

PAPER • OPEN ACCESS

Shortcuts to adiabaticity in Fermi gases

To cite this article: Pengpeng Diao *et al* 2018 *New J. Phys.* **20** 105004

View the [article online](#) for updates and enhancements.

You may also like

- [Maximizing entanglement in bosonic Josephson junctions using shortcuts to adiabaticity and optimal control](#)
Dionisis Stefanatos and Emmanuel Paspalakis
- [Shortcuts to adiabaticity: suppression of pair production in driven Dirac dynamics](#)
Sebastian Deffner
- [Realistic shortcuts to adiabaticity in optical transfer](#)
Gal Ness, Constantine Shkedrov, Yanay Florschheim *et al.*

Recent citations

- [Focus on Shortcuts to Adiabaticity](#)
Adolfo del Campo and Kihwan Kim



PAPER

Shortcuts to adiabaticity in Fermi gases

Pengpeng Diao¹, Shujin Deng^{1,2}, Fang Li¹, Shi Yu¹, Aurélie Chenu³, Adolfo del Campo^{3,4} and Haibin Wu^{1,2,5}¹ State Key Laboratory of Precision Spectroscopy, East China Normal University, Shanghai 200062, People's Republic of China² Collaborative Innovation Center of Extreme Optics, Shanxi University, Taiyuan 030006, People's Republic of China³ Theoretical Division, Los Alamos National Laboratory, Los Alamos, NM 87544, United States of America⁴ Department of Physics, University of Massachusetts, Boston, MA 02125, United States of America⁵ Author to whom any correspondence should be addressed.E-mail: hbwu@phy.ecnu.edu.cn**Keywords:** shortcuts to adiabaticity, unitary Fermi gas, quantum control, quantum thermodynamics, trapped ultracold gases, quantum dynamics, quantum frictionRECEIVED
9 July 2018REVISED
5 September 2018ACCEPTED FOR PUBLICATION
26 September 2018PUBLISHED
15 October 2018

Original content from this work may be used under the terms of the [Creative Commons Attribution 3.0 licence](#).

Any further distribution of this work must maintain attribution to the author(s) and the title of the work, journal citation and DOI.



Abstract

Shortcuts to adiabaticity (STA) provide an alternative to adiabatic protocols to guide the dynamics of the system of interest without the requirement of slow driving. We report the controlled speedup via STA of the nonadiabatic dynamics of a Fermi gas, both in the noninteracting and strongly coupled, unitary regimes. Friction-free superadiabatic expansion strokes, with no residual excitations in the final state, are demonstrated in the unitary regime by engineering the modulation of the frequencies and aspect ratio of the harmonic trap. STA are also analyzed and implemented in the high-temperature regime, where the shear viscosity plays a pivotal role and the Fermi gas is described by viscous hydrodynamics.

1. Introduction

Developing the ability to tailor the dynamics of complex quantum systems has been a long-time goal across a variety of fields. In addition, this goal is widely recognized as a necessity for the advancement of quantum technologies. However, the presence of strong correlations between constituent particles hinders the understanding and control of the time evolution of many-body systems. In view of this complexity barrier, emergent symmetries can play a pivotal role to simplify the dynamics far away from equilibrium and its control.

A paradigmatic test-bed of nonequilibrium many-body physics in the laboratory is provided by ultracold Fermi gases. Interatomic interactions in these systems can be considered of zero range. Using the Feshbach resonance technique [1], the strength of the interactions can be varied from zero value, creating an ideal Fermi gas, to a divergent interaction, leading to the unitary regime where the scattering length is infinite. Incidentally, these two extreme regimes are characterized by scale invariance as an emergent symmetry, which is broken for any finite value of the interaction strength. The appearance of scale invariance is crucial to describe the strongly-coupled unitary Fermi gas and leads to universality in the thermodynamics and hydrodynamics of the system [2–6]. Moreover, as a dynamical symmetry, scale invariance relates the time evolution of the unitary Fermi gas to equilibrium properties of the system. For instance, the evolution of local correlation functions such as the density profile of the system becomes self-similar. As a result, it can be simply described by a scaling of the coordinates with a time-dependent scaling factor. The connection between properties in- and out-of-equilibrium greatly reduces the complexity of the time evolution and has spurred developments in understanding intricate few-body and many-body dynamics. Beyond the study of Fermi gases, scale invariance has proved extremely useful in the exploration of ultracold atomic gases in time-dependent harmonic traps and provides the means to analyze time-of-flight (TOF) measurements [7, 8]. We can thus expect that it can be harnessed to provide fast control of quantum systems far-away from equilibrium.

Shortcuts to adiabaticity (STA) aim at speeding up the evolution of a system in a controlled way without the requirement of slow driving [9, 10]. As a general control tool, STA have found broad applications across a variety of fields, such as population transfer [9, 11–19], quantum thermodynamics [20–24], the control of critical

systems [25–30], and fast and robust quantum transport [31–33]. Several techniques have been developed for the design of STA. Counterdiabatic driving [11–14] constitutes a universal approach provided that the spectral properties of the system are known. When this is not the case, alternative methods are desirable. Prominent examples, with complementary advantages and varying range of applicability, include the fast-forward technique [31, 34, 35], the use of invariant of motions and scaling laws [9, 36–42], classical flow fields [43], the existence of Lax pairs in integrable systems [44], and counterdiabatic Born–Oppenheimer dynamics [45].

Progress to control trapped ultracold gases and many-body quantum fluids has been facilitated by the use of dynamical symmetries and the associated scaling laws [9, 36, 39, 41, 46–49]. In this context, STA were first demonstrated in the laboratory with a thermal atomic cloud [50], and soon after using a Bose–Einstein condensate, well described by mean field theory [51, 52]. Theoretical work indicated that STA could be applied to arbitrary quantum fluids with scale invariant symmetry [39, 41, 47, 49] and STA were later implemented to control an effectively one-dimensional atomic cloud with phase fluctuations [53]. Recently, we have demonstrated that STA can as well be applied in the strongly-coupled regime, using a three-dimensional (3D) anisotropic Fermi gas at unitarity as a test-bed [54]. The superadiabatic quantum friction suppression in finite-time thermodynamics has further been demonstrated in this system [24].

In this article, we present a detailed study of STA for the driving of Fermi gases both in the noninteracting regime and at unitarity. In particular, we show that it is possible to implement STA by engineering exclusively the time-dependent anisotropic trap, this is, without additional auxiliary controls. Further, we explore the superadiabatic control of a unitary Fermi gas in the high-temperature regime. At finite temperature, the shear viscosity cannot be neglected [6, 55], as it substantially affects the nonadiabatic dynamics of the system. The evolution can then be described by viscous hydrodynamics, and the well known ‘elliptic’ flow at unitarity [56] will be changed. While the effect of viscosity can limit the performance of STA in anisotropic expansions and compressions, it vanishes whenever the dynamics is isotropic. Our work shows that STA can be broadly applied in ultracold atomic gases across different interaction regimes and in the presence of viscosity.

The paper is organized as follows. In section 2 we characterize scale invariance as dynamical symmetry governing the dynamics of a Fermi gas at low temperature both in the noninteracting and unitary regimes. In section 3 we present the experimental demonstration of STA for the expansion and compression of a Fermi gas in the strongly interacting regime. The dynamics at high temperature, taking shear viscosity into consideration, is studied in section 4. We conclude with a summary and outlook in section 5.

2. Design of STA in ultracold Fermi gases

The noninteracting and unitary Fermi gases are both scale invariant, but with different scaling equations governing their dynamics. In the noninteracting case, the equations governing the evolution along different axes are decoupled due to the lack of collisions. By contrast, the dynamics along different axes are strongly coupled at unitarity.

