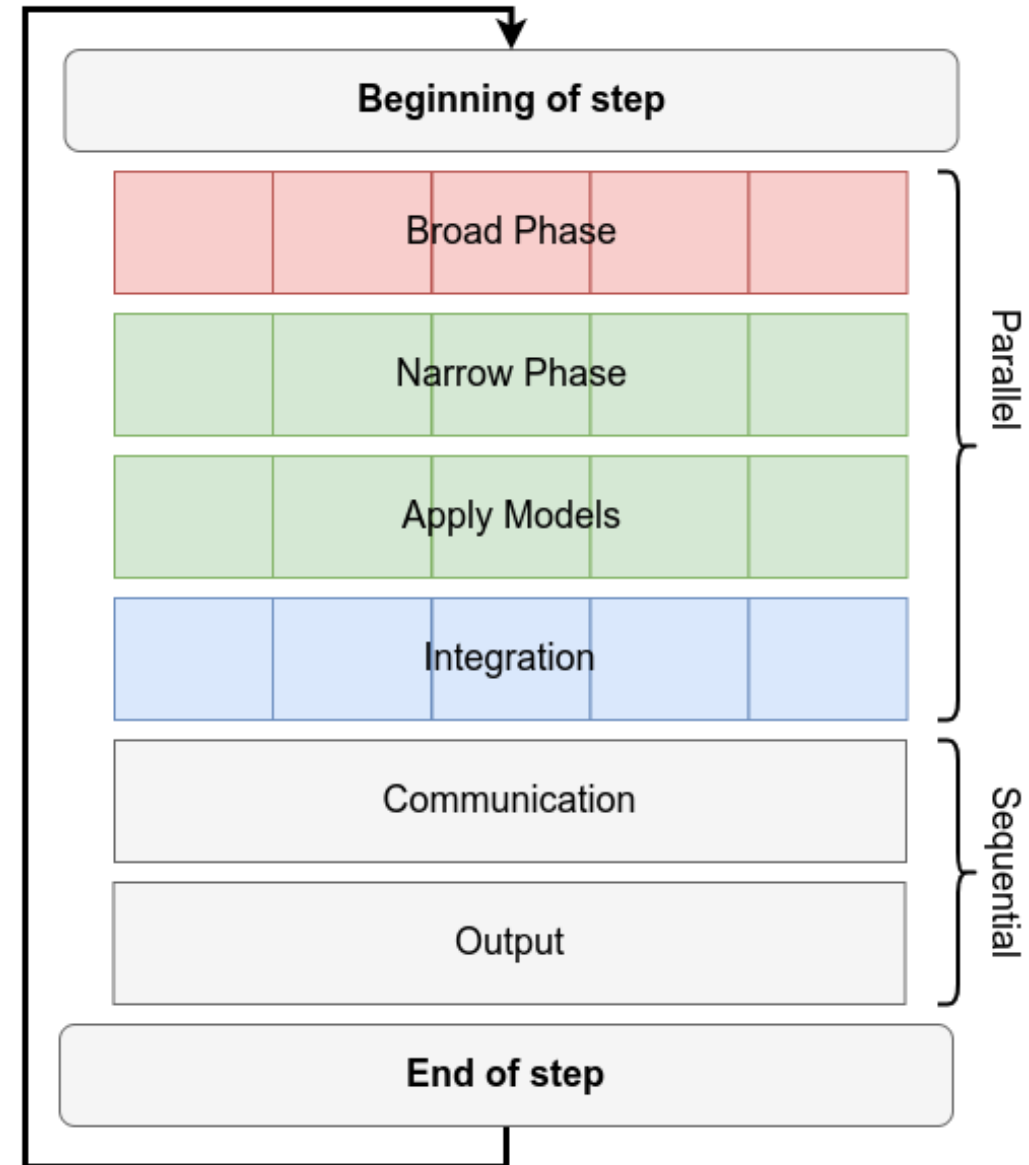
Narrow Phase: Precise collision detection on the particle pairs identified in the broad-phase

- uses the actual shape (sphere, cube, cylinder, etc.)
- calculates the distance/overlap between particles

Apply Models: Apply the physics models to each pair of interacting particles

- accumulate contributions to each particle:
Contact → *force, torque, ...*
Conduction/Radiation → *heat flux, ...*

Integration: Update the particle states by integrating the contributions from all the interacting partners



