

Estimation-Throughput Tradeoff for Underlay Cognitive Radio Systems

Ankit Kaushik^{*}, Shree Krishna Sharma[†], Symeon Chatzinotas[†], Björn Ottersten[†], Friedrich Jondral^{*}

^{*}Communications Engineering Lab, Karlsruhe Institute of Technology (KIT), Germany

{ankit.kaushik, friedrich.jondral}@kit.edu

[†]SnT - securityandtrust.lu, University of Luxembourg, Luxembourg

{shree.sharma, symeon.chatzinotas, bjorn.ottersten}@uni.lu

Abstract—Understanding the performance of cognitive radio systems is of great interest. To perform dynamic spectrum access, different paradigms are conceptualized in the literature. Of these, Underlay System (US) has caught much attention in the recent past. According to US, a power control mechanism is employed at the Secondary Transmitter (ST) to constrain the interference at the Primary Receiver (PR) below a certain threshold. However, it requires the knowledge of channel towards PR at the ST. This knowledge can be obtained by estimating the received power, assuming a beacon or a pilot channel transmission by the PR. This estimation is never perfect, hence the induced error may distort the true performance of the US. Motivated by this fact, we propose a novel model that captures the effect of channel estimation errors on the performance of the system. More specifically, we characterize the performance of the US in terms of the estimation-throughput tradeoff. Furthermore, we determine the maximum achievable throughput for the secondary link. Based on numerical analysis, it is shown that the conventional model overestimates the performance of the US.

I. INTRODUCTION

Cognitive radio communication is considered as a potential solution in order to address the spectrum scarcity problem of future wireless networks. The available cognitive radio paradigms in the literature can be categorized into interweave, underlay and overlay [1]. In Interweave Systems (IS), the Secondary Users (SUs) utilize the primary licensed spectrum opportunistically by exploiting spectral holes in different domains such as time, frequency, space, polarization, etc, whereas in Underlay Systems (US), SUs are allowed to use the primary spectrum as long as they respect the interference constraints of the Primary Receivers (PRs). On the other hand, Overlay Systems (OS) allow the spectral coexistence of two or more wireless networks by employing advanced transmission and coding strategies. Of these mentioned paradigms, this paper focuses on the performance analysis of the USs in terms of the estimation-throughput tradeoff considering transmit power control at the Secondary Transmitter (ST) with the help of the employed channel estimation technique.

A. Motivation

The main advantage of the US over the IS comes from the fact that the former system allows the SUs to transmit in a particular frequency band even if a Primary User (PU) is operating in that band. Further, PRs have some interference tolerance capability which is totally neglected in IS systems

[2], [3]. It should be noted that the interference caused by the STs is not harmful to the PRs all the time since it becomes harmful only if the interference exceeds the Interference Threshold (IT) of the PR. In this context, USs make better utilization of the available frequency resources in spectrum sharing scenarios. This is the main motivation behind studying underlay scenario in this paper.

In the literature, the performance analysis of the US is limited to knowledge of the channel. With its knowledge, ST operates at a transmit power such that the IT is satisfied at the PR. Although several existing contributions have considered power control in the USs, the channel estimation aspect has received less attention and the performance analysis of power control-based USs considering estimation errors is still an open problem. In a realistic scenario, direct estimation of the channel is not possible, rather this has to be done indirectly by listening to a beacon or a neighbouring pilot channel transmitted by the PR. That is, the ST employs a power based estimation technique by evaluating the received power. Furthermore, implementing power control based on the estimated received power requires knowledge of its noise power, which is rarely perfect [4]. Hence, in order to characterize the true performance of the US, it is important to include these aspects in the model.

Further, sensing-throughput tradeoff has been considered as an important performance metric while analyzing the performance of the ISs [5]–[7]. However, for the USs, the situation is different since the ST is involved in estimating the received power instead of simply detecting the presence or absence of the primary signals. With the inclusion of estimation error, US intends to operate at a suitable estimation time such that the probability of confidence remains above the desired level. In this sense, similar to the sensing-throughput tradeoff in ISs, it is evident that there exists a tradeoff between estimation time and secondary throughput in USs. In this context, this paper studies the estimation-throughput tradeoff in USs considering estimation errors while estimating the channel to the PR.