2.1. Noninteracting Fermi gas

Consider a 3D noninteracting Fermi gas confined in a time-dependent anisotropic harmonic trap, described by the Hamiltonian

$$\hat{H}(t) = \sum_{i=1}^N \left[-\frac{\hbar^2}{2m} \nabla_i^2 + \frac{1}{2} m (\omega_x^2(t) \hat{x}_i^2 + \omega_y^2(t) \hat{y}_i^2 + \omega_z^2(t) \hat{z}_i^2) \right]. \quad (1)$$

We focus on the evolution of the system following a time-modulation of the trap frequencies ω_j ($j = x, y, z$) to induce an expansion or compression of the gas. The system exhibits scale invariance and the dynamics in this regime can be described by time-dependent scaling factors $b_j(t)$ ($j = x, y, z$) given by

$$b_x(t) = \left[\frac{\langle \hat{R}_x^2(t) \rangle}{\langle \hat{R}_x^2(0) \rangle} \right]^{\frac{1}{2}}, \quad b_y(t) = \left[\frac{\langle \hat{R}_y^2(t) \rangle}{\langle \hat{R}_y^2(0) \rangle} \right]^{\frac{1}{2}}, \quad b_z(t) = \left[\frac{\langle \hat{R}_z^2(t) \rangle}{\langle \hat{R}_z^2(0) \rangle} \right]^{\frac{1}{2}}. \quad (2)$$

Thus, the scaling factors are defined in terms of the variance of the collective coordinates

$$\hat{R}_x^2 = \sum_{i=1}^N \hat{x}_i^2, \quad \hat{R}_y^2 = \sum_{i=1}^N \hat{y}_i^2, \quad \hat{R}_z^2 = \sum_{i=1}^N \hat{z}_i^2, \quad (3)$$

measured in the state of the cloud, and describe the evolution of the density profile of the trapped atomic cloud that is formed by the ideal Fermi gas. Their dynamics is dictated by the uncoupled equations, for each Cartesian coordinate,

$$\ddot{b}_j + \omega_j^2(t)b_j = \frac{\omega_{j,0}^2}{b_j^3}, \quad (j = x, y, z), \quad (4)$$

with boundary conditions $b_j(0) = 1$ and $\dot{b}_j(0) = 0$. As a result, the evolution of the cloud size is completely determined by the time-dependent trapping frequencies.

A simplified scenario concerns the expansion from an isotropic trap, where a single scaling factor $b(t)$ suffices to completely describe the evolution of the system. For the cloud to follow a given desirable trajectory described by $b(t)$, the trap frequencies are to be modulated as [39, 47]

$$\omega_j^2(t) = \frac{\omega_{j,0}^2}{b^4} - \frac{\ddot{b}}{b}. \quad (5)$$

The existence of scaling laws thus makes it possible to control the dynamics of the system via STA, speeding up the adiabatic transfer between two many-body stationary states by controlling the aspect ratio of the frequencies [39, 47, 54].

An important application of STA is the engineering of thermodynamic processes to extract the maximum available work in the minimum possible time [20–23]. In a unitary process, the mean work equals the change in energy between the final and initial state [57]. To optimize a process using STA, it suffices to characterize the nonadiabatic mean-energy. For a noninteracting 3D Fermi gas, the different degrees of freedom decouple. The total energy is thus the sum of the individual energy along each degree of freedom. For the initial state $\langle H(0) \rangle = 3m\omega_0^2\sigma_0^2$, where σ_0 is the mean square cloud size, the adiabatic limit of equation (5) is reached when $\dot{\omega}(t)/\omega(t)^2 \ll 1$ [58]. Then, for a state initially at thermal equilibrium in an isotropic trap with frequency ω_0 , the adiabatic scaling factor is given by $b_{\text{ad}}(t) = \sqrt{\omega_0/\omega(t)}$. The nonadiabatic evolution of the mean energy $\langle H(t) \rangle$ and mean work $\langle W(t) \rangle$ read

$$\langle H(t) \rangle = \frac{Q^*(t)}{b_{\text{ad}}^2} \langle H(0) \rangle = Q^*(t) 3m\omega_0\omega(t)\sigma_0^2, \quad (6)$$

$$\langle W(t) \rangle = \langle H(t) \rangle - \langle H(0) \rangle = \left(Q^*(t) \frac{\omega(t)}{\omega_0} - 1 \right) \langle H(0) \rangle, \quad (7)$$

where $Q^*(t)$ is the nonadiabatic factor given by [22, 59]

$$Q^*(t) = b_{\text{ad}}^2 \left[\frac{1}{2b^2} + \frac{\omega(t)^2}{2\omega_0^2} b^2 + \frac{\dot{b}^2}{2\omega_0^2} \right]. \quad (8)$$

Note that in the adiabatic limit, $\dot{b} \approx 0$, the scaling factor $b(t)$ approaches its adiabatic value $b_{\text{ad}}(t) = \sqrt{\omega_0/\omega(t)}$ and the nonadiabatic factor $Q^*(t)$ equals unity. In this case, the mean energy is set by the adiabatic value corresponding to the instantaneous trap frequency, $\langle H(t) \rangle = \langle H(0) \rangle \omega(t)/\omega_0$, and no quantum friction exists. Values of $Q^*(t) > 1$ indicate deviations from adiabatic dynamics and can be associated with quantum friction [60], which vanishes whenever $Q^*(t) = 1$.

2.2. Unitary Fermi gas

The unitary Fermi gas is reached in the strongly-interacting regime, where the divergent scattering length at resonance leads to different dynamics from the noninteracting Fermi gas. A 3D unitary Fermi gas in a time-dependent anisotropic harmonic trap is described by the Hamiltonian

$$\hat{H}(t) = \sum_{i=1}^N \left[-\frac{\hbar^2}{2m} \nabla_i^2 + \frac{1}{2} m (\omega_x^2(t) \hat{x}_i^2 + \omega_y^2(t) \hat{y}_i^2 + \omega_z^2(t) \hat{z}_i^2) \right] + \sum_{i<j} U(\mathbf{r}_i - \mathbf{r}_j), \quad (9)$$

where $U(\mathbf{r}_i - \mathbf{r}_j)$ describes zero-range pairwise interactions with a divergent scattering length. In particular, $U(\mathbf{r}_i - \mathbf{r}_j)$ is a homogeneous function with the same scaling dimension as the kinetic energy operator. In contrast to the noninteracting Fermi gas, the dynamics along different axes for the strongly interacting Fermi gas at resonance is strongly coupled. The evolution of the cloud size at unitarity is governed by

$$\ddot{b}_j + \omega_j^2(t)b_j = \frac{\omega_{j,0}^2}{b_j \Gamma^{2/3}}, \quad (10)$$

where $b_j(t)$ (with $j = x, y, z$) are the scaling factors corresponding to this regime and $\Gamma(t) = b_x(t)b_y(t)b_z(t)$ is the scaling volume factor.

Our approach to realize the superadiabatic control of the Fermi gas is based on the counterdiabatic driving technique [22, 39], which relies on first designing a desirable reference adiabatic evolution and subsequently identifying the consistent conditions for it to describe the exact nonadiabatic quantum dynamics, in a predetermined time τ .

