

# Performance Analysis of Fractionally Spaced Equalization in Non-linear Multicarrier Satellite Channels

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# Presentation Overview

1. Scenario
2. Channel impairments and System Constraints
3. System Architecture
4. Fractionally Spaced Equalization
5. Optimized Receiver De-mapping
6. Simulations
7. Conclusions
8. Acknowledgments

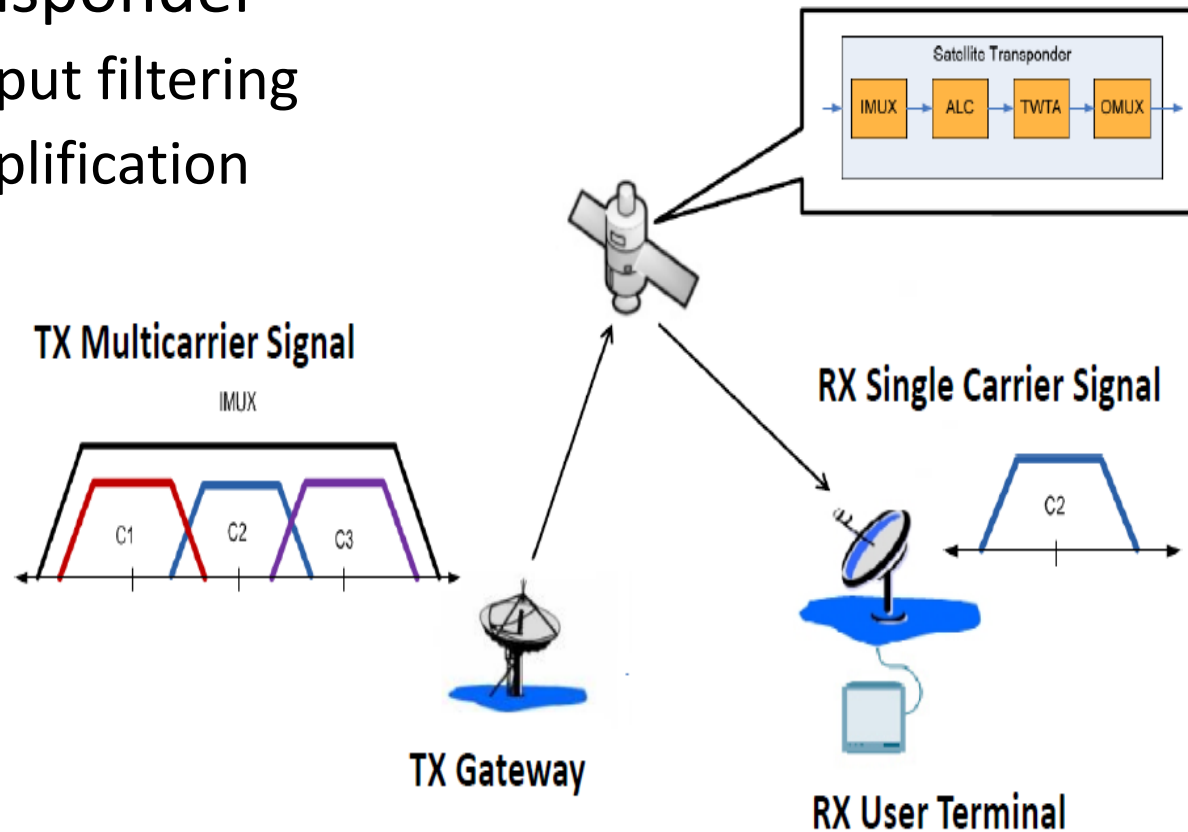
# Outline

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# Scenario

- Multicarrier gateway uplink
- Multicarrier transponder
  - Joint input /output filtering
  - Joint power amplification

