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Kinematic Spline Curves: A temporal invariant descriptor for fast action recognition

Enjie Ghorbel, Rémi Boutteau, Jacques Boonaert, Xavier Savatier, Stéphane Lecoeuche

Abstract

Over the last few decades, action recognition applications have attracted the growing interest of researchers, especially with the advent of RGB-D cameras. These applications increasingly require fast processing. Therefore, it becomes important to include the computational latency in the evaluation criteria.

In this paper, we propose a novel human action descriptor based on skeleton data provided by RGB-D cameras for fast action recognition. The descriptor is built by interpolating the kinematics of skeleton joints (position, velocity and acceleration) using a cubic spline algorithm. A skeleton normalization is done to alleviate anthropometric variability. To ensure rate invariance which is one of the most challenging issue in action recognition, a novel temporal normalization algorithm called Time Variable Replacement (TVR) is proposed. It is a change of variable of time by a variable that we call Normalized Action Time (NAT) varying in a fixed range and making the descriptors less sensitive to execution rate variability. To map time with NAT, increasing functions (called Time Variable Replacement Function (TVRF)) are used. Two different Time Variable Replacement Functions (TVRF) are proposed in this paper: the Normalized Accumulated kinetic Energy (NAE) of the skeleton and the Normalized Pose Motion Signal Energy (NPMSE) of the skeleton. The action recognition is carried out using a linear Support Vector Machine (SVM). Experimental results on five challenging benchmarks show the effectiveness of our approach in terms of recogni-
tion accuracy and computational latency.

Keywords: RBG-D cameras, action recognition, low computational latency, temporal normalization

1. Introduction

Human action recognition has represented an active field of research over the last decades. Indeed, it has become important due to its wide range of applications. As example, it could be cited video surveillance, Human Machine Interaction (HMI), gaming, home automation and e-health.

The first generation of approaches dealing with human action recognition was generally based on Red Green Blue (RGB) videos. Many reviews of these methods can be found in the literature [1, 2]. However, RGB videos present some major disadvantages such as the sensitivity to illumination changes, occlusions, viewpoint changes and background extraction. To overcome these limitations, new acquisition systems have recently been proposed to give additional information about the observed scene: Red Green Blue-Depth (RGB-D) cameras. Depth images have simplified and sped up the extraction of human skeletons via integrated libraries such as OpenNI and KinectSDK (around 45ms for skeleton extraction per frame according to [3]), which was a very difficult task with the use of RGB images. Other acquisition systems such as motion capture systems provide more accurate skeleton sequences but remain unadapted due to their high cost and their non-portability.

In [4], it has been demonstrated that depth-based methods are generally more accurate than skeleton-based methods since depth modality is more robust to noise and occlusions. However, skeleton-based descriptors are faster to compute because of their lower dimension and are therefore more suited for applications requiring a fast recognition.

Many recent papers have proposed RGB-D-based descriptors for human action recognition, showing their high accuracy of recognition in various datasets [5, 6, 7, 8, 9, 10, 11]. Nevertheless, a central challenge is often omitted in these earlier papers: How long does it take to recognize an action? In fact, if an action recognition system
does not work in real-time, its usability in real-life applications remains limited. Thus, the performance of motion descriptors can be viewed as a trade-off between accuracy of recognition and low latency as mentioned in [12], where latency is defined as the sum of computational latency (the time necessary for computation) and observational latency (the time of observation required to make a good decision). In this paper, we will focus mainly on computational latency because the actions are assumed to have already been segmented. Indeed, many off-line applications still require a quick recognition such as medical rehabilitation, gaming, coaching, etc.

Based on these observations, we propose a new skeleton-based human action descriptor called Kinematic Spline Curves (KSC) which operates with low computational latency and with acceptable accuracy compared with recent state-of-the-art methods. To build this descriptor, a Skeleton Normalization (SN) is first carried out to overcome the anthropometric variation. Then, kinematic features including joint position, joint velocity and joint acceleration are calculated from the normalized skeleton data.

After this step, a Temporal Normalization (TN) is carried out in order to reduce the effect of execution rate variability. The TN introduced in this paper is called Time Variable Replacement (TVR). It is based on a change of variables of time by a variable called Normalized Action Time (NAT). Thus, this variable is invariant to execution rate and varies in a fixed range whatever the length of the action is. Functions that can be used to do this change of variables are called Time Variable Replacement Functions (TVRF). In this article, Two TVRF are introduced, namely, the Normalized Accumulated kinetic Energy (NAE) of the skeleton and the Normalized Pose Motion Signal Energy (NPMSE).