To design the reference evolution of the cloud, let $\{\omega_{j,0} | j = x, y, z\}$ denote the frequencies of the anisotropic harmonic trap at $t = 0$. Similarly, let $\{b_{j,\tau} | j = x, y, z\}$ denote the target scaling factors upon completion of an expansion or compression stroke of duration τ . The required boundary conditions are as follows

$$\begin{aligned}\omega_j(0) &= \omega_{j,0}, & \omega_j(\tau) &= \omega_{j,0}/b_j(\tau)^2, \\ \dot{\omega}_j(0) &= 0, & \dot{\omega}_j(\tau) &= 0, \\ \ddot{\omega}_j(0) &= 0, & \ddot{\omega}_j(\tau) &= 0.\end{aligned}$$

Satisfying these boundary conditions, we choose the time-dependent trap frequencies via the polynomial ansatz $\omega_j(t) = \omega_{j,0} \sum_n c_n \left(\frac{t}{\tau}\right)^n$,

$$\omega_j(t) = \omega_{j,0} + [\omega_j(\tau) - \omega_{j,0}] \left[10 \left(\frac{t}{\tau}\right)^3 - 15 \left(\frac{t}{\tau}\right)^4 + 6 \left(\frac{t}{\tau}\right)^5 \right]. \quad (11)$$

Using the adiabatic equations of motion, we determine the reference expansion factor as

$$b_j(t) = \frac{\omega_{j,0}}{\omega_j(t) \Gamma^{1/3}(t)} = \frac{\omega_{j,0}}{\omega_j(t)} \left[\frac{\nu(t)}{\nu(0)} \right]^{1/2}, \quad (12)$$

where $\nu(t) = [\omega_x(t)\omega_y(t)\omega_z(t)]^{1/3}$ is the geometric mean frequency.

The above equations describe the evolution in the adiabatic limit under slow driving. Nonetheless, they can describe as well the exact nonadiabatic dynamics under a modified driving protocol, associated with a different time-dependence of the trapping frequencies, i.e., replacing $\omega_j(t) \rightarrow \Omega_j(t)$ where the explicit form of $\Omega_j(t)$ is to be determined. This approach has been studied for the single-particle time-dependent harmonic oscillator and many-body quantum systems. It is generally referred to as local counterdiabatic driving (LCD) [22, 39, 42]. The required driving frequencies are given by

$$\begin{aligned}\Omega_j^2(t) &= \frac{\omega_{j,0}^2}{b_j^2 \Gamma^{2/3}} - \frac{\ddot{b}_j}{b_j} \\ &= \omega_j^2(t) - \frac{\ddot{b}_j}{b_j}.\end{aligned} \quad (13)$$

This yields the explicit expression for $\Omega_j^2(t)$ as [24]

$$\begin{aligned}\Omega_j^2(t) &= \omega_j^2 - 2 \left(\frac{\dot{\omega}_j}{\omega_j} \right)^2 + \frac{\ddot{\omega}_j}{\omega_j} - \frac{4}{9} \left(\frac{\dot{\Gamma}}{\Gamma} \right)^2 + 3 \frac{\ddot{\Gamma}}{\Gamma} - \frac{2}{3} \frac{\dot{\omega}_j \dot{\Gamma}}{\omega_j \Gamma} \\ &= \omega_j^2 - 2 \left(\frac{\dot{\omega}_j}{\omega_j} \right)^2 + \frac{\ddot{\omega}_j}{\omega_j} + \frac{1}{4} \left(\frac{\dot{\nu}}{\nu} \right)^2 - \frac{1}{2} \frac{\ddot{\nu}}{\nu} + \frac{\dot{\omega}_j \dot{\nu}}{\omega_j \nu},\end{aligned} \quad (14)$$

which includes the counterdiabatic corrections arising from the time-dependence of ω_j , the geometric mean ν and their coupling.

According to [24], the nonadiabatic factor and mean work read

$$Q^*(t) = \Gamma_{\text{ad}}^{2/3} \left[\frac{1}{2\Gamma^{2/3}} + \frac{1}{6} \sum_{j=x,y,z} \frac{\dot{b}_j^2 + \omega_j^2(t) b_j^2}{\omega_{j,0}^2} \right], \quad (15)$$

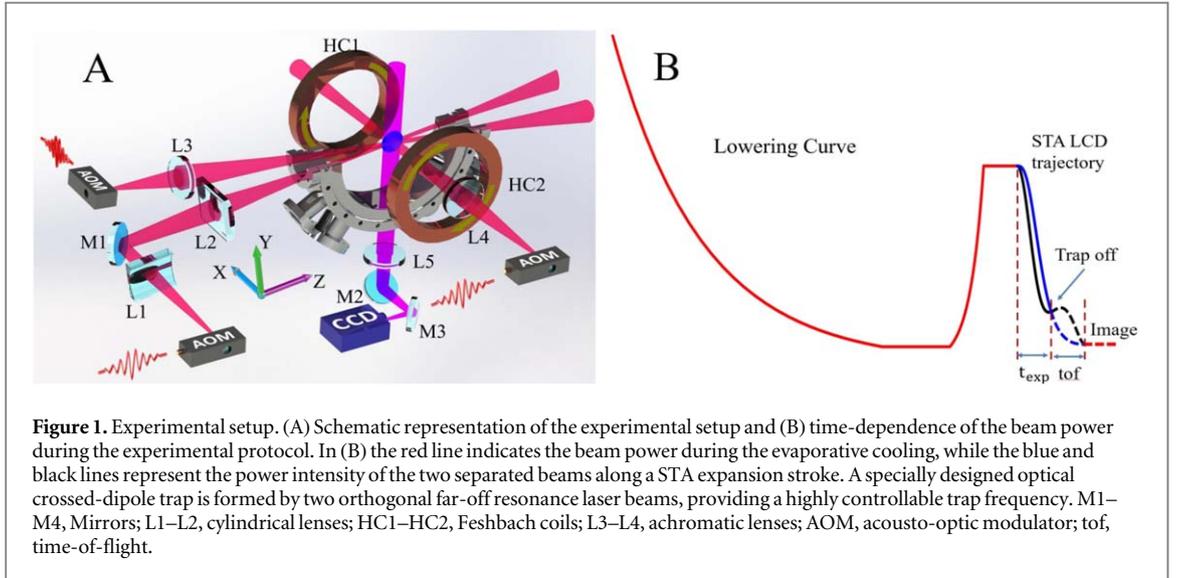
$$\langle W(t) \rangle = \langle H(t) \rangle - \langle H(0) \rangle = \left[\frac{1}{2\Gamma^{2/3}} + \frac{1}{6} \sum_{j=x,y,z} \frac{\dot{b}_j^2 + \omega_j^2(t) b_j^2}{\omega_{j,0}^2} - 1 \right] \langle H(0) \rangle. \quad (16)$$

The last equation follows from the fact that, for isolated quantum systems evolving under unitary dynamics, the (mean) work reduces to the difference in energy between the final and the initial state [57]. For the special case in which the time evolution is isotropic, the scaling factors are set by $b_j(t) = (\omega_{j,0}/\omega_j(t))^{1/2} = b(t)$, the volume scaling factor simplifies to $\Gamma(t) = b^3(t) = (\omega_{j,0}/\omega_j(t))^{3/2}$ and

$$\Omega_j^2(t) = \omega_j^2(t) - \frac{3}{4} \left[\frac{\dot{\omega}_j(t)}{\omega_j(t)} \right]^2 + \frac{1}{2} \frac{\ddot{\omega}_j(t)}{\omega_j(t)}. \quad (17)$$

The nonadiabatic factor $Q^*(t)$ and mean work $\langle W(t) \rangle$ are then given by

$$Q^*(t) = 1 + \frac{1}{12} \sum_{j=x,y,z} \left(\frac{\dot{\omega}_j}{\omega_j^3} - \frac{\ddot{\omega}_j}{\omega_j^4} \right), \quad (18)$$