- Advantages:
  - HW saving
  - Weight saving
  - Flexibility

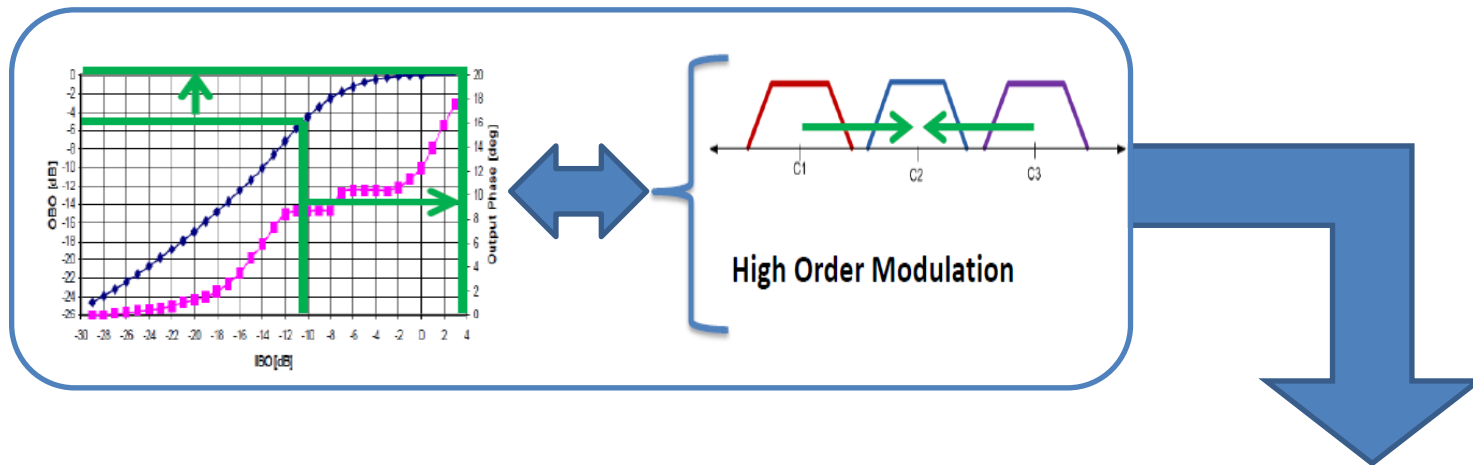


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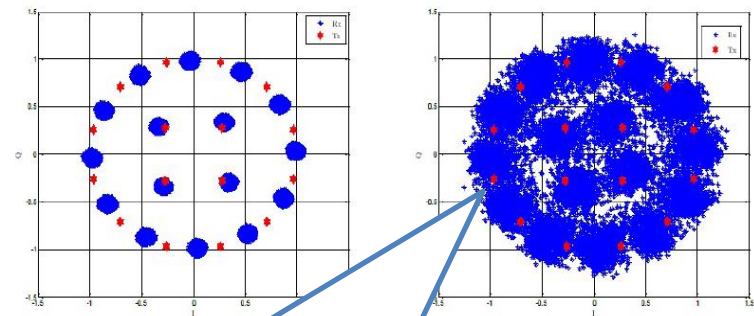
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# Channel Impairments and System Constraints

- Power & Spectral Efficiency Trade off



- System Constraints:
  - No On-board Signal Processing
  - Low complexity User Terminals



