

Finding Outliers in Satellite Patterns by Learning Pattern Identities

Fabien Bouleau¹ and Christoph Schommer²

¹*SES Engineering, Chateau de Betzdorf, L-6815 Betzdorf, Luxembourg*

²*University of Luxembourg, Dept. of Computer Science and Communication, Kirchberg, Luxembourg
fabien.bouleau@ses.com, christoph.schommer@uni.lu*

Keywords: data mining, time series, machine learning, pattern identification

Abstract: Spacecrafts provide a large set of on-board components information such as their temperature, power and pressure. This information is constantly monitored by engineers, who capture the outliers and determine whether the situation is abnormal or not. However, due to the large quantity of information, only a small part of the data is being processed or used to perform anomaly prediction. A common accepted research concept for anomaly prediction as described in literature yields on using projections, based on probabilities, estimated on learned patterns from the past (Fujimaki et al., 2005) and data mining methods to enhance the conventional diagnosis approach (Li et al., 2010). Most of them conclude on the need to build a status vector. We propose an algorithm for efficient outlier detection that builds an identity chart of the patterns using the past data based on their curve fitting information. It detects the functional units of the patterns without apriori knowledge with the intent to learn its structure and to reconstruct the sequence of events described by the signal. On top of statistical elements, each pattern is allotted a characteristics chart. This pattern identity enables fast pattern matching across the data. The extracted features allow classification with regular clustering methods like support vector machines (SVM). The algorithm has been tested and evaluated using real satellite telemetry data. The outcome and performance show promising results for faster anomaly prediction.

1 INTRODUCTION

The major concerns for satellite operations are the safety, reliability and durability of the spacecraft fleet. The spacecrafts are being constantly exposed to the space weather: radiations, solar flares, peaks of temperature, etc. Besides, due to the distance, there is no direct visibility on the spacecraft and no way to examine or fix it. The only health information available is the sensors information it sends to earth. It is an instant reading of all the on-board sensors (like a snapshot) sent at regular intervals of one or two seconds. Once rebuilt, each sequence of data associated to its sensor is a continuous time series expanding over several years.

Anomaly detection and prediction techniques are being constantly developed, in order to perform early detection and avoid the failures, since they have a cost. They may impact the spacecraft lifetime, its capacity, or in the worst case end up with a total loss of control of the satellite. For the most part, expert systems have been built using satellite engineers' knowledge. These systems will trigger an alarm before the anomaly happens. They are thus limited by the satel-

lite engineers knowledge and experience, since they know only a limited part of the model and spacecraft history. A study run by ESOC¹ (Martínez-Heras et al., 2012) shows that only 10% of the on-board sensors data is actually being watched. On top of that, the amount of data to process reaches terabytes. Processing the whole set of data to perform detection and classification is nowadays too much time consuming. There is consequently no systematic classification and analysis.

The most common way to tackle anomalies consists in looking at data from the past for similar behavior in order to identify the root cause and to search for indicators to help early detection. Currently, suspicious satellite data is classified manually by the data experts themselves. In this paper, we propose an algorithm for efficient outlier detection that builds a characteristics chart for each patterns using the data from the past using its curve fitting information, in order to enable anomaly detection and eventually prediction. Each detected pattern is thus allotted a characteris-

¹European Space Operations Centre, responsible for controlling the European Space Agency (ESA) satellites and space probes.