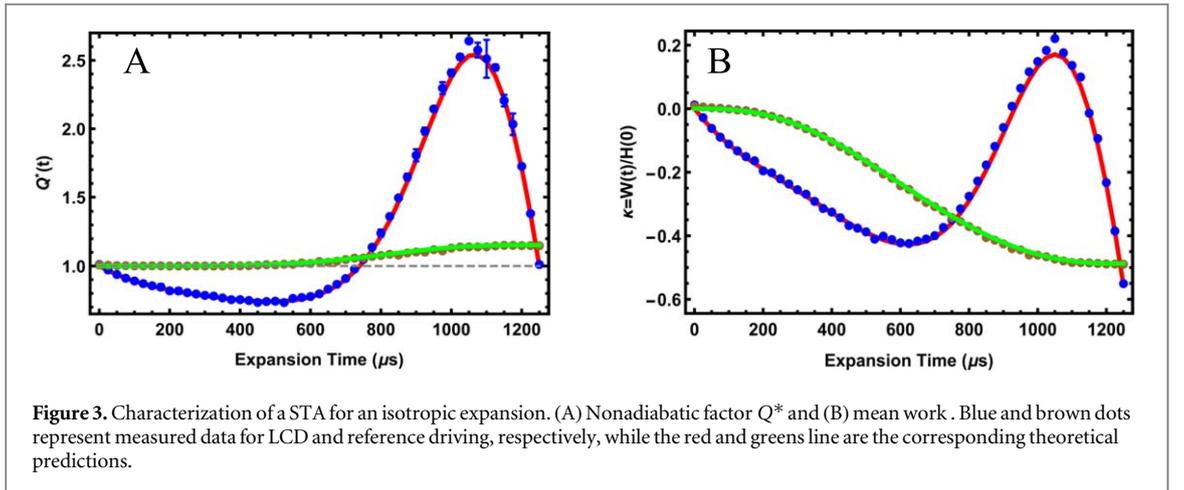
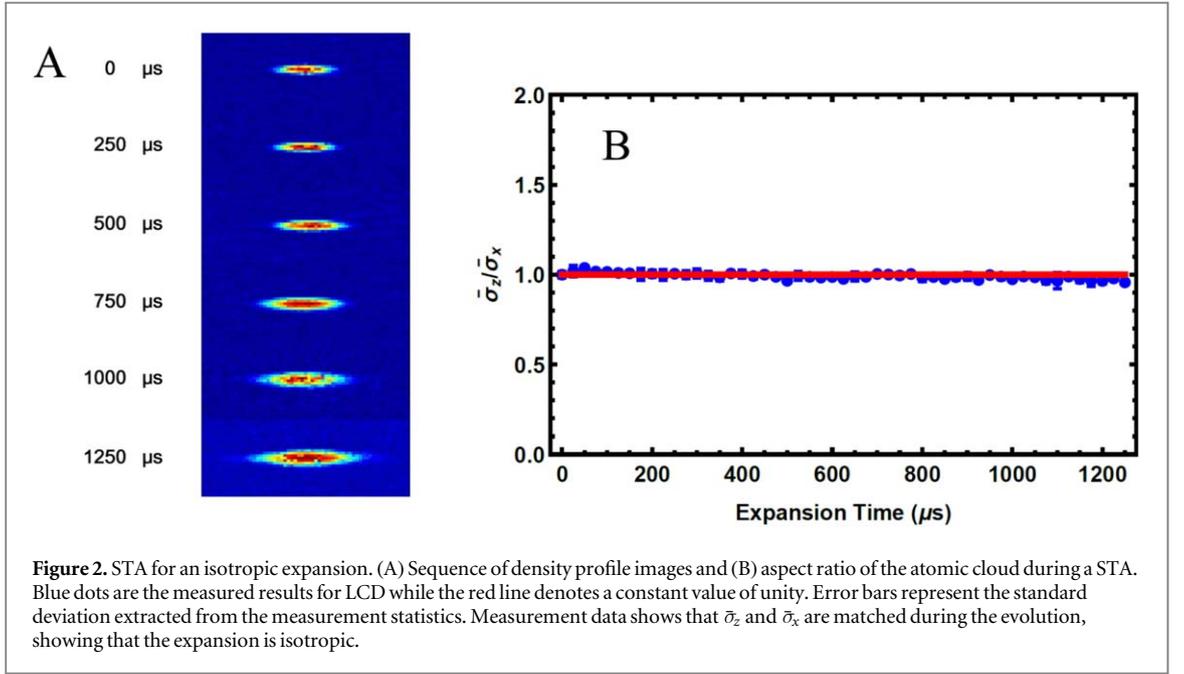


$$\langle W(t) \rangle = \left(\frac{Q^*(t)}{b_{\text{ad}}^2} - 1 \right) \langle H(0) \rangle. \quad (19)$$

3. Experimental implementation of STA in ultracold Fermi gases

Our experiment is implemented in a 3D anisotropically-trapped unitary quantum gas, made of a balanced mixture of ${}^6\text{Li}$ fermions in the lowest two hyperfine states $|\uparrow\rangle \equiv |F = 1/2, M_F = -1/2\rangle$ and $|\downarrow\rangle \equiv |F = 1/2, M_F = 1/2\rangle$. We probe the nonadiabatic expansion dynamics by varying in time the harmonic trap frequencies. The experimental setup is shown in figure 1, and is similar to that in [24]. The atoms are first loaded into an optical dipole trap formed by a single beam. A forced evaporation is performed to cool atoms to quantum degeneracy in an external magnetic field at 832 G. Then, the atoms are transferred to another dipole trap, which consists of an elliptic beam generated by a cylindrical lens along the z -axis and a nearly-ideal Gaussian beam along the x -axis. The resulting potential has a cylindrical symmetry around x . This trap facilitates the accurate tuning of the trap frequencies to control the anisotropy and geometry of the atomic cloud. A Feshbach resonance is used to tune the interaction of the atoms either to the noninteracting regime with the magnetic field $B = 528$ G or to the unitary limit with $B = 832$ G. The system is initially prepared in a stationary state of a normal fluid, with $\omega_x(0) = 2\pi \times 825$ Hz and $\omega_y(0) = \omega_z(0) = 2\pi \times 230$ Hz. The initial energy of the Fermi gas at unitarity is $E = 0.75(0.1)E_F$, corresponding to a temperature $T = 0.23(0.02)T_F$, where E_F and T_F are the Fermi energy and temperature of an ideal Fermi gas, respectively. Here we focus on the hydrodynamic expansion of a unitary Fermi gas, at the Feshbach resonance with magnetic field $B = 832$ G. To engineer an isotropic expansion in an anisotropic trap, the frequency aspect ratio needs to be controlled in the experiment (set up here at 3.59 at the beginning of a STA process). The target final value of the scaling factor $b(\tau)$ is chosen to be 1.5 in a transferring time $\tau = 1250$ μs . Snapshots of the density profile of the atomic cloud and its aspect ratio during the expansion are shown in figure 2. We engineer an isotropic expansion via LCD and define two time-dependent dimensionless cloud sizes, $\bar{\sigma}_z = \sigma_z(t)/\sigma_z(0)$ and $\bar{\sigma}_x = \sigma_x(t)/\sigma_x(0)$, to characterize the time evolution. It is clear that if the expansion is isotropic, $\bar{\sigma}_z/\bar{\sigma}_x$ should be equal to unity at all times. The measured data of the aspect ratio of the atomic cloud, presented in figure 2(b), confirms that the expansion is isotropic in spite of the anisotropy of the trap.