The performance of IS via sensing-throughput tradeoff has been characterized by Liang *et. al.* in [5]. According to [5], the objective is to maximize throughput at the ST subject to the sharing constraint set by regulation for primary system. We intend to derive a similar expression for the ST acting as an US. The objective of the ST as an US is to maximize

$\frac{1}{(T-\tau)f_s} \sum_n^{(T-\tau)f_s} |y_p[n]|^2$ and $P_s = \frac{1}{(T-\tau)f_s} \sum_n^{(T-\tau)f_s} |y_p[n]|^2$. Likewise (1), $w_p[n]$ and $w_s[n]$ represents circularly symmetric AWGN at PR and ST with zero mean and variance $\mathbb{E}[|w_p[n]|^2] = \sigma_p^2$ and $\mathbb{E}[|w_s[n]|^2] = \sigma_s^2$, correspondingly.

We consider that all transmitted signals are subjected to distance dependent path loss α_p, α_s . The small scale fading gains g_p, g_s are modelled as frequency-flat fading, thus, follow a unit-mean exponential distribution [10]. In the analysis, we consider the coherence time of the channels $\approx T$. But, there will be scenarios where the coherence time exceeds T , in such cases our characterization depicts a lower performance bound.

III. ESTIMATION-THROUGHPUT ANALYSIS

A. Conventional model

According to the conventional model, ST as US is required to control its transmit power P_{cont} such that the received power P_p at the PR is below IT (θ_1) [11] given by

$$P_p = g_p \alpha_p P_{\text{cont}} \leq \theta_1 \quad (5)$$

With controlled power at the ST, the expected data rate at the SR is defined as

$$\mathbb{E}_{g_s, P_{\text{cont}}}[R_s] = \mathbb{E}_{g_s, P_{\text{cont}}}\left[\log_2\left(1 + \frac{g_s \alpha_s P_{\text{cont}}}{\sigma_s^2}\right)\right]. \quad (6)$$

where $\mathbb{E}_{g_s, P_{\text{cont}}}[\cdot]$ represents the expectation over P_{cont} at ST and the channel gain g_s .

B. Proposed Model

To determine P_{cont} according to (5), the conventional model considers that $g_p \alpha_p$ is perfectly known at the ST, which is rarely the case. Hence, channel estimation must be included in the model. This however, opens up the following issues. First, the estimation of the channel cannot be carried out directly [12], [13]. Second, the model must include the effect of estimation errors and noise uncertainty on the system's performance. In view of this, we consider these aspects in the proposed model.

Power control: We first obtain the information concerning the $g_p \alpha_p$ by estimating the P_{rcvd} . As a result, we determine P_{cont} directly from the P_{rcvd} based on the following expression

$$P_{\text{cont}} = \frac{\theta_1 K}{P_{\text{rcvd}}}, \quad (7)$$

where K represents scaling factor. The scaling factor is required at the ST to hold $\mathbb{E}[P_p]$ at θ_1 . It is defined as

$$K = \frac{1}{\mathbb{E}_{g_p, P_{\text{rcvd}}}\left[\frac{g_p \alpha_p}{P_{\text{rcvd}}}\right]}, \quad (8)$$

where, $\mathbb{E}_{g_p, P_{\text{rcvd}}}[\cdot]$ represents the expectation over g_p and P_{rcvd} . Therefore to implement power control according to (7), it requires the knowledge of probability density function (pdf) $f_{g_p \alpha_p / P_{\text{rcvd}}}$ and the path loss α_p ¹. By considering the expression

¹For a practical implementation, α_p needs to be evaluated by the ST before power control scheme is applied to the system. The path loss α_p in (8) is determined as

$$\alpha_p = \frac{\mathbb{E}[P_{\text{rcvd}}] - \sigma_p^2}{P_{\text{tran}}}.$$

$g_p \alpha_p / P_{\text{rcvd}}$ in the denominator of (8) and $P_p = \theta_1 K \alpha_p g_p / P_{\text{rcvd}}$ in (5), it is clear that the $f_{g_p \alpha_p / P_{\text{rcvd}}}$ can be evaluated from f_{P_p} . In this way, K can be determined at the ST.