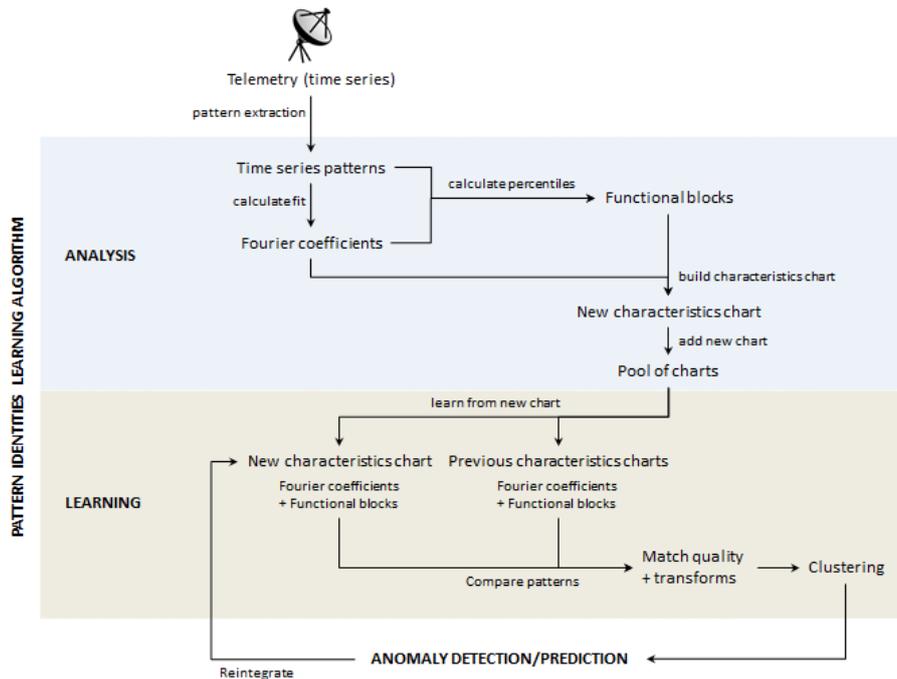


Figure 1: Conceptual Design. The data flows from the telemetry down to the anomaly detection/prediction. Our algorithm is represented by the two boxes in-between: the analysis part processes the patterns in order to extract their characteristics charts, composed of the percentiles explained in section 3.3 and other elements listed in section 3.4. The learning part aims to compare the newly incoming patterns with the pool of already classified ones, as described in the sections 3.1 and 3.2. The resulting status vector is then built from the comparisons. The algorithm also integrates the detected anomalies as an updated characteristics chart, which is then reprocessed.

tics chart with the most relevant statistical elements. This pattern identity chart allows fast pattern matching across the data and pattern classification. In the following section, we will present the state of the art approaches in the space industry. We will then introduce our algorithm for fast pattern matching and the subsequent techniques that can be used for detecting the pattern, fuzzy comparison, to measure the quality of the match and window sliding. The results are presented and discussed in the next part. We will eventually conclude by summarizing the contributions of this paper in the last part.

2 CONVENTIONAL APPROACHES TO OUTLIER DETECTION

Expert systems are built on the knowledge of the satellite engineer, sometimes based on the manufacturer’s inputs. They apply to one part of the system only and usually focus on a specific anomaly. Though very accurate, the number of these systems grows fast and each of them requires weeks or sometimes

months to be created.

There are two main concepts regarding the model-based approach. The first consists in identifying the signature of the device instead of the anomaly. The model is then implemented to reproduce its behavior. Anomalies can tentatively be reproduced and analyzed by satellite engineers depending on the inputs. The second model-based approach is to build a fully fledged model of the spacecraft, commonly designated as simulator, to either test the maneuvers against it or use its data output as predicted behavior.

The model-based approach nevertheless suffers from its lack of flexibility with regards to internal and environmental reconfigurations. The model needs to be updated as soon as the satellite hardware is altered (broken gyro for instance). On top of that, environmental elements such as space weather may alter the measures. The effort to develop and maintain such a model is merely prohibitive and only some parts are considered due to the overall complexity of the satellite.