The evolution of the mean energy and mean work are also measured in this isotropic expansion and are shown in figure 3. For LCD, the nonadiabatic factor Q^* exhibits large deviations from unity—the adiabatic value—evidencing the nonadiabatic character of the evolution during the STA. Nonetheless, the final value at the transferring time τ equals unity, $Q^*(\tau) = 1$, revealing a friction-free transferring process at the end of the stroke. By contrast, for the chosen reference trajectory, Q^* gradually increases during the evolution and $Q^*(\tau) > 1$ upon completion of the protocol. Values of $Q^*(\tau) > 1$ for the reference driving indicate the presence of nonadiabatic excitations in the final state that can be associated with friction, as they are responsible for reducing the work output with respect to the LCD, see figure 3(b).



4. STA for a strongly interacting Fermi gas at high temperature

Our implementation of STA at low temperatures relies on the existence of scale-invariance, as manifested by equation (10) characterizing a superfluid Fermi gas. However, the hydrodynamics can exhibit quite a different behavior in the high-temperature regime, on which we focus next. The viscosity in this regime modifies substantially the dynamics and thus cannot be neglected. The cloud expansion and collective modes have been used to measure shear viscosity in the unitary Fermi gas [6, 55]. To describe the dynamics in the high-temperature regime, viscous hydrodynamics has been used in the scaling approximation [6, 55, 61]. The modified equations of motion for the scaling factors take the form [55]

$$\ddot{b}_j = \frac{\omega_{j,0}^2}{\Gamma^{2/3} b_j} [1 + C_Q(t)] - \frac{\hbar \langle \alpha_S \rangle \sigma_{jj}}{m \langle x_j^2 \rangle_0 b_j} - \omega_j^2(t) b_j, \quad (20)$$

where the coefficient $C_Q(t)$ is the fractional increase in the volume-integrated pressure arising from viscous heating and $\langle \alpha_S \rangle$ is the cloud-averaged shear viscosity coefficient, $\langle \dots \rangle$ denoting the average over the cloud density. The coefficients $C_Q(t)$ and diagonal elements of the viscous stress tensor σ_{jj} are specifically given by

$$\dot{C}_Q(t) = \frac{\Gamma^{2/3}}{\langle \mathbf{r} \cdot \nabla U_{\text{total}} \rangle_0} \hbar \langle \alpha_S \rangle \sum_j \sigma_{jj}^2, \quad (21)$$

$$\sigma_{jj} = 2 \left(\frac{\partial v_j}{\partial x_j} - \frac{1}{3} \nabla \cdot \mathbf{v} \right) = 2 \frac{\dot{b}_j}{b_j} - \frac{2}{3} \frac{\dot{\Gamma}}{\Gamma}, \quad (22)$$

since $v_j = x_j \dot{b}_j / b_j$ and $\nabla \cdot \mathbf{v} = \dot{\Gamma} / \Gamma$. Equation (20) approximates accurately the finite-temperature dynamics of a unitary Fermi gas when the viscosity is small and moments such as $\langle \alpha_S \rangle$ are well defined [55]. Note that both the viscosity heating rate coefficient $C_Q(t)$ and σ_{jj} are zero for an isotropic expansion with $b_x = b_y = b_z$. In this case, the equations of motion for the scaling factors given in equation (20) reduce to those of the superfluid unitary Fermi gas in equation (10). Therefore, the dynamical evolution of the cloud size is energy-independent. STA for isotropic expansions and compressions can thus be efficiently implemented via LCD in this regime, with the same protocols demonstrated in the previous section. Nonetheless, the TOF dynamics used to probe the cloud upon completion of the STA is modified. This is the case as the time evolution after switching off the trap is anisotropic. The presence of shear viscosity leads then to momentum transfer from the quickly expanding direction into the slowly expanding direction. This results in a slow decrease of the aspect ratio compared to the expansion in the superfluid regime.

Here we implement the LCD STA to study the nonadiabatic dynamics in the high-temperature regime at unitarity. This is tantamount to the implementation of a hot superadiabatic expansion stroke (e.g., in a quantum Otto cycle), of the kind proposed for friction-free quantum thermal machines [21, 22]. For simplicity, we consider an isotropic expansion stroke with the reference frequencies chosen as

$$\omega_j(t) = \omega_{j,0} \left[1 + 10[b_j(\tau)^{-2} - 1] \left(\frac{t}{\tau} \right)^3 - 15[b_j(\tau)^{-2} - 1] \left(\frac{t}{\tau} \right)^4 + 6[b_j(\tau)^{-2} - 1] \left(\frac{t}{\tau} \right)^5 \right], \quad (23)$$

where the expansion factor $b_j(\tau)$ is set as 1.5 and the transferring time $\tau = 1.5$ ms.

In this experiment, the trap depth is increased and the aspect ratio of the trap frequencies is about 22. Specifically, the system is initially prepared in a stationary state with harmonic trap frequencies $\omega_x = \omega_y = 2\pi \times 5581.5$ Hz and $\omega_z = 2\pi \times 252.7$ Hz. The harmonic trap potential U_0 is up to 229 μ K while the Fermi energy E_F is only about 6.5 μ K. With this setup, the anharmonic features of the trap are greatly suppressed. The initial energy of the Fermi gas at unitarity is $E = 0.78(0.1)E_F$, corresponding to a temperature $T = 0.24(0.02)T_F$.

Subsequently, the trap frequency is lowered by decreasing the laser intensity according to equations (17) and (23), and the trap anisotropy is precisely controlled by the power ratio of the two trap beams [24]. Finally, after a time of evolution in the time-dependent trap, the trap beams are completely turned off and the cloud is probed via standard resonant absorption imaging techniques after a TOF for expansion of $t_{\text{TOF}} = 500$ μ s. Each data point is an average over 5 shots taken with identical parameters. To prepare a higher temperature Fermi gas for comparison, the Fermi gas is parametrically heated up to $E = 2.47 E_F$ (corresponding to a temperature $T = 0.85 T_F$) with the same trap potential. Specifically, this is achieved by modulating the trap frequency with the resonant frequency. The TOF density profile along each direction is fitted by a Gaussian function as $A_0 + A_1 \exp(-x_j^2 / \sigma_j^2)$. From this fit, we obtain the observed cloud size $\sigma_{z,\text{obs}}$ and $\sigma_{r,\text{obs}}$ that we use to determine the in-trap cloud size $\sigma_{r,\text{in-trap}}(0)$ and $\sigma_{z,\text{in-trap}}(0)$ with the hydrodynamics theory.

In order to investigate the effect of shear viscosity on the dynamics at high temperature, we perform two types of experiments. We first observe the evolution of the mean square cloud size at different temperatures by suddenly switching off the trap after an isotropic STA expansion, i.e., implementing a TOF expansion, which corresponds to setting $\omega_j(t)$ for $(t > \tau)$ to zero in equation (20). In this case, both the viscosity heating rate coefficient $C_Q(t)$ and σ_{jj} are zero with $b_x(t) = b_y(t) = b_z(t)$ for $t > \tau$. Isotropic STA protocol for a high-temperature Fermi gas, in principle, should be the same as in the superfluid regime. However, the presence of shear viscosity will lead to momentum transfer from the radial direction into axial direction and result in a TOF dynamics quite different for different temperatures. The TOF expansion at the energy $E = 2.47 E_F$ and $E = 0.78 E_F$ are shown in figure 4. After releasing the atomic cloud from the cigar-shaped trap, the shear viscosity slows the flow in the initially-narrow, rapidly-expanding, x direction and transfers energy to the z direction along which the expansion is slower. For a fixed time after release, the cloud aspect ratio then decreases with increasing shear viscosity. Due to the large anisotropic frequency ratio, the expansion along the axial direction is very small and, as a result, does not exhibit significant variations for different energies, see figure 4(a). However, the gas experiences fast expansion along the radial direction, reaching a size about 20 times bigger than the initial one. This illustrates clearly the effect of increasing the shear viscosity, see figure 4(b). The small residual excitation following the STA is because the engineered frequency in the experiment differs slightly from the designed ideal trajectory.