Weight estimation for load-balancing

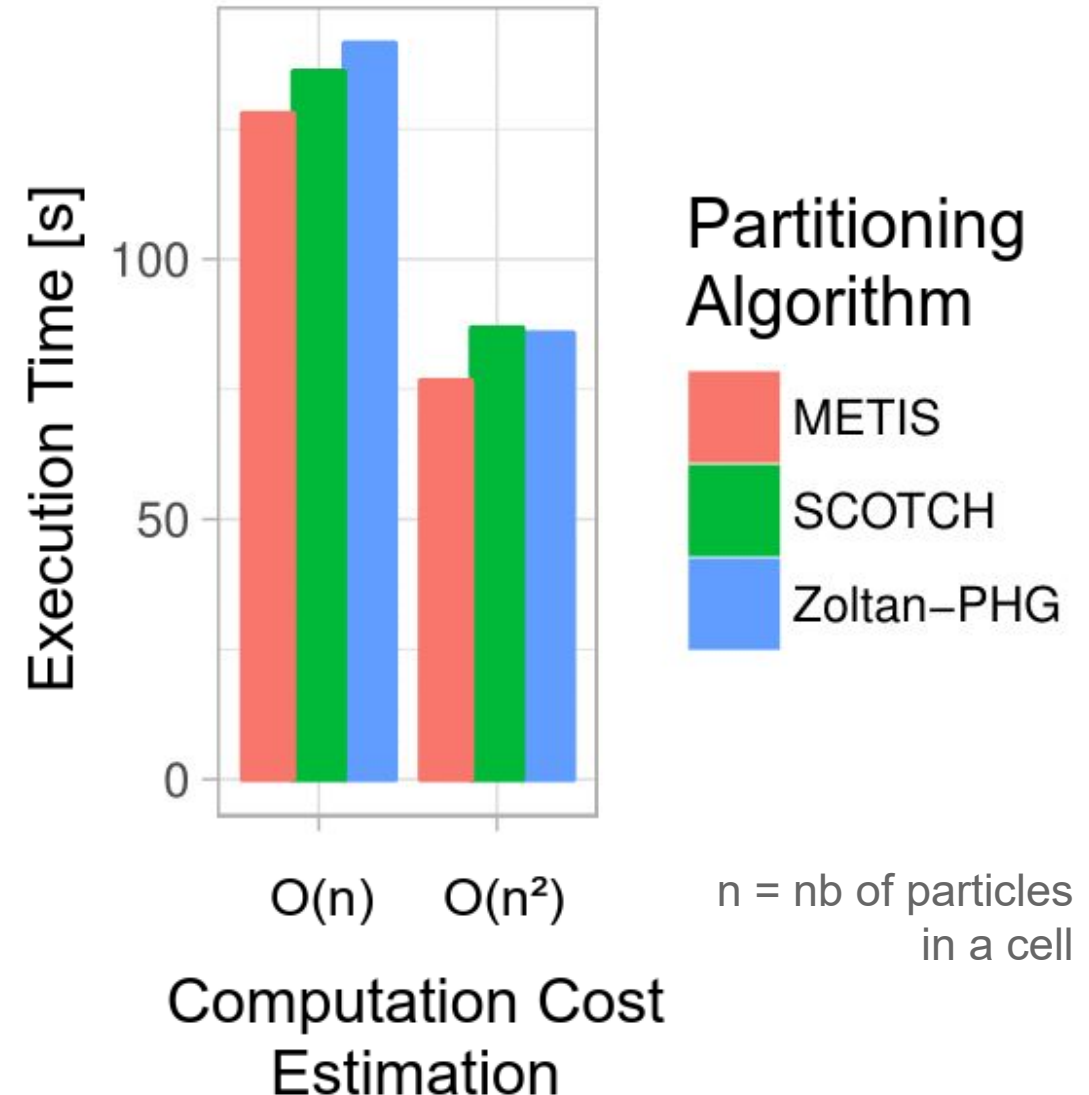
How to estimate the computing cost ?