Systematic analysis methods emerge, relying classification techniques such as support vector machines for pattern recognition. These techniques are nevertheless subject to performance issues as the cloud of

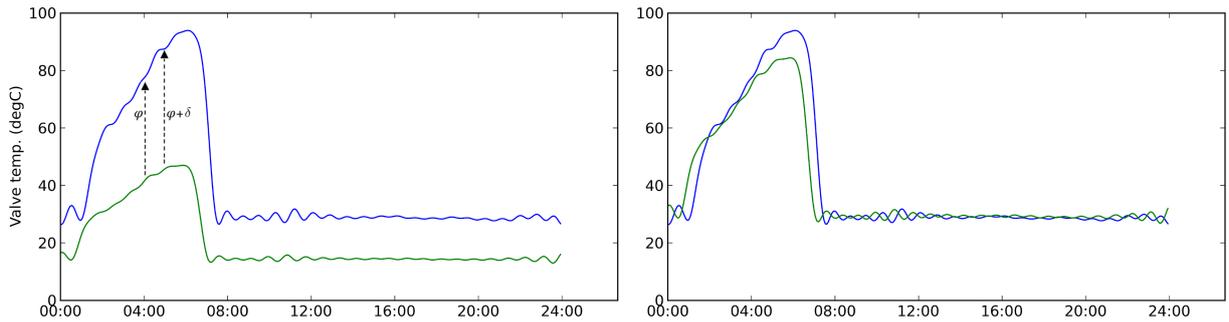


Figure 2: Fourier series representation of two thermal signatures f_1 (lower curve) and f_2 (upper curve). We apply the affine transforms on the f_1 curve to obtain f_1' , which appears on the plot on right hand side. The algorithm evaluated the best fit with $a = 0.502$ and $k = 0.21$, using the points at 180° and 190° .

point grows. Besides, most of them require complete reprocessing if only a subset needs to be taken into account.

All these traditional approaches rely on apriori knowledge based on a narrow set of data and the data mining methods suffer from performance issues induced by scalability limitation. The synthesized data based outlier detection approach is being increasingly considered. The concept is to use the curve fitting data to perform pattern matching using specific techniques and properties. Each pattern is described by an identity chart in which appear the curve fitting data and other relevant statistical elements. This identity chart is then used to perform fast pattern matching across the entire database. As for the curve fitting, Fourier series propose an interesting set of properties that allow efficient pattern comparison and match quality measurement. Furthermore, using the sliding window technique as described by (Beringer and Hüllermeier, 2006) would enable efficient reclassification of the patterns while saving reprocessing time and therefore keeping the fast pattern matching performance at its best.

Table 1 lists the conventional outlier detection techniques. All these approaches rely on cloud of points rather than a reduced dataset. The order of magnitude for a single parameter over the entire lifetime of one spacecraft (roughly 15 years) is around 500 million points to process. Besides, this data is globally non-stationary: some elements are bound to seasonal effect, some to external factors like solar flares, moon attraction, etc. or simply the orbital position of the satellite. Most algorithms scale with the dimensionality of the input data, inducing a problem of computational cost. To address this issue, approaches like Symbolic Aggregate approxXimation (Lin et al., 2003) target the reduction of dimensionality. It nevertheless performs a systematic reduction, regardless the semantics of the data. It obviously does not make sense to compare Volts with Amperes, as does trying

to make the intensity signature of battery charge and discharge match. Detecting the different phases of a signal, be it power or thermal signature for instance, is henceforth paramount and will be addressed by our algorithm.

Although we are following up the thermal signatures of satellite thrusters dataset only along this paper for the sake of clarity of the explanations, our algorithm was applied alike over different types of geostationary satellites and different types of sensor measures (battery voltage, tank pressure, etc.).

3 PROPOSED OUTLIER IDENTIFICATION SYSTEM

Our approach to perform outlier identification is to extract the features of the time series and enable traditional classification algorithms. Depending on the context, the data analysis may nevertheless differ and require re-classification. Our method provides fast data processing algorithms by using synthesized information.