In a second kind of experiment in the high-temperature regime, we investigate the influence of the shear viscosity on the anisotropic expansion. For a cylindrical symmetric dipole trap, the frequencies ω_x and ω_y should always be the same, meaning that the scaling factors fulfill $b_x(t) = b_y(t)$. Referring to equation (20) to implement a STA in a high-temperature unitary Fermi gas, the frequencies should satisfy

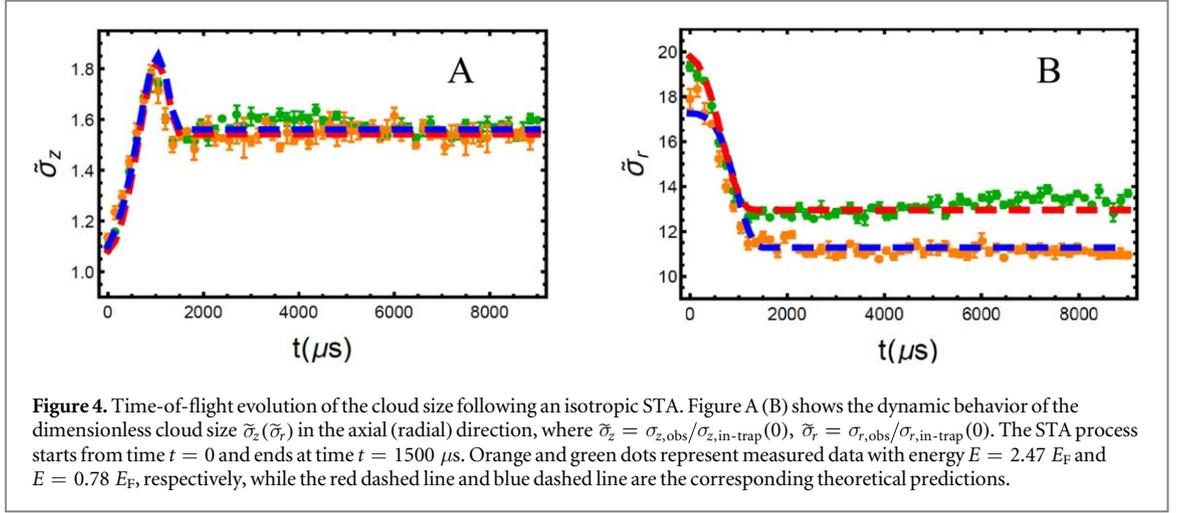


Figure 4. Time-of-flight evolution of the cloud size following an isotropic STA. Figure A (B) shows the dynamic behavior of the dimensionless cloud size $\bar{\sigma}_z$ ($\bar{\sigma}_r$) in the axial (radial) direction, where $\bar{\sigma}_z = \sigma_{z,\text{obs}}/\sigma_{z,\text{in-trap}}(0)$, $\bar{\sigma}_r = \sigma_{r,\text{obs}}/\sigma_{r,\text{in-trap}}(0)$. The STA process starts from time $t = 0$ and ends at time $t = 1500 \mu\text{s}$. Orange and green dots represent measured data with energy $E = 2.47 E_F$ and $E = 0.78 E_F$, respectively, while the red dashed line and blue dashed line are the corresponding theoretical predictions.

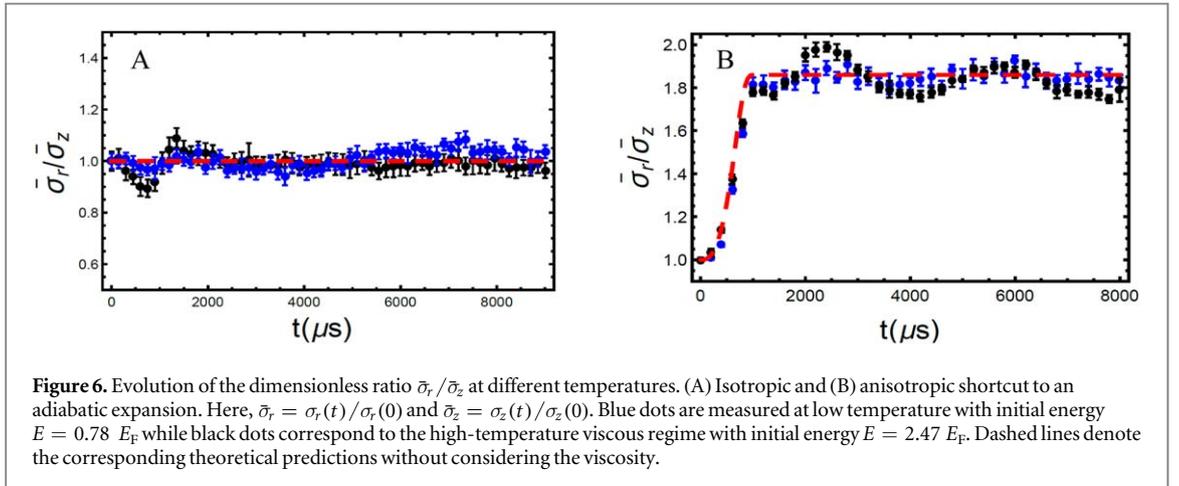
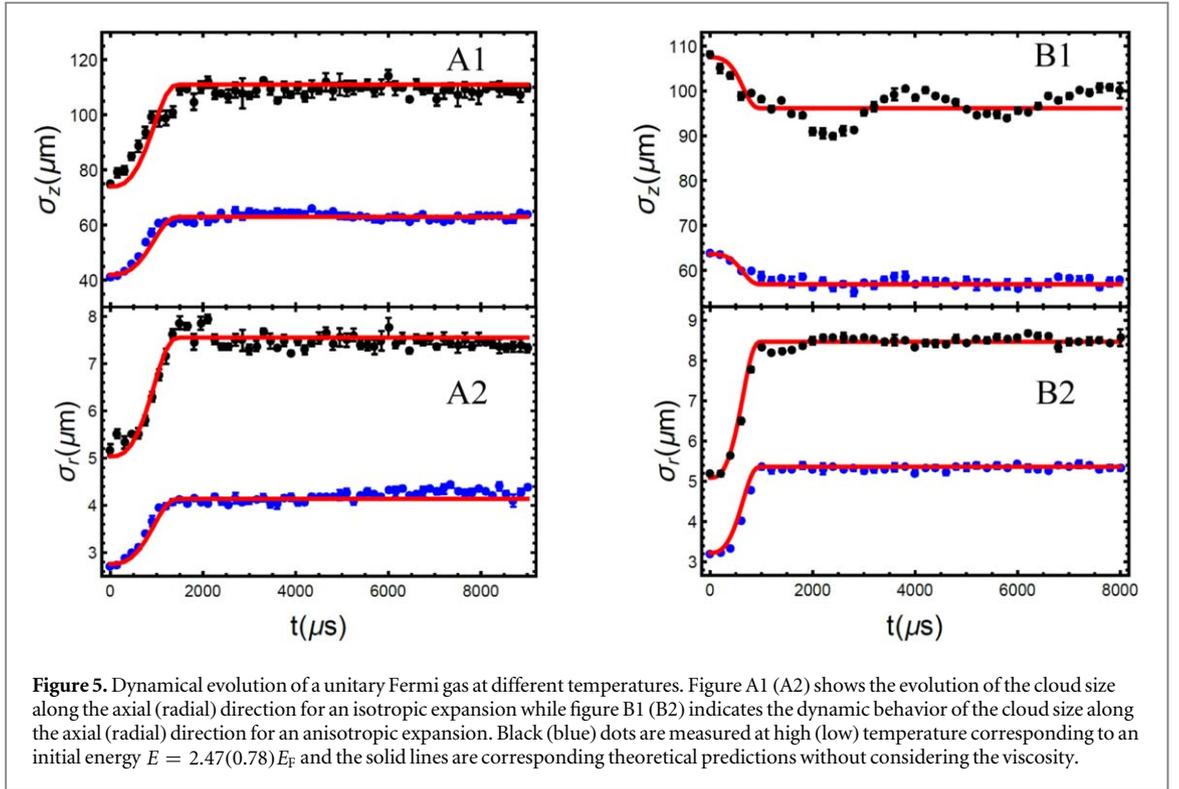
$$\Omega_j^2(t) = \frac{\omega_{j,0}^2}{\Gamma^{2/3} b_j^2} [1 + C_Q(t)] - \frac{\hbar \langle \alpha_S \rangle \sigma_{jj}}{m \langle x_j^2 \rangle_0 b_j^2} - \frac{\ddot{b}_j}{b_j}. \quad (24)$$