- Difficult to measure at the level of a single cell
- Multiple phases and different complexities

<i>Computation Phase</i>	<i>Complexity</i>
Broad-phase	$O(\text{nb particles in cell}^2)$
Narrow-phase	$O(\text{nb interactions})$
Apply Models	$O(\text{nb interactions})$
Integration	$O(\text{nb particles})$

- Nb of interactions is difficult to estimate

→ **Workload estimation** has a significant impact on the **load-balancing** and on the **performance**

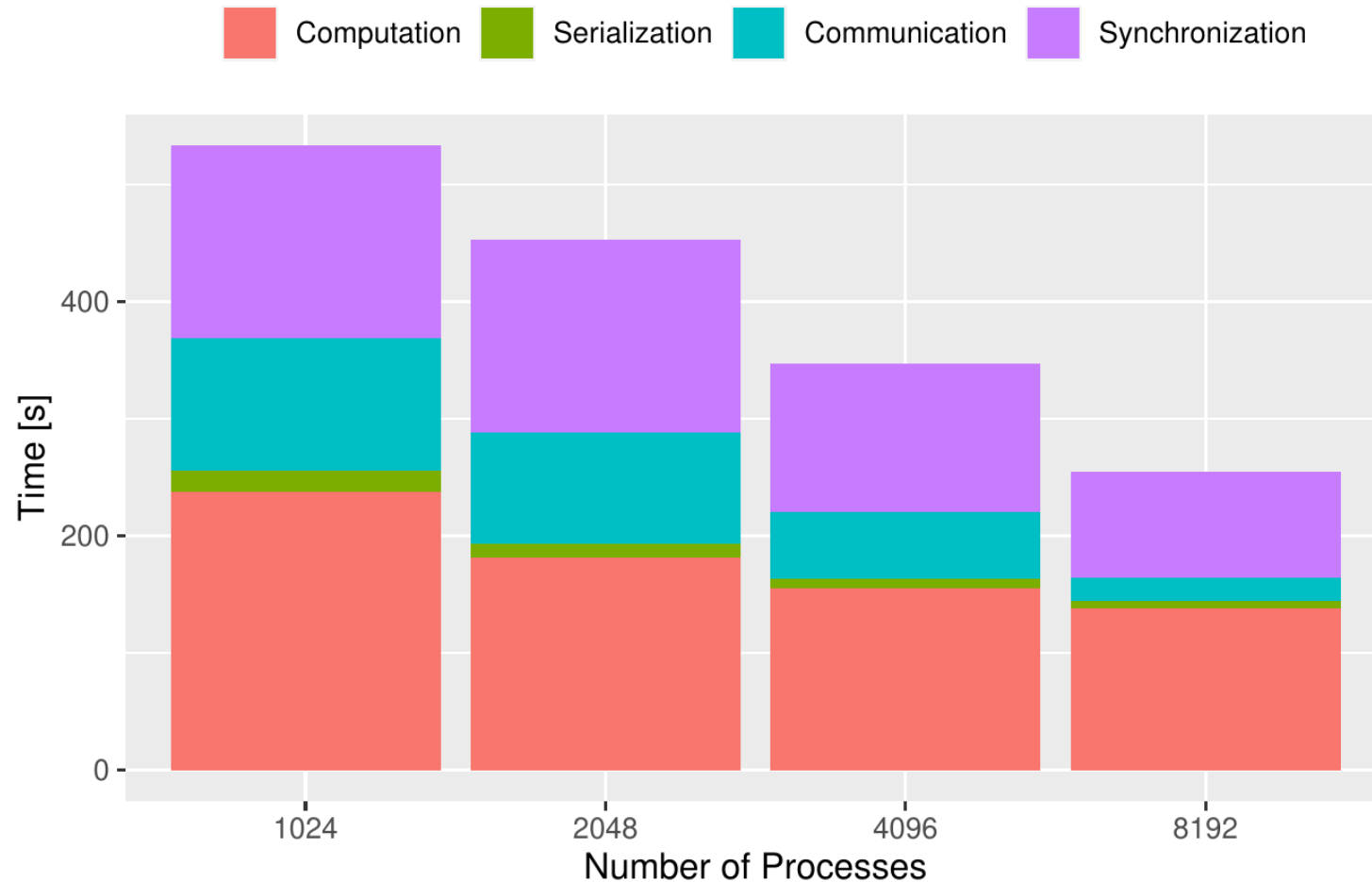


Preliminary Results