This step is a novel, fast and simple way to make actions with different execution rate comparable, without the loss of the temporal information. Finally, features are interpolated via a cubic spline interpolation and are uniformly sampled in order to obtain vectors with the same size.

To achieve a fair comparison of our descriptor with other approaches in terms of accuracy and computational latency, we report the accuracy of recognition and the execution time per descriptor on various challenging benchmarks. Available algorithms of recent state-of-the-art methods are tested with the same parameters and settings on
four datasets: MSRAction3D dataset [5], UTKinect dataset [13], MSRC12 dataset [14] and Multiview3D Action dataset [15]. Our descriptor is also tested on a large-scale dataset NTU RGB+D dataset [16].

Based on our previous work [17], the paper presents a complete action recognition method including novelties such as: 1) The generalization and the extension of a fast and simple novel Temporal Normalization (TN) method called Time Variable Replacement (TVR) in order to avoid the execution rate variability. 2) The detailed analysis of the different component influence (kinetic values, temporal normalization, spatial normalization, etc). 3) A larger experimentation by including three other challenging benchmarks (MSRC-12, Multiview3D and NTU RGB+D datasets).

This article follows this scheme: in Section 2 an overview of related methods is given. Section 3 presents the concept of cubic spline interpolation and Section 4 presents the methodology used to build our descriptor. In Section 5 the experiments and the results are discussed. Finally, Section 6 summarizes this paper and includes some ideas for future work.

2. Related work

In a recent survey [18], action recognition methods have been categorized according to the nature of the used representation: learned representations and hand-crafted representations.

Hand-crafted methods are the most common approaches used in the literature [6, 8, 19]. They are based on the classical schema of action recognition, where low-level features are first extracted, then the final descriptor is modeled using low level features and finally a classifier is used to train a classification model such as Support Vector Machine (SVM) or \( k \) Nearest Neighbors (\( k \)NN).

With the recent advances in deep learning, learning-based representations have been proposed. Instead of selecting specific features, this category of methods learn itself the appropriate ones as in [20, 21, 22, 23, 24]. These methods are very interesting and efficient. However, they require an important amount of data, as well as an important execution time for learning.
In this paper, we focus on hand-crafted methods, since we are interested in recognizing actions using small scale datasets.

The RGB-D-based human action descriptors are commonly divided into two categories, namely depth-based descriptors and skeleton-based descriptors.

### 2.1. Depth-based descriptors

The first tendency was to adapt motion descriptors, initially developed for RGB or gray-level images, to depth images. For example, we can cite the work of [25] where the Spatio-Temporal Interest Points detector (STIP) [26] and the cuboid descriptor [27] were adapted to depth images. They called them respectively the Depth-Spatio-Temporal Interest Points (DSTIP) and the Depth-Similarity Cuboid Features (DSCF).

Other examples can be mentioned such as the extension of Histogram of Oriented Gradient (HOG) [28] to the HOG3D [29] and also its extension to HOG2 [6]. However, some researchers rapidly pointed out the limitations of these adapted methods justifying their claims by the fact that depth modality has different properties and a different structure from color modality [7, 9].

Because of the popularity of the Bag-Of-Words approach and its variants in the field of RGB-based action recognition [30, 31], many attempts have been made to extend this kind of methods to depth modality [32, 33, 34].

Less conventional depth-based descriptors were also proposed [7, 35, 36, 9]. One of the most efficient representations that we can cite is the 4D normals. This original idea was introduced in the work of [7] where the motion of the human body was considered as a hyper-surface of $\mathbb{R}^4$ (three dimensions for the spatial components and one dimension for the temporal component). In differential geometry, one of the well-known ways to characterize a hyper-surface is to find its normals. Thus, Oreifej and Liu chose these features and built the descriptors by quantifying a 4D histogram of normals using polychrons (a 4D extension of simple polygons [37]).

Many authors were inspired by this relevant representation, but changed the quantization step (because of the neighboring information loss with the use of HON4D). Slama et al. [36] modeled 4D normals as subspaces lying on Grassmann manifold. At
the same time, Yang et al. [9] used the same representation by learning a sparse dictionary and then by coding each action as a word of the learned dictionary. The obtained descriptor was called the Super Normal Vector (SNV). This new generation of features based on depth modality has shown its high accuracy compared to other representations. Notwithstanding this important advantage, they generally require considerable computation time as shown in Section 5.