The first question is which curve fitting technique shall be used in our case in order to preserve efficiency. From our analysis of the different methods, we came to the conclusion that discrete Fourier transform is the most suitable in the case of satellite telemetry. First of all, because of the interesting properties of Fourier with regards to the convolution of two series and how they can be easily factorized that we elaborate below. Besides, due to the oscillating nature of the signals and the background induced by spectrum analysis, most analysis algorithms use this technique. The curve fitting step is therefore already available and normalized in the database.

In this section, we introduce how in our methodology we proceed to compare two patterns using the curve fitting information, along with the interesting

properties. We will also show how we measure the quality of our match, the tools we use for horizontal identification and eventually how we define the pattern's characteristics chart.

3.1 Pattern Comparison

Given two Fourier series f_1 and f_2 of the same frequency:

$$f_1(t) = k_1 + \sum_{i=1}^N a_{i,1} \cos(i\omega t + \varphi) + b_{i,1} \sin(i\omega t + \varphi) \quad (1)$$

$$f_2(t) = k_2 + \sum_{i=1}^N a_{i,2} \cos(i\omega t + \varphi) + b_{i,2} \sin(i\omega t + \varphi) \quad (2)$$

Once factorized, the convolution $R(f_1, f_2, t)$ can then be written the following way:

$$R(f_1, f_2, t) = k_1 - k_2 + \sum_{i=1}^N (a_{i,1} - a_{i,2}) \cos(i\omega t + \varphi) + (b_{i,1} - b_{i,2}) \sin(i\omega t + \varphi) \quad (3)$$

The resulting Fourier series represents the distance between the two original Fourier series f_1 and f_2 . Let \hat{R} be the representation of $R(f_1, f_2, t)$ in the frequency domain. We define the quality of the comparison $\rho(\hat{R})$ by the following equation:

$$\rho(\hat{R}) = \sum_{i=1}^N \frac{\hat{R}(i)}{i^2} \quad (4)$$

Vertical scaling and translation are the only two purely mathematical transforms we need for the comparison. The horizontal transforms require deeper understanding of the signal itself and will be covered in the next section. Since the nature of the pattern is affected, and henceforth the quality of the comparison, the measures of the transforms will be kept in the characteristics chart of the pattern. The transforms are modeled the following way:

$$\begin{aligned} a &= \frac{f_2(\varphi + \delta) - f_2(\varphi)}{f_1(\varphi + \delta) - f_1(\varphi)} \\ k &= f_2(\varphi) - a \times f_1(\varphi) \\ f_1'(\theta) &= a \times f_1(\theta) + k \end{aligned} \quad (5)$$

3.2 Pattern Reconsolidation

The second diagram on figure 2 shows that even though we have a good performance match after the

vertical transforms, the algorithm is still missing it. We are hence introducing the concept of sliding pattern which consists in circularly drifting one of the two series to the right or to the left.

As for the modeling, let θ be the circular drift component defined as $0 \leq \theta < 2\pi$. The f_2 series equation would then be written as follows:

$$f_2(t) = k_2 + \sum_{i=1}^N a_{i,2} \cos(i\omega t + \varphi + \theta) + b_{i,2} \sin(i\omega t + \varphi + \theta) \quad (6)$$

The best value of θ is then determined by looking for the minimal $\rho(\hat{R})$ as per equation 4. From there, different approaches are applicable. The most straightforward (and less optimized) is to cycle θ by even steps. Other more accurate techniques can also be applied, such as dichotomy or stochastic research. Stochastic research remains better since it tackles the extrema problem.

3.3 Pattern Functional Units

As previously stated, each parameter of the satellite telemetry comes as a long time series. The individual patterns that will be required for the training set for the classification can be either provided or must be algorithmically determined. The telemetry stream and its curve fit are extracted on a daily basis, regardless the semantics. This is an arbitrary decision based on the satellite engineers as there is one station-keeping maneuver per day. The temperature constantly increases between 12am and 8am that day represents the maneuvers itself, the thruster being idle for the rest of the day.