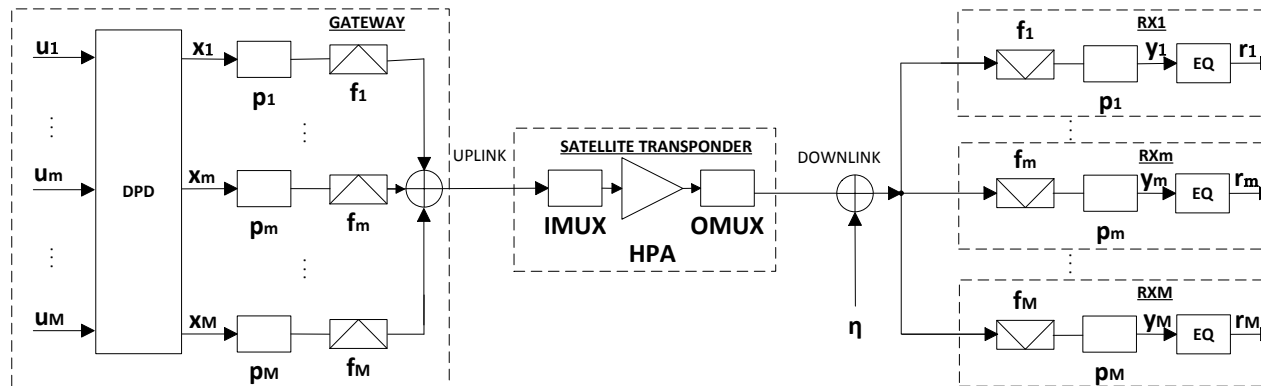
INTERMODULATION PRODUCTS

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# System Architecture

- Countermeasures Techniques:
  1. Multicarrier Predistortion at the gateway <sup>1</sup>
  2. Advanced Receiver Processing:
    1. Fractionally Spaced Equalization
    2. Optimized de-mapping at the user terminals (UT)



<sup>1</sup>R. Piazza, E. Zenteno, and e. al, "Multicarrier digital predistortion/equalization techniques for non-linear satellite channels," in *Proc. 30th AIAA Intern. Commun. Satellite Syst. Conference (ICSSC)*, Ottawa, Canada, Sep. 2012.



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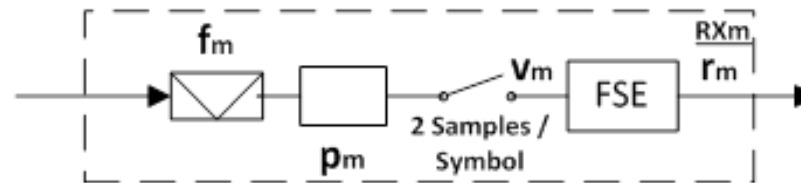
# Fractionally Spaced Equalization

- Receiver equalization that exploits higher sampling rate <sup>2</sup>:
  - $K > 1$  samples per symbol
- It aims to compensate for:
  - Non-constant group delay of the channel
  - Residual Linear and non-linear distortions
  - Non-optimal receiver sampling

<sup>2</sup>R. D. Gitlin, S. B. Weinstein, "Fractionally Spaced Equalization: An Improved Digital Transversal Equalizer," *Bell Systems Technical Journal*, 60:2, February 1981, available online <http://archive.org/details/bstj60-2-275>.

- FSE as Linear Filtering:

$$- r_m(n) = \sum_{k_1} b_m(k_1) v_m(n - k_1) = \mathbf{b}_m \mathbf{v}_m(n)$$



- Parameters Estimation:

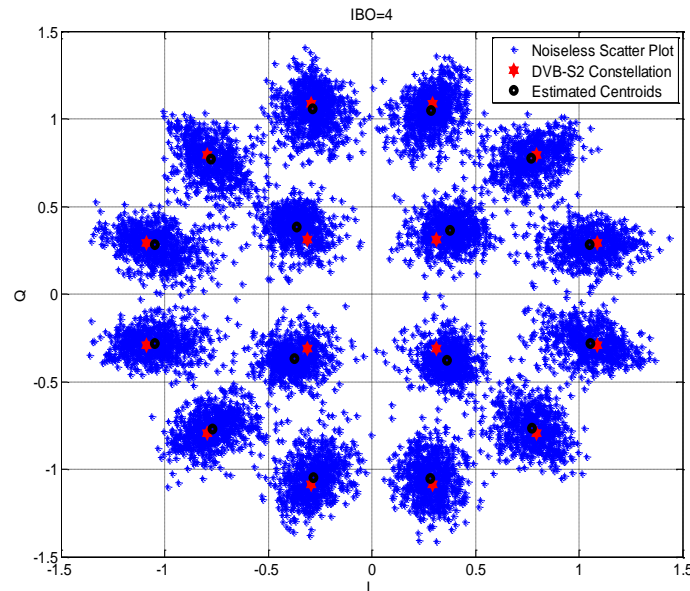
- $\mathbf{b}_m = \operatorname{argmin}_{\mathbf{b}_m} \{ \sum_{n=1}^N E[ r_m(n) - u_m(n) ]^2 \}$
- Standard Least Squares Solution
- Adaptive and based on pilots