Given τ is utilized for P_{rcvd} estimation, the throughput at the SR is given by

$$R_s = \frac{T - \tau}{T} \log_2 \left(1 + \frac{g_s \alpha_s P_{\text{cont}}}{\sigma_s^2} \right). \quad (9)$$

It will be clear later in this section that small τ results in large variations for the P_{rcvd} and vice versa. According to (7), this induces variations in P_{cont} . These variations causes P_p to deviate from θ_1 . If not considered in the model, these variations may affect the performance of the system. To deal with this, we define probability of confidence P_c and accuracy μ that captures the variations of P_p at the PR. As desired by the regulatory bodies, it is important for the system to restrain P_c above a certain desired level \bar{P}_c for a given μ . Hence, the probability of confidence constraint is defined as

$$P_c \geq \bar{P}_c. \quad (10)$$

Clearly, there exists a tradeoff that involves maximizing the expected throughput at the SR subject to a probability of confidence constraint given by

$$\max_{\tau} \mathbb{E}_{g_s, P_{\text{cont}}}[R_s(\tau)] \quad (11)$$

$$\text{s.t. } P_c(\tau f_s, \mu) = \mathcal{P}\left(\frac{|P_p - \mathbb{E}[P_p]|}{\mathbb{E}[P_p]} < \mu\right) \geq \bar{P}_c,$$

The probability of confidence is given by

$$P_c = F_{P_p}((1 + \mu)\mathbb{E}[P_p]) - F_{P_p}((1 - \mu)\mathbb{E}[P_p]). \quad (12)$$

Now, due to introduction of K in P_{cont} , cf. (7) holds the variations in P_p across θ_1 , hence $\mathbb{E}[P_p] = 10^{(\theta_1/10)}$. In that sense, P_c truly captures the variations of P_p across θ_1 . Furthermore, the throughput depicted from (6) for the conventional model overestimates the throughput of the US. This overestimation in the throughput is evaluated as β that depicts the difference between the $\mathbb{E}[R_s]$ obtained from the models. It is evident that for analyzing the tradeoff depicted in (11), first it is important to characterize the pdfs f_{P_p} and f_{R_s} .

C. Path loss channel

To simplify the analysis, we consider a case where the transmitted signals are subject to path loss only, that is, the small scale channel gains correspond to $g_s = g_p = 1$. This way, we first consider the variations in P_p due to the presence of noise in the system.

Characterization of performance parameters: Considering (2), P_{rcvd} follows a non-central chi-squared distribution $\chi'^2(N\gamma, N)$, where $\gamma = \alpha_p P_{\text{tran}} / \sigma_s^2$ denotes the received SNR [14].

According to (7), P_{cont} follows an inverse non-central chi-squared distribution. The pdf for P_{cont} is given by

$$f_{P_{\text{cont}}}(x) = \frac{NK\theta_1}{2\sigma_p^2 x^2} e^{-\frac{N}{2\sigma_p^2} \left(\frac{K\theta_1}{x} + \alpha_p P_{\text{tran}}\right)} \left(\frac{K\theta_1}{x\alpha_p P_{\text{tran}}}\right)^{\frac{N}{4} - \frac{1}{2}} \quad (13)$$

$$I_{\frac{N}{2}-1} \left(\frac{N}{\sigma_p^2} \sqrt{\frac{K\theta_1\alpha_p P_{\text{tran}}}{x}} \right),$$

where $I_{\frac{N}{2}-1}(\cdot)$ represents the Bessel function of order $\frac{N}{2} - 1$ [15].

Following the pdf $f_{P_{\text{cont}}}$ and the relation (7), the pdf of P_p is given by

$$f_{P_p}(x) = \frac{\alpha_p N K \theta_1}{2\sigma_p^2 x^2} e^{-\frac{N\alpha_p}{2\sigma_p^2} \left(\frac{K\theta_1}{x} + P_{\text{tran}} \right)} \left(\frac{K\theta_1}{x P_{\text{tran}}} \right)^{\frac{N}{4} - \frac{1}{2}} \quad (14)$$

$$I_{\frac{N}{2}-1} \left(\frac{N\alpha_p}{\sigma_p^2} \sqrt{\frac{K\theta_1 P_{\text{tran}}}{x}} \right).$$

Based on (14), the distribution function for P_p is determined as

$$F_{P_p}(x) = 1 - \mathcal{Q}_{\frac{N}{2}-1} \left(\sqrt{\frac{N P_{\text{tran}} \alpha_p}{\sigma_p^2}}, \sqrt{\frac{N \cdot \alpha_p \theta_1 K x}{\sigma_p^2}} \right). \quad (15)$$

where $\mathcal{Q}_{\frac{N}{2}-1}(\cdot, \cdot)$ is the Marcum-Q function [15]. Substituting the distribution (15) in (12) to determine P_c for the path loss channel.