With regards to classification, the different events need to be isolated in an unsupervised way. The algorithm must hence be capable to learn the pattern structure without apriori knowledge. One intermediate alternative is to use the information databases in which the burn times are scheduled by the engineers. It would nevertheless then relies on user's input and can therefore not adapt to new or unexpected situations. Another approach is to extract the information from the ground control system itself, where the command are actually sent to the spacecraft. If this is more deterministic and accurate, it is still driven by human actions and enters in the semi-supervised category. Some of the actions may furthermore be initiated by the satellite itself and will thus not be captured.

For the reasons aforementioned, if these solutions can be considered as helpers, a proper unsupervised method is still needed. Our approach is to divide the signal horizontally by using the percentiles method.

Table 1: Related work on outlier detection techniques.

Class	Approach
Supervised Decision trees	Rule induction Bayesian networks Memory-based reasoning Support Vector Machines (SVMs) Neural networks
Semi-supervised Transductive SVMs (TSVMs)	Generative Nearest-Neighbor Heuristic
Unsupervised Hierarchical clustering	k-Means Expectation-Maximization

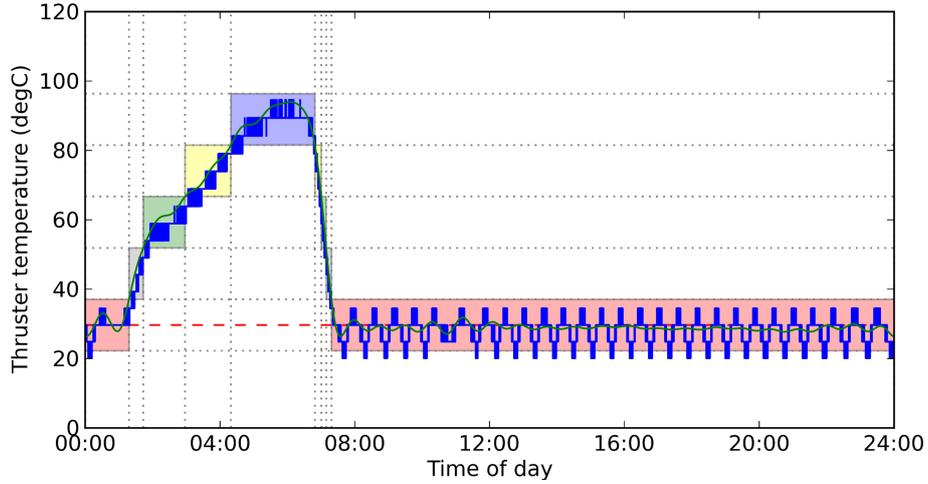


Figure 3: Original data plot divided by the percentiles method. The green curve represents the Fourier series and the dashed red line the median, used as basepoint to calculate the percentiles. In this example, without apriori knowledge, the blocks captured the idle phase (red block around the median) and the "thruster fired" phase. Further analysis show that the fired phase can be split in 3 steps, that the algorithm still needs to learn.

The first element of the percentiles method is the median \tilde{m} . Let $n \in \mathbb{N}$ and p the percentile step ($p = 0.5$ for intervals of 50%). The horizontal areas are defined by the following thresholds:

$$\left(n - \frac{1}{2}\right) p\tilde{m} \leq y_n(x) < \left(n + \frac{1}{2}\right) p\tilde{m} \quad (7)$$

Let $A = ((a_0, b_0), \dots, (a_n, b_n))$ be the DFT coefficients. The blocks intervals are delimited the following way:

$$X_n = DTF(A) \cap \left(n - \frac{1}{2}\right) p\tilde{m} \quad (8)$$

Curve fitting with Fourier in the context has the drawback of smoothing the data. In order not to miss any outlier, the characteristics chart must therefore enumerate the peaks. In this method, we keep the residuals information per block. With $X_i =$