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# Non-linear Bias in the RX symbols

- Equalized symbols shows some residual non-linear bias w.r.t. to the reference constellation



- This bias degrades the bit error rate (BER) performance
  - Need to determine more accurate reference constellation for decoding

# Average and Centroids based De-mapping

- For linear systems average constellation de-mapping (ACD) suffices:
  - One scaling factor :  $\beta = \underset{c}{\operatorname{argmin}} \frac{\sum_{k=1}^M \sum_{x \in \mathcal{F}_k} |x - c|^2}{\sum_{k=1}^M |a_k|^2}$
- For a general non-linear system we need one-to one re-mapping (CBD):
  - For each constellation point  $k$ :
    - Centroid  $c_k = \underset{c}{\operatorname{argmin}} \sum_{x \in \mathcal{F}_k} |x - c|^2$ ,  $k \in [1, M]$
  - Centroids estimation based on pilots

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# Figure Of Merit

- Total Degradation:
  - Evaluated at a Target Packet Error Rate
  - Spectral Efficiency & HPA Power efficiency

$$TD = \left. \frac{E_b}{N_0} \right|_{NL} - \left. \frac{E_b}{N_0} \right|_{Ideal} + OBO.$$

HPA efficiency loss

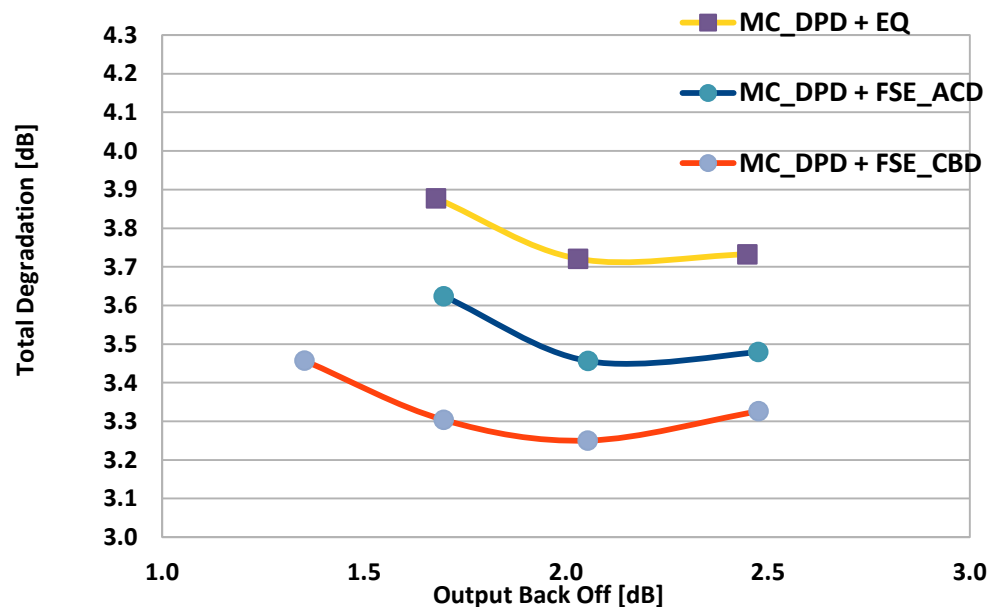
Code loss

where  $OBO = P_{out}/P_{sat} \Big|_{dB}$



# TD Performance Two Carriers Satellite Channel (1)

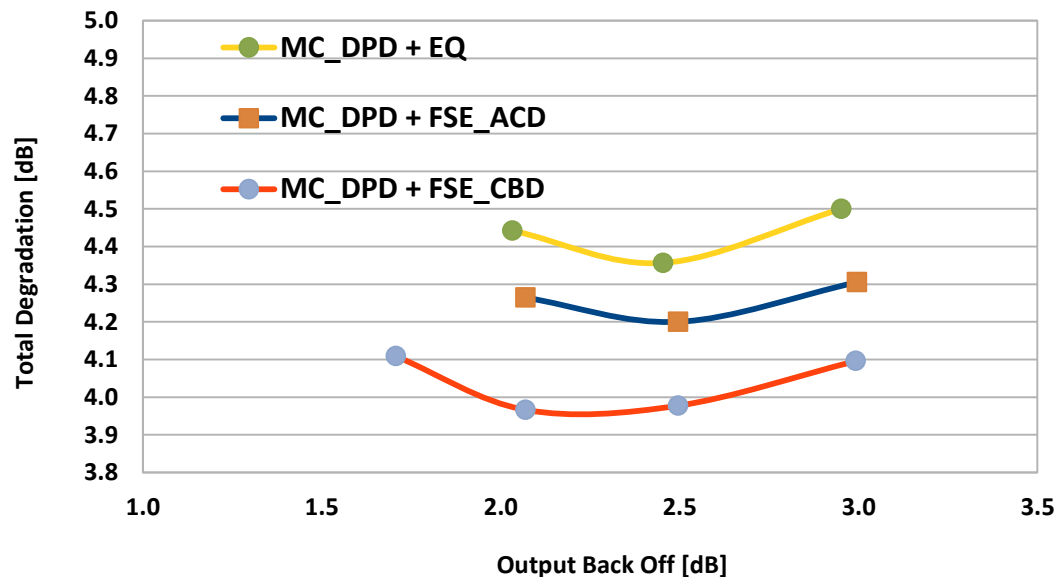
- Setting: 16.36 Mbaud, 16 APSK, Roll-off=0.2, LDPC with Code Rate=3/4, Transp. BW=36MHz



- EQ: Baseline symbols spaced equalization
- FSE with Average Const. Decoding provides 0.2 dB over EQ
- Centroids decoding provides additional 0.15 dB
- Total of 0.3-0.4 dB of gain

# TD Performance Two Carriers Satellite Channel (2)

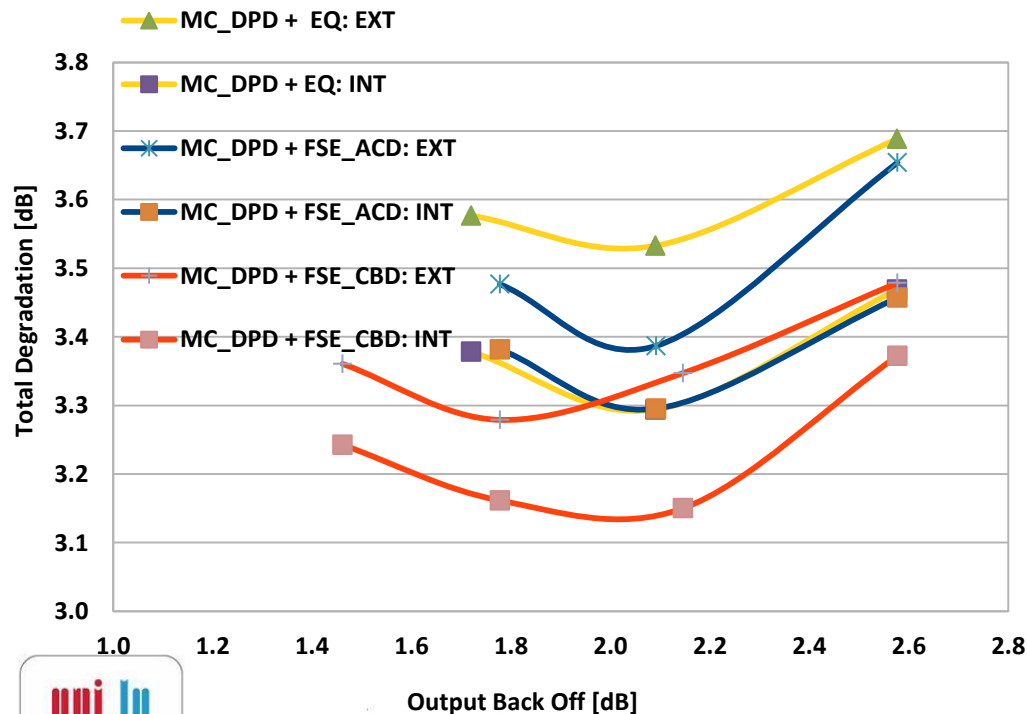
- Setting: 18 Mbaud, 16 APSK, Roll-off=0.2, LDPC with Code Rate=3/4, Transp. BW=36MHz