Based on relation (6) and $f_{P_{\text{cont}}}$, the pdf for R_s is given as

$$f_{R_s}(x) = \frac{N K \theta_1 \alpha_s \log 2}{2\sigma_p^2 \sigma_s^2} \left(\frac{p(x) + 1}{[p(x)]^2} \right) e^{-\frac{N}{2\sigma_p^2} \left(\frac{K\theta_1 \alpha_s}{p(x)\sigma_s^2} + \alpha_p P_{\text{tran}} \right)} \quad (16)$$

$$\left(\frac{K\theta_1 \alpha_s}{p(x)\alpha_p P_{\text{tran}} \sigma_s^2} \right)^{\frac{N}{4} - \frac{1}{2}} I_{\frac{N}{2}-1} \left(\frac{N}{\sigma_p^2} \sqrt{\frac{K\theta_1 \alpha_p P_{\text{tran}} \alpha_s}{p(x)\sigma_s^2}} \right),$$

where, $p(x) = (2^x - 1)$. Consequently, from (16), the expected throughput at the SR for the path loss channel is evaluated as

$$\mathbb{E}[R_s(\tau)] = \int_0^\infty x f_{R_s}(x) dx. \quad (17)$$

Noise uncertainty: The characterization of P_c and $\mathbb{E}[R_s]$ based on P_{rcvd} requires the perfect knowledge of σ_p^2 at the ST. In this regard, we determine the influence of noise uncertainty on the performance of the system. Following [4], the noise power σ_p^2 can be expressed as a bounded interval $[1/\rho \cdot \sigma_p^2, \rho \cdot \sigma_p^2]$, where ρ amounts the level of noise uncertainty in the system. To simplify the analysis, we represent noise uncertainty as $\Delta\sigma^2 = 10^{\rho/10}$. Therefore, to characterize the effect of noise uncertainty, we substitute σ_p^2 as $\sigma_p^2 \pm \Delta\sigma^2$ in (12). This way, we develop the best and worst performance bounds for the US.

D. Fading channel

Now, we extend the analysis of the estimation-throughput tradeoff to a fading scenario, which is found more often in practice. Fading causes random variations in the channel. According to the system model, these variations remain constant for a complete frame duration. To cancel the effect of these variations, an ST implements power control for each frame in order to sustain (5). In this section, we investigate the effect of channel estimation error on the performance of the US with fading.

Characterization of performance parameters: For determining the expressions of P_c and $\mathbb{E}[R_s]$ for the fading channel, it is required to determine the pdf for P_{cont} . Based on this, we obtain the pdfs for P_p and R_s . The exact analytical expression of the pdfs for P_{cont} and P_p are given by (18) and (19), see the top of the next page, where $\Gamma(\cdot)$ denotes the Gamma function, $\Gamma(\cdot, \cdot)$ represents the incomplete Gamma function and ${}_2F_1(\cdot, \cdot, \cdot, \cdot)$ in (19) is the Hypergeometric function [15].

With the characterization of f_{P_p} , P_c for the fading channel can be evaluated according to (12). Moreover, the expression for $f_{P_{\text{cont}}}$ in (18) is used to determine the pdf for R_s as

$$f_{R_s}(x) = \int_0^\infty \frac{1}{\alpha_s g_s} f_{P_{\text{cont}}} \left(\frac{2^x - 1}{\alpha_s g_s} \right) e^{-g_s} dg_s \quad (20)$$

According to (17), the expression for f_{R_s} in (20) is used to evaluate the expected throughput $\mathbb{E}[R_s]$ for the fading channel.

IV. NUMERICAL ANALYSIS

In this section, we evaluate the performance of the US for the proposed model. In this regard, we perform simulations to validate the expressions obtained in the previous section. Moreover, the system parameters are selected such that they conform to the scenario described in Fig. 1. To investigate the performance of the system based on the estimation model, in the analysis, the conventional model is used as a benchmark. Unless explicitly mentioned, the following choice of the system parameters is considered for the analysis, $P_{\text{tran}} = 0$ dBm, $\theta_1 = -110$ dBm, $f_s = 1$ MHz, $\gamma = 0$ dB, $\alpha_p = 100$ dB, $\alpha_s = 80$ dB, $T = 100$ ms, $\mu = 0.025$, $\bar{P}_c = 0.95$, $\sigma_p^2 = \sigma_s^2 = -100$ dBm and $\Delta\sigma^2 = \pm 3$ dB.