Here the trap-averaged shear viscosity and the viscous heating coefficient $C_Q(t)$ need to be determined to design the trap frequencies and aspect ratio. Although they have been precisely measured in equilibrium, the dynamics of the trap-averaged shear viscosity is very complex. As a result, we implement a STA by LCD that is guaranteed to work for a unitary Fermi gas with no viscosity, using equations (10) and (13), and study the deviations that arise due to the viscous hydrodynamics. To this end, we compare the dynamics in both isotropic and anisotropic STA protocols, for which the trap frequencies are chosen as follows

$$\begin{aligned} \text{Isotropic STA } \omega_z(0) &= 2\pi \times 252.7 \text{ Hz} \longrightarrow \omega_z(\tau) = 2\pi \times 112.3 \text{ Hz}, \\ &\omega_x(0) = 2\pi \times 5\,581.5 \text{ Hz} \longrightarrow \omega_x(\tau) = 2\pi \times 2\,480.7 \text{ Hz}, \\ \text{Anisotropic STA } \omega_z(0) &= 2\pi \times 252.7 \text{ Hz} \longrightarrow \omega_z(\tau) = 2\pi \times 208.8 \text{ Hz}, \\ &\omega_x(0) = 2\pi \times 5\,581.5 \text{ Hz} \longrightarrow \omega_x(\tau) = 2\pi \times 2\,480.7 \text{ Hz}. \end{aligned}$$

The aspect ratio of the target stationary state for an anisotropic expansion is 11.9. For comparison, the STA trajectories are implemented with the energies of $E = 2.47 E_F$ and $E = 0.78 E_F$, respectively; see figure 5. For the isotropic expansion, the dynamics along different directions shares the same behavior, shown in figure 5 A1 and A2. The viscosity rarely affects the dynamic evolution even at a quite high temperature with energy values up to $2.47 E_F$. By contrast, the anisotropic expansion dynamics, where $b_x = b_y \neq b_z$, shows different behavior with increasing viscosity for different energy values. The STA for the anisotropic expansion works well at low temperatures. In the strongly coupled regime, the cloud size in the axial direction behaves as in a compression stroke, since the frequency in the radial direction decreases faster and the energy would ‘flow’ into the radial direction. The experimental results are consistent with the theoretical calculation using equation (10). However, the dynamical behavior of the axial direction exhibits an excitation at high temperature, while the radial behavior is still consistent with the theoretical prediction. The large deviation between b_x and b_z would result in a constant increase of the viscous heating coefficient $C_Q(t)$. When the viscosity coefficient $\langle \alpha_S \rangle$ is large and $\frac{\hbar \langle \alpha_S \rangle \sigma_{jj}}{m \langle x_j^2 \rangle_0 b_j^2}$ becomes comparable to the square of the frequency, the STA trajectory should be corrected according to equation (24). Neglecting the contribution of viscosity, the expansion stroke does not satisfy the boundary conditions and thus exhibits some excitation after the transferring time. Since the frequency aspect ratio is very large, the contribution of the viscosity in the radial direction is smaller than the square of the frequency. We could hardly see the deviation of the expansion behavior away from its theoretical calculation in the radial direction, which is shown in figure 5 B2.

To further compare the dynamic of the atomic cloud for the isotropic and anisotropic expansion, the dimensionless cloud size $\bar{\sigma}_j = \sigma_j(t)/\sigma_j(0)$ is shown in figure 6. The ratio of $\bar{\sigma}_r/\bar{\sigma}_z$ is very close to one and the system remains at thermal equilibrium when the STA driving is completed. For different energies at different times, the ratio $\bar{\sigma}_r/\bar{\sigma}_z$ keeps a constant value closed to unity as shown in figure 6(A). The slight deviation in the experimental data (black dots) during the nonadiabatic transfer is due to the large viscosity. The anisotropic expansion shown in figure 6(B) is largely dependent on the energy. When the energy is low and the viscosity can be neglected, the ratio $\bar{\sigma}_r/\bar{\sigma}_z$ remains constant, keeping aspect ratio $b_x(\tau)/b_x(0) = 1.86$. However, $\bar{\sigma}_r/\bar{\sigma}_z$ oscillates for high energy due to the presence of the viscosity. Further, contrary to the superfluid case, residual excitations of the breathing mode are damped as a function of time due to the viscous hydrodynamics.



5. Conclusions

In conclusion, we have studied the control of the nonadiabatic expansion dynamics of an interacting Fermi gas in both the noninteracting and unitary regimes. To this end, we have engineered STA by counterdiabatic driving exploiting scale-invariance as an emergent dynamical symmetry in these two limits. By doing so, the cloud size follows a prescribed adiabatic trajectory without the requirement of slow driving that can be used to implement a superadiabatic transition between two different stationary quantum states. Superadiabatic expansions can be applied in a variety of scenarios to control and manipulate ultracold gases. They can be used as a dynamical microscope to probe the state of the atomic cloud [47, 62] as well as to implement friction-free superadiabatic strokes in quantum thermodynamics [20–23].

For the 3D anisotropic ideal Fermi gas, we have implemented STA via an isotropic nonadiabatic expansion. These shortcuts rely on engineering a unique scaling factor describing the expansion of the atomic cloud along all different axes, as a function of time. Their implementation is possible even in the resonant regime, thanks to the individual control of the trap frequencies as well as their aspect ratio, using the technique proposed in [24].

We have also investigated STA at high temperature for a unitary Fermi gas in a time-dependent anisotropic trap. The TOF dynamics is changed as the increasing shear viscosity transfers the momentum from the quickly expanding direction into the slowly expanding direction. By comparing the dynamical evolution along a

shortcut to adiabaticity for isotropic and anisotropic expansions, we have demonstrated the impact of the shear viscosity on the nonadiabatic dynamics and its effect on the residual excitation of the breathing modes of the cloud.

Acknowledgments

This research is supported by the National Key Research and Development Program of China (grant no.2017YFA0304201), National Natural Science Foundation of China (NSFC) (grant nos. 11734008, 11374101, 91536112, and 11621404), Program of Shanghai Subject Chief Scientist (17XD1401500), the Shanghai Committee of Science and Technology (17JC1400500), UMass Boston (project P20150000029279) and the John Templeton Foundation. AdC acknowledges partial support from Institut Henri Poincaré and CNRS via the thematic trimester at the Centre Émile Borel entitled ‘Measurement and control of quantum systems: theory and experiments’ in Spring 2018.