- Higher baud-rate leads to higher degradation
- FSE with Average Const. Decoding provides 0.15dB over EQ
- Centroids decoding provides additional 0.25 dB
- Total of ~0.4 dB of gain

# TD Performance Triple Carriers Satellite Channel (1)

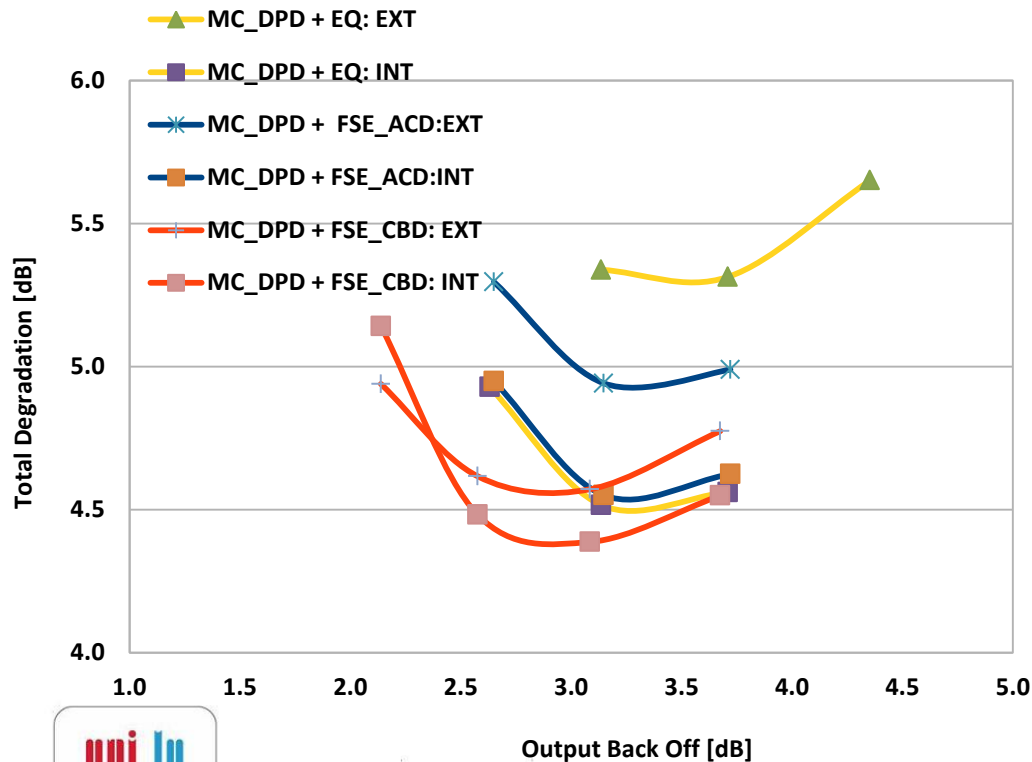
- Setting: 10 Mbaud, 16 APSK, Roll-off=0.2, LDPC with Code Rate=3/4, Transp. BW=36MHz