A. Path loss channel

Firstly, the analysis of the estimation throughput tradeoff based on (11) is performed. Fig. 2 demonstrates the variation of the performance parameters $\mathbb{E}[R_s]$ and P_c with τ . It is evident that the expected throughput decreases linearly with τ , while the throughput according to the conventional model described in (6) remains constant. The slope of $\mathbb{E}[R_s]$ depends on the choice of system parameters. On the other side, P_c increases with τ according to (12). The horizontal dashed line represents the P_c constraint, cf. (10). Solving (11), to obtain the maximum $\mathbb{E}[R_s]$. Hence, according to (11), it is required to determine τ such that $P_c = \bar{P}_c$. This corresponds to the projection of the point $P_c = \bar{P}_c$ on the curve $\mathbb{E}[R_s]$. The projection is illustrated through a vertical dashed line, cf. Fig. 2. Hence, the circle on the curve $\mathbb{E}[R_s]$ denotes the maximum throughput with $\Delta\sigma^2 = 0$ dB under the considered system parameters.

Finally, we include noise uncertainty $\Delta\sigma^2$ in the estimation throughput analysis and determine the performance bounds for the proposed model. Clearly, $\Delta\sigma^2 = -3$ dB signifies a better SNR that improves P_c of the system, cf. Fig. 2. With $\Delta\sigma^2 = -3$ dB, the probability of confidence constraint ($P_c = \bar{P}_c$) is fulfilled at a lower τ , leading to a larger $\mathbb{E}[R_s]$. Consequently, $\Delta\sigma^2 = -3$ dB attains the best performance

$$f_{P_{\text{cont}}}(x) = \exp\left(-\frac{\theta_1 N K}{2\sigma_p^2 x + N\alpha_p P_{\text{tran}} x}\right) (N-2)N\alpha_p \sigma_p^2 \alpha_p P_{\text{tran}} \left(2 + \frac{N\alpha_p P_{\text{tran}}}{\sigma_p^2}\right)^{\frac{N}{2}} \left(\frac{\theta_1 K}{\alpha_p P_{\text{tran}} x}\right)^{\frac{2+N}{4}} \left(\frac{\theta_1 N^2 K \alpha_p P_{\text{tran}}}{\sigma_p^4 x}\right)^{\frac{1}{2} - \frac{N}{4}} \quad (18)$$

$$\left(\Gamma\left[\frac{N}{2} - 1\right] - \Gamma\left[\frac{N}{2} - 1, \frac{\theta_1 N^2 K \alpha_p P_{\text{tran}}}{(4\sigma_p^4 x + 2N\sigma_p^2 \alpha_p P_{\text{tran}} x)}\right]\right) / \left(2(2\sigma_p^2 + N\alpha_p P_{\text{tran}})^2 x \Gamma\left[\frac{N}{2}\right]\right).$$

$$f_{P_p}(x) = \frac{1}{\theta_1 K \alpha_p} \sigma_p^2 \left(\frac{\theta_1 K}{P_{\text{tran}} x}\right)^{\frac{2+N}{4}} [h(x)]^{\frac{2+N}{4}} {}_2F_1\left[\frac{2+N}{4}, \frac{4+N}{4}, \frac{N}{2}, 4h(x)\right], \text{ where } h(x) = \frac{\theta_1 N^2 K \alpha_p^2 P_{\text{tran}} x}{(\theta_1 N K \alpha_p + 2\sigma_p^2 x + N\alpha_p P_{\text{tran}} x)^2} \quad (19)$$