References

- [1] Chin C, Grimm R, Julienne P and Tiesinga E 2010 *Rev. Mod. Phys.* **82** 1225–86
- [2] Ku M J H, Sommer A T, Cheuk L W and Zwierlein M W 2012 *Science* **335** 563–7
- [3] Kinast J, Turlapov A, Thomas J E, Chen Q, Stajic J and Levin K 2005 *Science* **307** 1296–9
- [4] Ho T L 2004 *Phys. Rev. Lett.* **92** 090402
- [5] Makotyn P, Klauss C E, Goldberger D L, Cornell E A and Jin D S 2014 *Nat. Phys.* **10** 116
- [6] Cao C, Elliott E, Joseph J, Wu H, Petricka J, Schäfer T and Thomas J E 2011 *Science* **331** 58–61
- [7] Castin Y and Dum R 1996 *Phys. Rev. Lett.* **77** 5315–9
- [8] Kagan Y, Surkov E L and Shlyap–nikov G V 1996 *Phys. Rev. A* **54** R1753–6
- [9] Chen X, Lizuain I, Ruschhaupt A, Guéry-Odelin D and Muga J G 2010 *Phys. Rev. Lett.* **105** 123003
- [10] Torrontegui E, Ibáñez S, Martínez-Garaot S, Modugno M, del Campo A, Guéry-Odelin D, Ruschhaupt A, Chen X and Muga J G 2013 Shortcuts to adiabaticity *Advances in Atomic, Molecular, and Optical Physics* ed E Arimondo et al vol 62 (New York: Academic) ch 2, pp 117–69
- [11] Demirplak M and Rice S A 2003 *J. Phys. Chem. A* **107** 9937
- [12] Demirplak M and Rice S A 2005 *J. Phys. Chem. B* **109** 6838
- [13] Demirplak M and Rice S A 2008 *J. Chem. Phys.* **129** 154111
- [14] Berry M V 2009 *J. Phys. A: Math. Theor.* **42** 365303
- [15] Ruschhaupt A, Chen X, Alonso D and Muga J G 2012 *New J. Phys.* **14** 093040
- [16] Zhang J et al 2013 *Phys. Rev. Lett.* **110** 240501
- [17] Masuda S and Rice S A 2015 *J. Phys. Chem. A* **119** 3479–87
- [18] Du Y X, Liang Z T, Li Y C, Yue X X, Lv Q X, Huang W, Chen X, Yan H and Zhu S L 2016 *Nat. Commun.* **7** 12479
- [19] Chen Y H, Shi Z C, Song J, Xia Y and Zheng S B 2017 *Phys. Rev. A* **95** 062319
- [20] Deng J, Wang Q-H, Liu Z, Hänggi P and Gong J 2013 *Phys. Rev. E* **88** 062122
- [21] del Campo A, Goold J and Paternostro M 2014 *Sci. Rep.* **4** 6208
- [22] Beau M, Jaramillo J and del Campo A 2016 *Entropy* **18** 168
- [23] Funo K, Zhang J N, Chatou C, Kim K, Ueda M and del Campo A 2017 *Phys. Rev. Lett.* **118** 100602
- [24] Deng S, Chenu A, Diao P, Li F, Yu S, Coulamy I, del Campo A and Wu H 2018 *Sci. Adv.* **4** eaar5909
- [25] del Campo A, Rams M M and Zurek W H 2012 *Phys. Rev. Lett.* **109** 115703
- [26] Takahashi K 2013 *Phys. Rev. E* **87** 062117
- [27] Damski B 2014 *J. Stat. Mech.: Theory Exp.* **P12019**
- [28] Saberi H, Opatrny T, Mølmer K and del Campo A 2014 *Phys. Rev. A* **90** 060301
- [29] del Campo A and Sengupta K 2015 *Eur. Phys. J. Spec. Top.* **224** 189–203
- [30] Takahashi K 2017 *Phys. Rev. A* **95** 012309
- [31] Masuda S and Nakamura K 2009 *Proc. R. Soc. A* **466** 1135–54
- [32] Torrontegui E, Ibáñez S, Chen X, Ruschhaupt A, Guéry-Odelin D and Muga J G 2011 *Phys. Rev. A* **83** 013415
- [33] An S, Lv D, del Campo A and Kim K 2016 *Nat. Commun.* **7** 12999
- [34] Masuda S and Nakamura K 2011 *Phys. Rev. A* **84** 043434
- [35] Masuda S, Nakamura K and del Campo A 2014 *Phys. Rev. Lett.* **113** 063003
- [36] del Campo A 2011 *Eurphys. Lett.* **96** 60005
- [37] Choi S, Onofrio R and Sundaram B 2012 *Phys. Rev. A* **86** 043436
- [38] Jarzynski C 2013 *Phys. Rev. A* **88** 040101
- [39] del Campo A 2013 *Phys. Rev. Lett.* **111** 100502
- [40] Choi S, Onofrio R and Sundaram B 2013 *Phys. Rev. A* **88** 053401
- [41] Deffner S, Jarzynski C and del Campo A 2014 *Phys. Rev. X* **4** 021013
- [42] Jarzynski C, Deffner S, Patra A and Subasi Y 2017 *Phys. Rev. E* **95** 032122
- [43] Patra A and Jarzynski C 2017 *New J. Phys.* **19** 125009
- [44] Okuyama M and Takahashi K 2016 *Phys. Rev. Lett.* **117** 070401
- [45] Duncan C W and del Campo A 2018 *New J. Phys.* **20** 085003
- [46] Muga J G, Chen X, Ruschhaupt A and Guéry-Odelin D 2009 *J. Phys. B: At. Mol. Opt. Phys.* **42** 241001
- [47] del Campo A 2011 *Phys. Rev. A* **84** 031606
- [48] Choi S, Onofrio R and Sundaram B 2011 *Phys. Rev. A* **84** 051601
- [49] del Campo A and Boshier M G 2012 *Sci. Rep.* **2** 648
- [50] Schaff J F, Song X L, Vignolo P and Labeyrie G 2010 *Phys. Rev. A* **82** 033430
- [51] Schaff J F, Song X L, Capuzzi P, Vignolo P and Labeyrie G 2011 *Europhys. Lett.* **93** 23001

- [52] Schaff J F, Capuzzi P, Labeyrie G and Vignolo P 2011 *New J. Phys.* **13** 113017
- [53] Rohringer W, Fischer D, Steiner F, EMazets I E, Schmiedmayer J and Trupke M 2015 *Sci. Rep.* **5** 9820
- [54] Deng S, Diao P, Yu Q, del Campo A and Wu H 2018 *Phys. Rev. A* **97** 013628
- [55] Elliott E, Joseph J A and Thomas J E 2014 *Phys. Rev. Lett.* **113** 020406
- [56] O'Hara K M, Hemmer S L, Gehm M E, Granade S R and Thomas J E 2002 *Science* **298** 2179–82
- [57] Talkner P, Lutz E and Hänggi P 2007 *Phys. Rev. E* **75** 050102
- [58] Lewis H R and Riesenfeld W B 1969 *J. Math. Phys.* **10** 1458–73
- [59] Jaramillo J, Beau M and del Campo A 2016 *New J. Phys.* **18** 075019
- [60] Feldmann T and Kosloff R 2006 *Phys. Rev. E* **73** 025107
- [61] Schäfer T 2010 *Phys. Rev. A* **82** 063629
- [62] Papoular D J and Stringari S 2015 *Phys. Rev. Lett.* **115** 025302