$\{(x_{i,1}, x'_{i,1}), \dots, (x_{i,n}, x'_{i,n})\}$ the list of block intervals and $f(i)$ the Fourier series, we define S_n as:

$$S_n = \sum_{j=1}^{|X_n|} \sum_{i=x_{n,j}}^{x'_{n,j}} (y - f(i))^2 \quad (9)$$

As represented on figure 3, the pattern can thus be subdivided into functional blocks, that will figure in the characteristics chart. In our original example, we know by experience that the upper blocks represent the different phases of the thruster burn while the lowest one the idle period. As for the characteristics chart, we will not only keep the quantitative block representation, but the sequence itself. This will help on one hand to split the active from the idle phases and, on the other hand to characterize the remaining steps of the thruster burn, which are "fired", "on-time" and "cooldown".

Table 2: Performance of the daily data collection phase for the 16 thermal signatures for a single day. This shows that the data is made available within 2 minutes.

Collected element	Quantity of processed data	Processing time
Fourier transform	~43200 points	8s
Residuals calculation	~43200 points	75.6s
Percentile blocks calculation	30 FFT coefficients	1.38s
Blocks processing	56 blocks	0.39s
Cumulated results		85.37s

Table 3: Performance of our pattern comparison algorithm for the 16 thermal signatures. The analysis time of the two months of data goes down to 6 minutes, whereas processing the original cloud of points requires approximately one hour.

Thruster identifier	Patterns	Vertical scalings	Horizontal drifts	Processing time
E1inj	42	41	54	15.37s
E2inj	41	24	47	13.92s
W1inj	45	30	63	22.26s
W2inj	42	39	54	14.87s
E1val1	58	59	85	22.87s
E2val1	58	5	58	18.78s
N1val1	57	32	67	20.64s
N2val1	58	46	87	24.03s
N3val1	56	62	101	25.51s
N4val1	59	91	123	29.96s
W1val1	57	41	70	20.81s
W2val1	58	53	67	20.08s
E1val2	57	55	88	25.26s
E2val2	59	17	59	20.16s
W1val2	59	58	91	25.51s
W2val2	58	50	73	24.23s
Cumulated results	864	703	1187	344.26s

3.4 Definition of the Characteristics Chart

The characteristics chart is the element to gather all the features of the studied pattern. The signals however must be put in their original context. As we define it, the chart shall comprise the immutable (or reference) elements:

- Fourier series, as per equation (1)
- Percentiles blocks, as per equation (8)
- Per-block residuals, as per equation (9)
- Timestamp
- Spacecraft context

The timestamp information is usually represented as day of year plus the year. The day of year allows the classification of seasonal patterns, while the year information indicates the elderness of the data. The

spacecraft context elements can be subdivided in two categories: the spacecraft configuration and its status. The configuration part represents the setup of the spacecraft (switch, valves, etc.) while the status describes its condition such as a defective sensor or a broken CPU. This chart remains flexible and additional features can be experimentally added, such as ephemeris data and space weather.

The characteristics charts are then classified and linked with each other in order to preserve the analytical elements:

- Pattern matching quality, as per equation (4)
- Transform elements, as per equations (5) and (6)

This set of information defines our knowledge database. It will most likely be stored in a relational database, for taking advantage of the indexing engine.

4 EXPERIMENTAL VALIDATION

The validation of our approach is quite difficult for three reasons. First of all, in order to be accurate, the telemetry of the entire lifetime of the satellite should be processed. In this paper we will run it on the most recent subset, that consists in two months of data. Besides, only the propulsion subsystem is analyzed below, the outliers and anomalies of the power subsystem for instance being very difficult for the satellite engineers to detect and explain. The propulsion subsystem henceforth provide a better second sight for validation. Eventually, despite several anomaly detection and curve fitting techniques exist such as (Li et al., 2010) and (Fujimaki et al., 2005) none of them actually plainly address the problematic.