- External carrier degraded by the MUX filters edge
- FSE with Average Const. Decoding provides up to 0.1dB over EQ
- Centroids decoding provides additional ~ 0.15 dB
- Total ~0.2 dB of gain

# TD Performance Triple Carriers Satellite Channel (2)

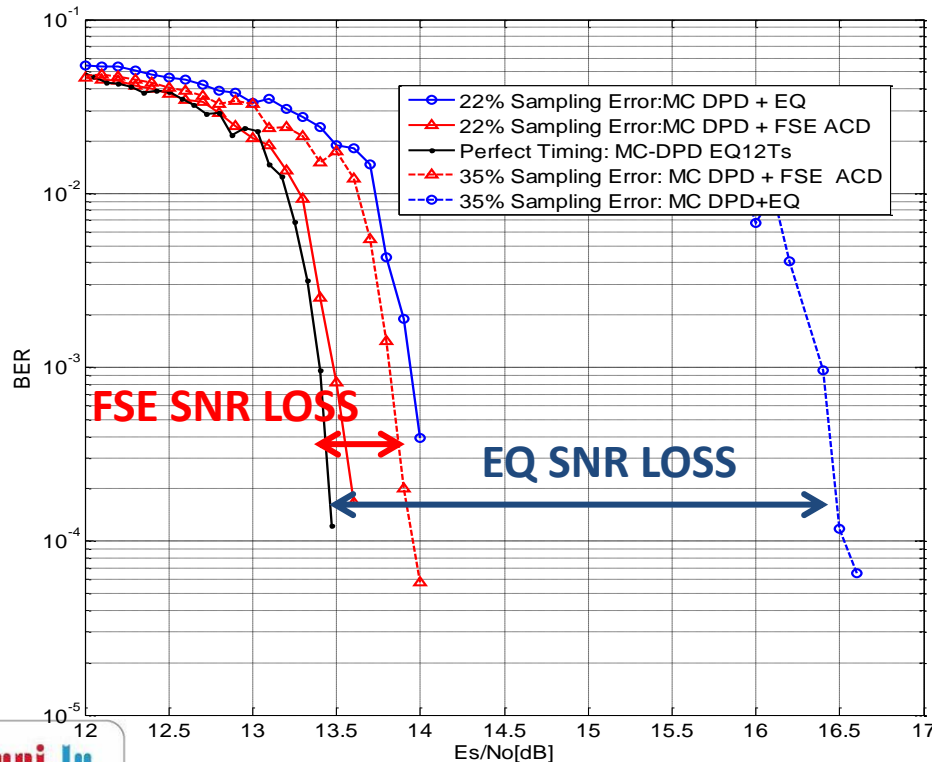
- Setting: 10 Mbaud, 32 APSK, Roll-off=0.2, LDPC with Code Rate=4/5, Transp. BW=36MHz



- Higher Spectral efficiency leads to higher degradation
- FSE with Average Const. Decoding provides up to 0.25 dB to over EQ
- Centroids decoding provides additional ~ 0.25 dB
- Total ~0.5 dB of gain

# Robustness to Sampling Error: Central carrier of a Three Carrier Channel

- Setting: 16 APSK, Roll Off=0.2, IBO=4 dB, LDPC with Code Rate=3/4, Transp. BW=36MHz



- Standard EQ is very sensitive to sampling
- FSE compensates substantially for the sampling error
  - 22% : perfect recovery
  - 35%: only 0.5 dB of loss

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- UT FSE equalization evaluated for multicarrier satellite channels:
  - Provides about  $\sim 0.1/0.2$  dB of gain when multicarrier predistortion is applied at the GW
  - Is shown to be robust with respect to sampling accuracy
- Optimized Symbols de-mapping:
  - Provides additional  $\sim 0.1-0.3$  dB of gain
  - Low complexity

# Acknowledgement & Contact

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