2.2. Skeleton-based descriptors

One of the pioneer work proposed to build a 3D Histogram Oriented of Joints (HOJ) where the 3D position of joints is used [13]. Thus, each posture is represented by a specific histogram. The evolution of these postures is included in a Hidden Markov Model (HMM) which is based on a bag of postures. These features are interesting but are very sensitive to anthropometric variability.

To reduce the effect of this body variation, new methods emerged, where the relative position of joints were used instead of the absolute position as in [38]. These authors [38] proposed the use of the spatial and temporal distances between joints as features. In [39, 40], the main idea is to calculate a similarity shape measure between joint trajectories. To realize that, these curves are reparametrized using the Square-Root Velocity Function (SRVF), leading to a representation in a Riemannian manifold.

Recently, new skeleton-based descriptors have been proposed, inspired by earlier bio-mechanical studies [41] where the skeleton was a very commonly-used representation. Our work is principally inspired by these descriptors more particularly by the two following papers.

On the one hand, Vemulapalli et al. [8, 42] proposed to define the rotations and translations between adjacent skeleton segments using transformation matrices of the Special Euclidean group $SE(3)$. Therefore, the obtained features represent a concatenation of transformation matrices expressed in $SE^n(3)$, where $n$ is equal to the number of segment connections. To switch from a discrete space to a continuous one and to represent descriptors as curves of the Lie group $SE^n(3)$, an interpolation is done on the points of $SE^n(3)$ after the transition to $se^n(3)$, the Lie algebra associated with $SE^n(3)$. This method considers the evolution of the static pose but does not take into
account some important physical measures such as velocity and acceleration.

On the other hand, Zanfir et al. [43] chose to use the kinematics of skeleton joints as features: joint positions, joint velocities and joint accelerations. To overcome anthropometric variability, a skeleton normalization is done. After that, joint velocities and joint accelerations are computed using the information from joint positions. The three kinematic values are then concatenated in a single vector, where the importance of each kinematic value is weighted by optimized parameters. Using this kinematic-based descriptor, the action recognition is done using a kNN classifier (k Nearest-Neighbors).

Even if this method has given good results according to the experimentation of [43], the discontinuity of features can generate some limitations. Indeed, the non-uniformity of velocity during acquisition or the presence of noisy skeletons can negatively impact the results.

3. Cubic spline Interpolation: A review

As presented in Introduction, a cubic spline interpolation will be used to interpolate kinematic features. We reject the idea of using approximation instead of interpolation because of the low number of frames (generally between 20 and 50 per action in well-known datasets) favoring an inaccurate approximation. This method is a well-known numerical method which connects coherently a set of $N$ points $(\alpha_k, y_k)_{k \in [1,N]}$ with $\alpha_1 < \alpha_2 < ... < \alpha_k < ... < \alpha_N$. The goal is to estimate the function $f$ which is assumed to be a continuous $C^1$ piecewise function of $N - 1$ cubic third degree polynomials $f_k$ as described by equation (1).

$$f(t) = (f_k(t)) \quad for \quad \alpha_k < t < \alpha_{k+1} \quad (1)$$

Each function $f_k$ is defined on the slice $[\alpha_k, \alpha_{k+1}]$. In order to respect the continuity of $f$, each $f_k$ is joined at $\alpha_k$ by $f_{k-1}$ (the first derivative $y_k' = \frac{y_{k+1} - y_k}{x_{k+1} - x_k}$ and the second derivative $y_k'' = \frac{y_{k+1}' - y_k'}{x_{k+1} - x_k}$ are also assumed to be continuous). The coefficients $a_k, b_k, c_k, d_k$ of each polynomial $f_k$ are computed following the equations.
Figure 1: An overview of our approach: this figure describes the different steps to compute Kinematic Spline Curves (KSC). The first step represents the skeleton normalization which re-size skeleton to make it invariant to anthropometric variability. Based on the informotion of normalized joint positions, the joint velocities and joint accelerations are computed. Therefore, the three values are concatenated to obtain KF. To palliate execution rate variability, \( t \) is replaced by the NAT variable by using a Time Variable Replacement Function (TVRF). This step represents a novel temporal normalization method, referred as TVR. Then, each component KF is interpolated using a cubic spline algorithm in order to obtain \( M \) functions \( KF^{c} \). Finally, the uniform sampling of \( KF^{c} \) allows us to build the final descriptor KSC.