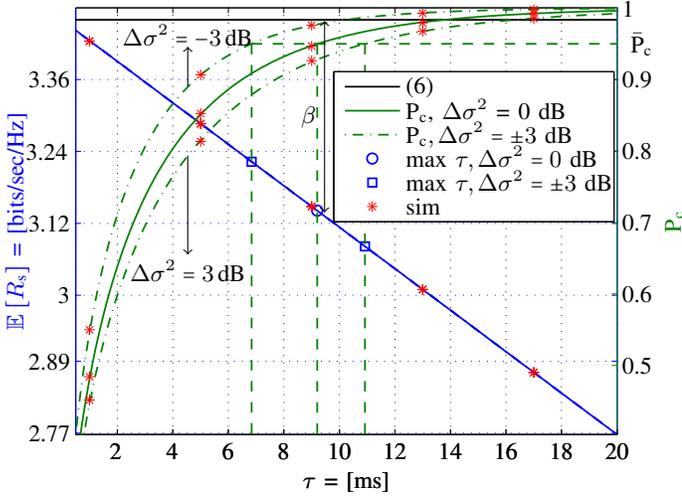


Fig. 2. An illustration of estimation-throughput tradeoff for the path loss channel with $\gamma = 0$ dB. β represents the least performance loss for $\gamma = 0$ dB where the constraint for $P_c = \bar{P}_c$ is sustained.

bound for the US. On similar basis, $\Delta\sigma^2 = 3$ dB determines the worst performance bound.

In the previous analysis, we obtained the maximum throughput for the US while operating the system at $P_c = \bar{P}_c$. Hence for further analysis, the system is analyzed considering the maximum throughput. Additionally, we use the analytical expressions for plotting the curves.

Next, it is interesting to consider the influence of received SNR on the performance of the system with different \bar{P}_c . From Fig. 3, it is observed that $\mathbb{E}[R_s]$ is more sensitive to γ for $\gamma \leq 5$ dB. This becomes clear by understanding the influence of γ on P_c . That is, with increasing γ the curvature for the curve P_c increases. However, its projection representing $\mathbb{E}[R_s]$ lies on an elevated line with a certain slope. This explains the shape of curve obtained for $\mathbb{E}[R_s]$. Moreover, as \bar{P}_c increases, $\mathbb{E}[R_s]$ becomes sensitive towards the variation in γ , cf. Fig. 3. This is due to the fact that by reducing \bar{P}_c , the system tends towards the larger curvature.

For the final analysis concerning the path loss channel, we consider the effect of the estimation accuracy on $\mathbb{E}[R_s]$ for fixed $\gamma = 0$ dB and different $\bar{P}_c \in \{0.92, 0.95, 0.97\}$. It is visible from Fig. 4 that $\mathbb{E}[R_s]$ decays exponentially with μ . In order to capture this effect, we consider the characterization of P_c in (12). It is evident that P_c is related to μ via Marcum-Q function

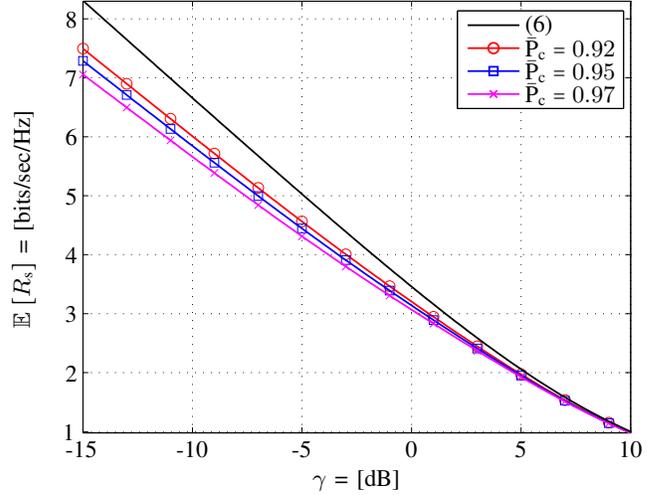


Fig. 3. An illustration of the dependency of the received SNR at ST on the maximum throughput at the SR for different values of probability of confidence constraint $\bar{P}_c \in \{0.92, 0.95, 0.97\}$. The variation in $\alpha_p \in [85, 110]$ dB translates to the variation in γ .