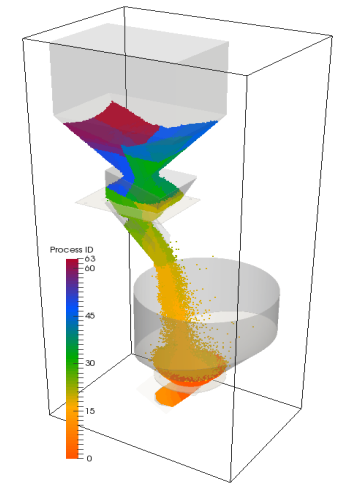
Load Estimation and Imbalance

Profiling large scale execution

- Use 'extra' synchronizations to isolate the phases in the execution



→ Time spent in synchronization indicates imbalance between the processes

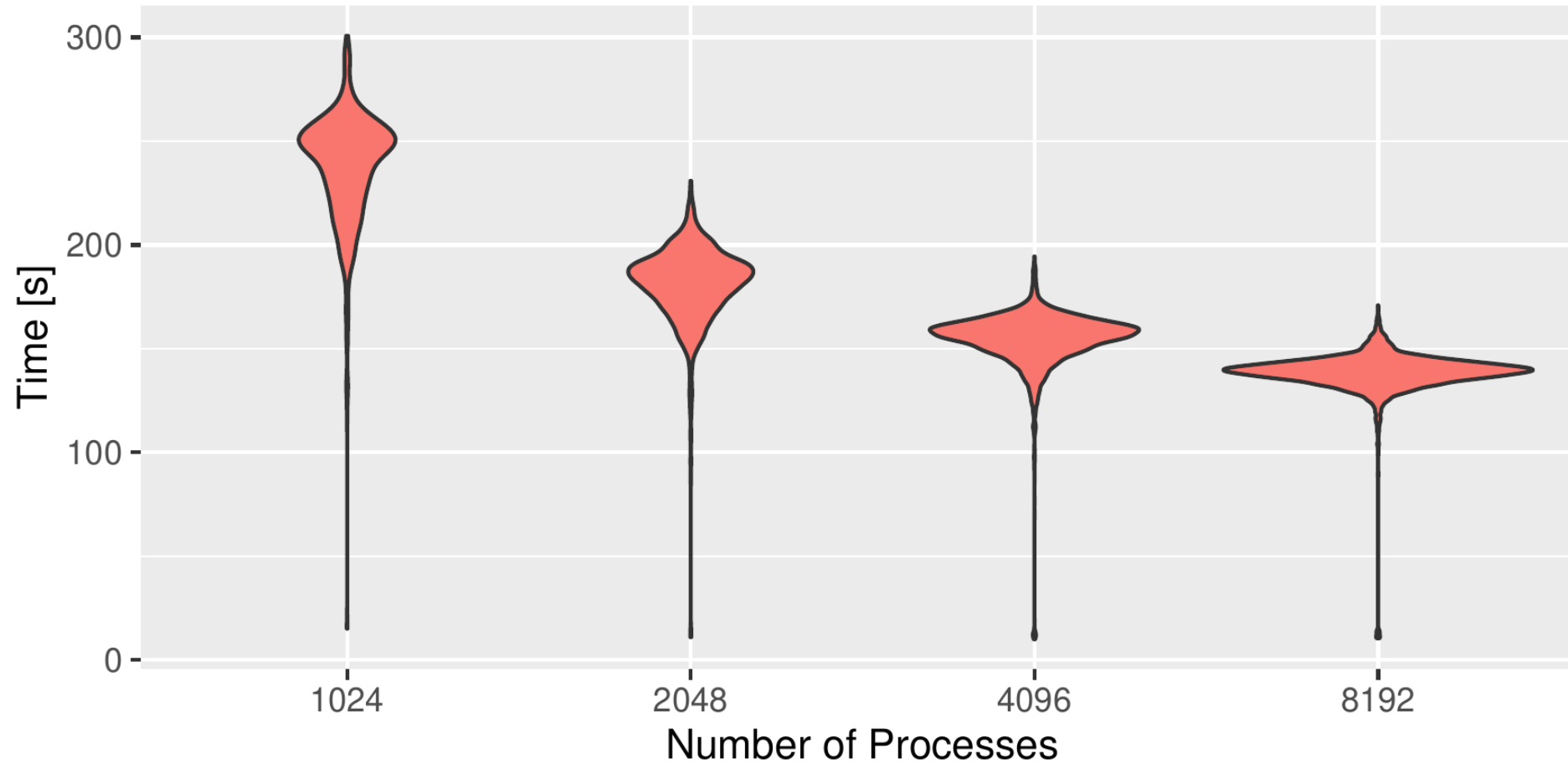


Hopper discharge
with 5.5M particles

1000 timesteps
Partitioner: Zoltan-RCB
Cost function: $1+n^2$

Measured Imbalance

Distribution of the computation time (excluding communication-related time)



Measured
Imbalance:

1.26

1.27

1.26

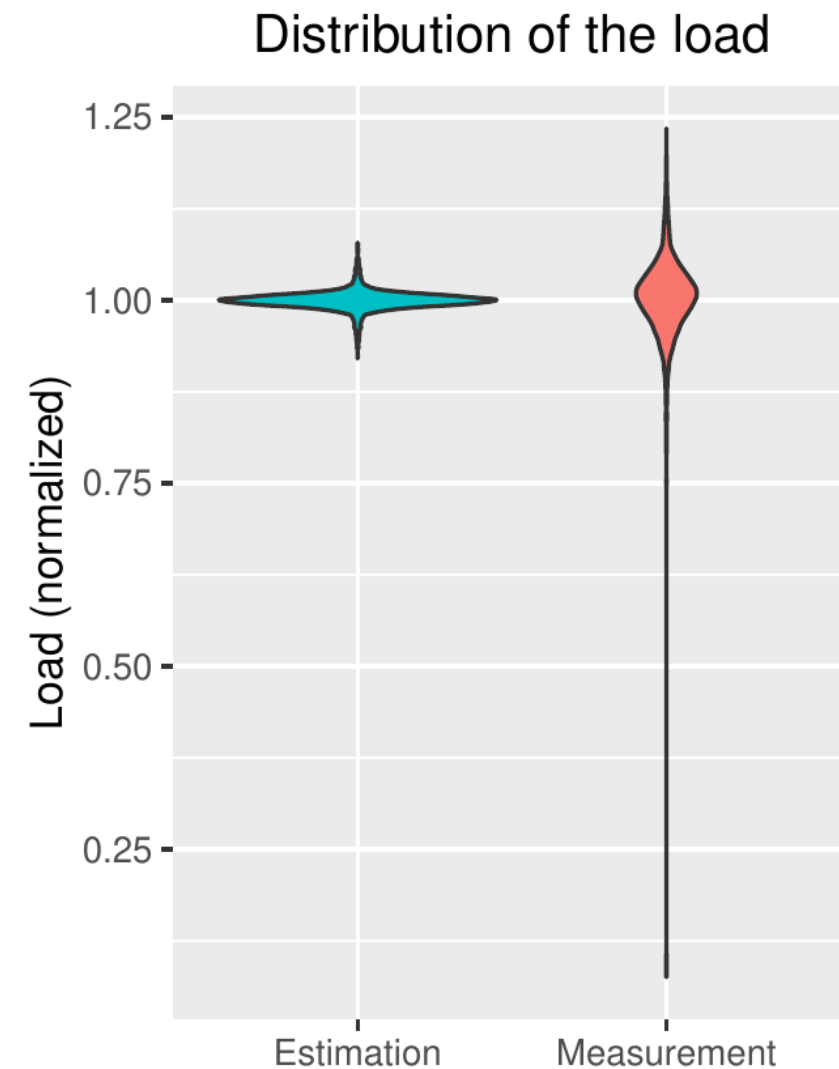
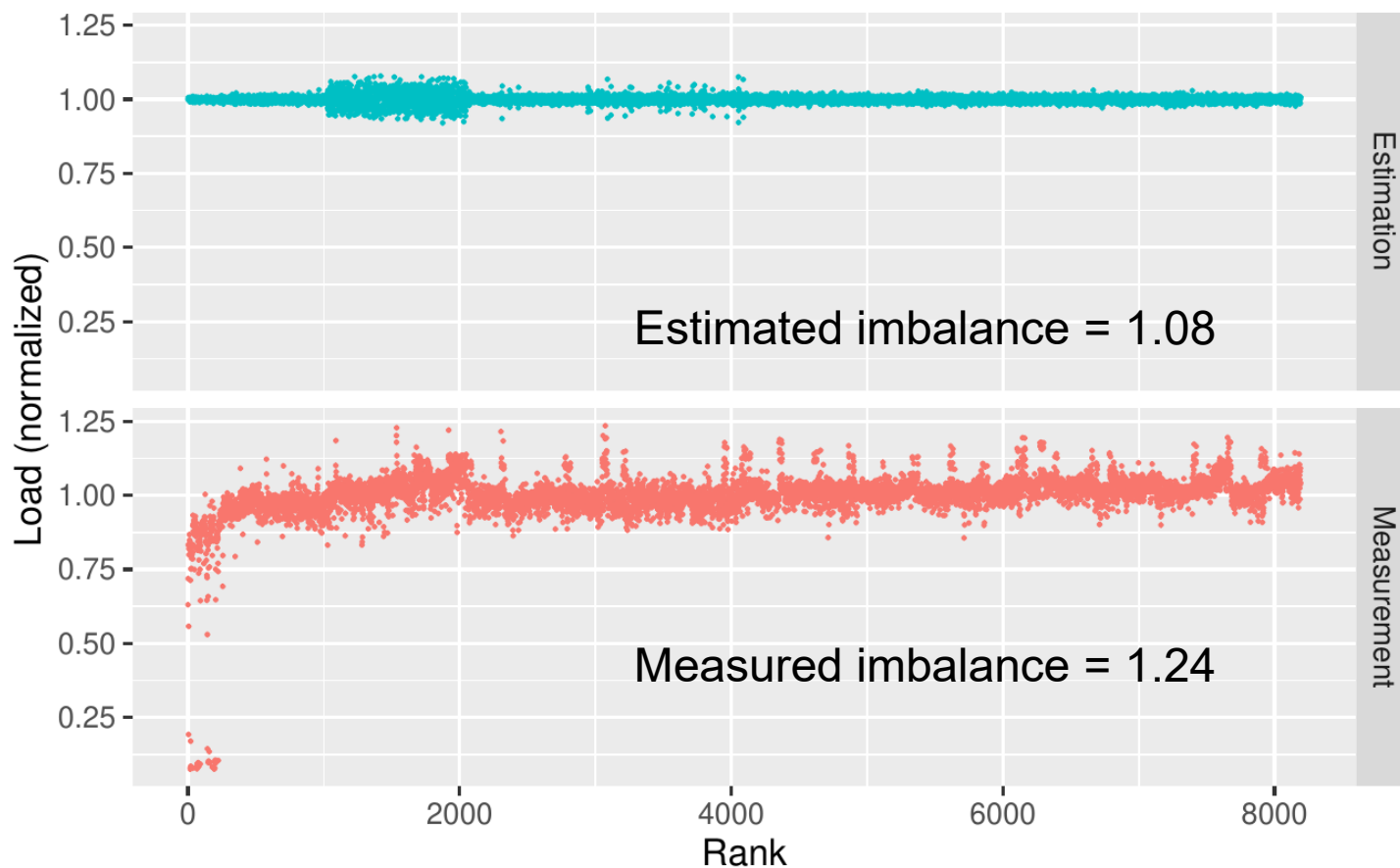
1.24