Our experiments dataset is the thrusters temperature telemetry, since related to our original example. We are focusing here on the propulsion subsystem of a single spacecraft. It is composed of 18 parameters, 16 of which representing the thrusters thermal signature, 1 of which is the timestamp (day-of-year) and the last being the thruster identifier. The propulsion subsystem is known to be subject to seasonality, due to the exposition to the sun. The timestamp parameter is therefore relevant in the analysis. The thruster identifier provides its cardinality (north, south, west or east) and correlates with the type of maneuver performed (south-north translation, west-east drift, etc.).

The performance measures depend on how the implementation is performed (programming language, optimizations, etc.) and the hardware it is run on. To obtain our results, we have developed the algorithm using IPython and Matplotlib, since they are accessible for free to everyone. The benchmarks have been performed on a HP Proliant DL580 Intel Xeon E7420 dual CPU quad-core 2GHz running Debian 7 amd64.

Table 2 shows the data collection performance for one day of telemetry on 16 thrusters. It includes the Fourier fit for the pattern comparison optimization, the percentiles blocks calculation for learning the functional blocks, the Fourier fit residuals per block for compensating the smoothing effect of the Fourier series, and the extraction of statistical elements (median, mode, minimum and maximum) to search for the optimal thresholds for the percentiles.

Table 3 presents the outlier detection performance by only using the data presented above. The original cloud of data at this stage is completely ignored. The performance is the best with minimal transforms and processing time. A higher number of transforms means additional iterations and wasted processing time. The ideal case would be to identify the matching points of f_1 into f_2 and calculate the necessary

transforms to achieve it in one iteration only.

As a conclusion, we can observe that the characteristics charts as proposed in our algorithm have been extracted for the last two months of thruster thermal data in less than six minutes and is ready for being processed with regular classification technique. The match rankings are also made available in our database along the charts in order to mitigate the classification and re-classify the case being.

5 CONCLUSION

In this paper, we have addressed the problem of outlier detection in large data warehouse. For this, we have developed an algorithm using curve fitting information to speed up the patterns comparison and efficiently extracting the patterns features for classification. Processing years of cumulated time series for outlier detection is thus made possible.

We have also addressed the problem of data smoothing induced by Fourier fitting with the percentiles method. The nature of the pattern is then refined using the statistical information of the generated blocks.

In order to keep some flexibility in the analysis, the pattern matching algorithm introduces the concept of match quality (equation (4)) on top of pattern transforms. The resulting relevance vector mitigates the results, allows fuzzy classification and provides metrics for re-classification.

The performance of our method is given by experimenting on a relevant subset of data. Measurable efficiency elements are provided in terms of quantity and speed. The results show an acceptable ratio in terms of exploitability and availability of the data: both the data collection and data mining parts are achieved within minutes and the number of iterations is kept minimal.

The horizontal best fit method by sliding the pattern as presented in our algorithm is a topic of on-going and future work. In this respect, the technique can be extended using the sliding window technique described by (Beringer and Hüllermeier, 2006) or by determining the functional units of the blocks definitions as per the percentiles method.

The percentiles method on the other hand is mainly applicable to horizontally shaped time series such as battery charge cycle in the power subsystem. Improving the semantics detection in differently shaped signals is a topic of on-going and future work. Clustering techniques on external information such as the maneuvers schedule and the spacecraft change of state can be used to enhance the resulting definitions.

As a conclusion to this paper, we will note that our approach provides accurate characteristics chart for the propulsion subsystem of the spacecraft. It extracts the essential patterns information to enable systematic processing in the satellite engineers analysis. Beyond, it preprocesses the pattern matching for classification. This approach provides directions for further fast outlier identification techniques in time-series data.

ACKNOWLEDGMENTS

This work has been made within the research project SPACE, which is an interdisciplinary research project between the Interdisciplinary Centre for Security, Trust, and Reliability (SnT), the University Luxembourg, and SES Engineering. We thank all the SPACE members as well as all the SES engineers for their kind support.