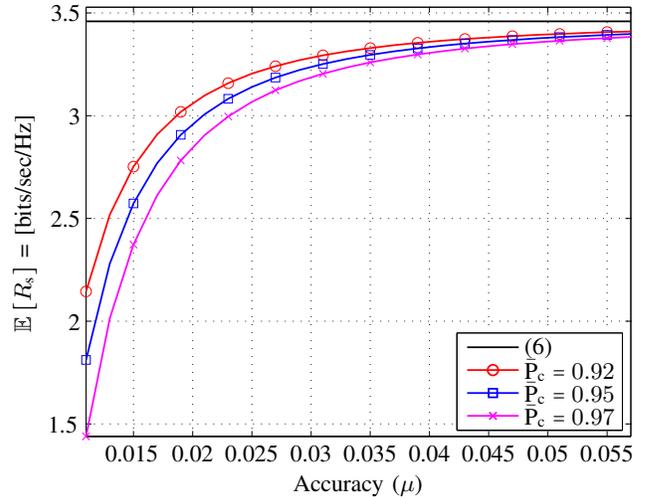


Fig. 4. A variation of the maximum throughput at the SR with estimation accuracy μ for different probability of confidence constraint $\bar{P}_c \in \{0.92, 0.95, 0.97\}$ with fixed $\gamma = 0$ dB.

considered in (14). Consequently, for a fixed P_c , the variation in μ is compensated by τ . Following (16), this variation is mapped into $\mathbb{E}[R_s]$.

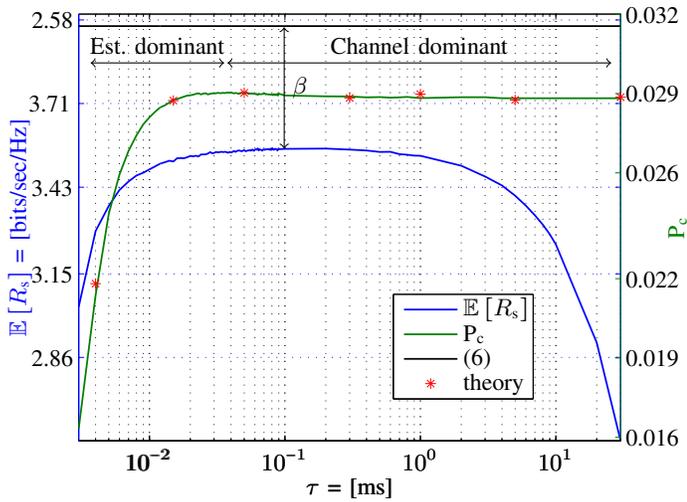


Fig. 5. An illustration of estimation-throughput tradeoff for the channel with fading for $\gamma = 0$ dB. β represents the performance loss, however for this case the constraint for P_c is not satisfied.

B. Fading channel

In this section, we extend our analysis to a channel that involves fading. The curves for P_c and $\mathbb{E}[R_s]$ were generated through simulation. However for P_c , we validate the simulation results through the analytical expression, cf. (12).

Fig. 5 captures the estimation throughput tradeoff for US with fading for $\gamma = 0$ dB. It is interesting to note that for $\tau > 30 \mu\text{s}$, P_c attains saturation. Unlike path loss, despite increasing τ , the variations in the P_p across the θ_1 at the PR cannot be reduced. This phenomenon is due to the inclusion of fading channel in power control, cf. (7). Due to the influence of fading, we divide the system performance at the PR into estimation dominant regime and channel dominant regime, cf. Fig. 5. In the estimation dominant regime $\tau < 30 \mu\text{s}$, the system shows a improvement in P_c with increase in τ . In the channel dominant regime $\tau > 30 \mu\text{s}$, P_c reaches a saturation. This helps us to conclude that the variations in P_p are mainly because of channel. Therefore, unlike the path loss channel, increasing τ doesn't improve the performance of the system.

Finally, we consider the performance at the SR in terms of expected throughput. For $\tau < 20 \mu\text{s}$, the system experiences a strong change in $\mathbb{E}[R_s]$, it remains relatively constant for $20 \mu\text{s} < \tau < 1$ ms and finally decreases linearly beyond 1 ms. To describe this behaviour, we consider (9). Clearly, $\mathbb{E}[R_s]$ is dependent on g_s , P_{cont} and $(T - \tau)/T$, but only P_{cont} and τ depends on N . For $\tau < 20 \mu\text{s}$, a slight change in N has large influence on the value of K , cf. Fig. 5. Thus, K increases first drastically with N and saturates after a certain point $\tau > 20 \mu\text{s}$. However, beyond this point, the factor $(T - \tau)/T$ becomes dominant.