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Estimated Load vs Measured Load

Load for each process



- Discrepancy between the estimated and the measured load
- The load-balancing depends on a good load estimation

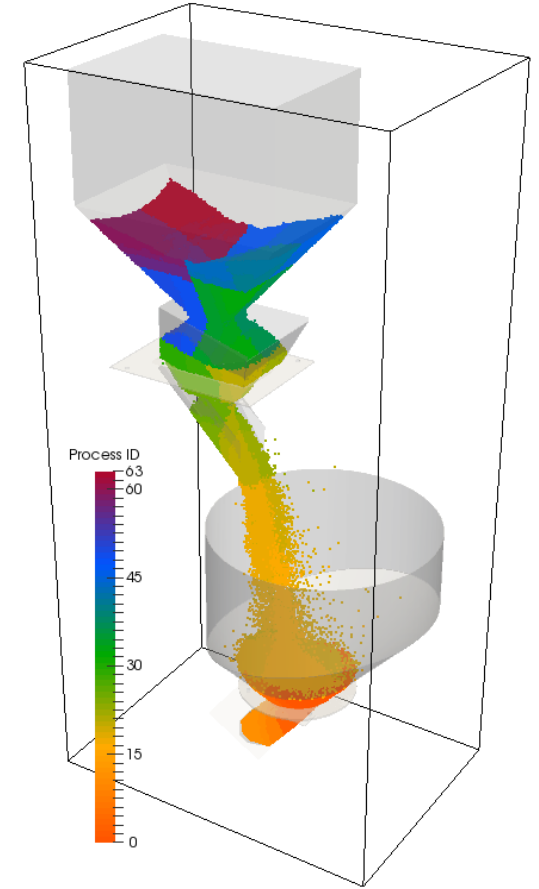
→ **Propose an accurate load estimation function for XDEM** (work-in-progress)

Thank you for your attention !

Question?

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University of Luxembourg

LuXDEM Research Team
<https://luxdem.uni.lu>



We acknowledge EuroHPC JU for awarding this project access to MeluXina.



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Period: Sep. 2023 – Aug. 2024
EuroHPC used: MeluXina



Some results presented in this research were carried out using the HPC facilities of the University of Luxembourg