REFERENCES

- Azevedo, D. N. R. and Ambrósio, A. M. Dependability in satellite systems: An architecture for satellite telemetry analysis.
- Beringer, J. and Hüllermeier, E. (2006). Online clustering of parallel data streams. *Data & Knowledge Engineering*, 58(2):180–204.
- Bouleau, F. and Schommer, C. (2013). Outlier identification in spacecraft monitoring data using curve fitting information. In *European Conference on Data Analysis 2013*, page 158.
- Das, K., Bhaduri, K., and Votava, P. (2011). Distributed anomaly detection using 1-class svm for vertically partitioned data. *Statistical Analysis and Data Mining*, 4(4):393–406.
- Deng, K., Moore, A., and Nechyba, M. (1997). Learning to recognize time series: Combining arma models with memory-based learning. In *IEEE Int. Symp. on Computational Intelligence in Robotics and Automation*, volume 1, pages 246 – 250.
- Fujimaki, R., Yairi, T., and Machida, K. (2005). An anomaly detection method for spacecraft using relevance vector learning. In Ho, T., Cheung, D., and Liu, H., editors, *Advances in Knowledge Discovery and Data Mining*, volume 3518 of *Lecture Notes in Computer Science*, pages 785–790.
- Fukushima, Y. Telemetry data mining with svm for satellite monitoring.
- Isaksson, C. and Dunham, M. H. (2009). A comparative study of outlier detection algorithms. In *Machine Learning and Data Mining in Pattern Recognition*, pages 440–453. Springer.
- Keogh, E. (2004). T5: Data mining and machine learning in time series databases.
- Keogh, E., Chakrabarti, K., Pazzani, M., and Mehrotra, S. (2001). Locally adaptive dimensionality reduction for indexing large time series databases. In *Proceedings of the 2001 ACM SIGMOD international conference on Management of data*, SIGMOD '01, pages 151–162, New York, NY, USA. ACM.
- Keogh, E., Lonardi, S., and chi' Chiu, B. Y. (2002). Finding surprising patterns in a time series database in linear time and space. In *In In proc. of the 8th ACM SIGKDD International Conference on Knowledge Discovery and Data Mining*, pages 550–556. ACM Press.
- Last, M., Kandel, A., and Bunke, H. (2004). *Data mining in time series databases*. World scientific Singapore.
- Létourneau, S., Famili, F., and Matwin, S. (1999). Data mining for prediction of aircraft component replacement. *Special Issue on Data Mining*.
- Li, Q., Zhou, X., Lin, P., and Li, S. (2010). Anomaly detection and fault diagnosis technology of spacecraft based on telemetry-mining. In *Systems and Control in Aeronautics and Astronautics (ISSCAA), 2010 3rd International Symposium on*, pages 233–236.
- Lin, J., Keogh, E., Lonardi, S., and Chiu, B. (2003). A symbolic representation of time series, with implications for streaming algorithms. In *Proceedings of the 8th ACM SIGMOD workshop on Research issues in data*

mining and knowledge discovery, DMKD '03, pages 2–11, New York, NY, USA. ACM.

- Martínez-Heras, J.-A., Donati, A., Sousa, B., and Fischer, J. (2012). Drmust—a data mining approach for anomaly investigation.
- Rebbapragada, U., Protopapas, P., Brodley, C. E., and Alcock, C. (2009). Finding anomalous periodic time series. *Machine learning*, 74(3):281–313.
- Saleh, J. and Castet, J. (2011). *Spacecraft Reliability and Multi-State Failures: A Statistical Approach*. John Wiley & Sons.
- Yairi, T., Kawahara, Y., Fujimaki, R., Sato, Y., and Machida, K. (2006). Telemetry-mining: A machine learning approach to anomaly detection and fault diagnosis for space systems. In *Proceedings of the 2nd IEEE International Conference on Space Mission Challenges for Information Technology*, SMC-IT '06, pages 466–476, Washington, DC, USA. IEEE Computer Society.