V. CONCLUSION

To implement power control mechanism for the US, it requires the knowledge of the channel at the ST. Acquiring the knowledge of channel through estimation induces variations in the parameters, e.g., power received at the PR. This may be

harmful for the system. In this regard, we proposed a model to capture these variations and characterize the true performance of the US. The performance at PR and SR has been depicted based on probability of confidence and expected throughput. Moreover, the paper investigated the estimation-throughput tradeoff for the US. Based on analytical expressions, the maximum expected throughput for the secondary link was determined. Additionally, the variation in expected throughput against different system parameters was analyzed. Finally, by means of numerical analysis, it has been clearly demonstrated that the conventional model overestimates the performance of the US.

For the underlay scenario with fading, it was observed that probability of confidence didn't improve despite increase in estimation time. Hence for fading channel, the probability of confidence is not a suitable choice for the PR constraint. For the future work, we would like to investigate estimation-throughput tradeoff for the US subject to the probability outage constraint at the PR.

REFERENCES

- [1] A. Goldsmith, S. Jafar, I. Maric, and S. Srinivasa, "Breaking Spectrum Gridlock With Cognitive Radios: An Information Theoretic Perspective," *Proceedings of the IEEE*, vol. 97, no. 5, pp. 894–914, May 2009.
- [2] X. Jiang, K.-K. Wong, Y. Zhang, and D. Edwards, "On hybrid overlay-underlay dynamic spectrum access: Double-threshold energy detection and markov model," *IEEE Transactions on Vehicular Technology*, vol. 62, no. 8, pp. 4078–4083, Oct 2013.
- [3] S. Sharma, S. Chatzinotas, and B. Ottersten, "A hybrid cognitive transceiver architecture: Sensing-throughput tradeoff," in *CROWNCOM*, Jun. 2014.
- [4] R. Tandra and A. Sahai, "SNR Walls for Signal Detection," *IEEE Journal of Selected Topics in Signal Processing*, vol. 2, no. 1, pp. 4–17, Feb 2008.
- [5] Y.-C. Liang, Y. Zeng, E. Peh, and A. T. Hoang, "Sensing-Throughput Tradeoff for Cognitive Radio Networks," *IEEE Transactions on Wireless Communications*, vol. 7, no. 4, pp. 1326–1337, April 2008.
- [6] M. Cardenas-Juarez and M. Ghogho, "Spectrum Sensing and Throughput Trade-off in Cognitive Radio under Outage Constraints over Nakagami Fading," *IEEE Communications Letters*, vol. 15, no. 10, pp. 1110–1113, October 2011.
- [7] Y. Sharkasi, M. Ghogho, and D. McLernon, "Sensing-throughput tradeoff for OFDM-based cognitive radio under outage constraints," in *ISWCS*, Aug 2012, pp. 66–70.
- [8] A. Kaushik, M. R. Raza, and F. K. Jondral, "On the Deployment of Cognitive Relay as Underlay Systems," in *CROWNCOM*, Jun. 2014.
- [9] J. Jing, L. Wu, Y. Xu, and W. Ma, "Spectrum sharing through receiver beacons in fading channels," in *WCSP*, Oct 2010, pp. 1–5.
- [10] D. Tse and P. Viswanath, *Fundamentals of Wireless Communication*. Cambridge University Press, 2005.
- [11] Y. Xing, C. Mathur, M. Haleem, R. Chandramouli, and K. Subbalakshmi, "Dynamic Spectrum Access with QoS and Interference Temperature Constraints," *IEEE Transactions on Mobile Computing*, vol. 6, no. 4, pp. 423–433, April 2007.
- [12] T. Tian, H. Iwai, and H. Sasaoka, "Pseudo BER Based SNR Estimation for Energy Detection Scheme in Cognitive Radio," in *VTC Spring*, May 2012, pp. 1–5.
- [13] S. Sharma, S. Chatzinotas, and B. Ottersten, "SNR Estimation for Multi-dimensional Cognitive Receiver under Correlated Channel/Noise," *IEEE Transactions on Wireless Communications*, vol. 12, no. 12, pp. 6392–6405, December 2013.
- [14] H. Urkowitz, "Energy detection of unknown deterministic signals," *Proceedings of the IEEE*, vol. 55, no. 4, pp. 523 – 531, april 1967.
- [15] I. S. Gradshteyn and I. M. Ryzhik, *Table of Integrals, Series, and Products*, 6th ed. San Diego, CA: Academic Press., 2000.