\[ f_k(\alpha) = a_k(\alpha - \alpha_k)^3 + b_k(\alpha - \alpha_k)^2 + c_k(\alpha - \alpha_k) + d_k \]  

where

\[
\begin{align*}
  a_k &= \frac{1}{(\alpha_{k+1} - \alpha_k)^2} \left( -2 \frac{y_{k+1} - y_k}{\alpha_{k+1} - \alpha_k} + y_{k+1} + y_k \right) \\
  b_k &= \frac{1}{\alpha_{k+1} - \alpha_k} \left( 3 \frac{y_{k+1} - y_k}{\alpha_{k+1} - \alpha_k} - 2y_{k+1} - y_k \right) \\
  c_k &= y_k \\
  d_k &= y_k
\end{align*}
\]  

We choose this kind of interpolation because of the particular behavior of third
degree polynomial which presents a maximum of one inflection point. Therefore, this
type of curve is at the same time realistic (in our case) and does not present undesired
oscillations. Furthermore, this algorithm presents low complexity, compared to other
interesting interpolation techniques such as B-spline.

To carry out the cubic spline interpolation, a matlab toolbox implementing the algo-

4. Kinematic Spline Curves (KSC)

In this section, we describe the different procedures allowing the calculation of the
proposed human action descriptors KSC. Figure 1 illustrates these different processes.
Each subsection details one of these steps.

4.1. Spatial Normalization (S.N.) via skeleton normalization

In this study, an action is represented by a skeleton sequence varying over time.
At each instant \( t \), the skeleton is represented by the pose \( \mathbf{P}(t) \), which is composed
of \( n \) joints with the knowledge of their 3D position \( \mathbf{p}_j(t) = [x_j(t), y_j(t), z_j(t)] \) with
\( j \in [1, n] \).

\[
\mathbf{P}(t) = [\mathbf{p}_1(t), \ldots, \mathbf{p}_j(t), \ldots, \mathbf{p}_n(t)]
\]  

Thus, a skeleton sequence, which represents a specific action (segmented actions),
can be seen as a multidimensional time series. As in the majority of bio-mechanical
studies, the initial position of human hip joint is assumed to be the origin. This is why
we subtract the hip joint coordinates \( \mathbf{p}_{\text{hip}} \) from each joint coordinates. Figure 2 gives
an example of skeleton and describes hip joint location.

\[
\mathbf{P}(t) = [\mathbf{p}_1(t) - \mathbf{p}_{\text{hip}}, \ldots, \mathbf{p}_j(t) - \mathbf{p}_{\text{hip}}, \ldots, \mathbf{p}_n(t) - \mathbf{p}_{\text{hip}}]
\]  

Although we consider that the hip joint is the absolute origin, an important spatial
variability continues to be present, mainly due to anthropometric variability. To over-
come this variability, we propose a skeleton normalization that is very similar to the
normalization used in [43]. However, these latter chose to learn an average skeleton
for each dataset and then to constrain each skeleton of the dataset to have the same limb sizes. The problem is that in real-world applications, the average skeleton of a specific dataset cannot be representative. Thus, we propose the Euclidean normalization of each segment length without imposing a specific length. Hence, we obtain skeletons with unitary segments. Each skeleton is normalized successively starting with the root (hip joint) and moving gradually to the connected segments. This approach preserves the shape of the skeleton and its performance will be discussed in the Section 5. Algorithm 1 describes the skeleton normalization used. All joint positions are normalized except the hip joint position which is assumed to be the root and is therefore unchanged.

\[ \mathbf{p}^{\text{norm}}_{\text{hip}} = \mathbf{p}_{\text{hip}}. \]

We use the normalized skeleton sequence \( \mathbf{P}^{\text{norm}} \) obtained after applying Algorithm 1 to \( \mathbf{p}^{\text{hip}} \) to design our descriptor as depicted by equation (6). Since all joints are interconnected, we obtain a normalized position for each joint \( i \), \( (\mathbf{p}^{\text{norm}}_{a_i}, \mathbf{p}^{\text{norm}}_{b_i} \in [1, n]) \).

\[ \mathbf{P}^{\text{norm}} = [\mathbf{p}^{\text{norm}}_1, \mathbf{p}^{\text{norm}}_2, \ldots, \mathbf{p}^{\text{norm}}_n] \]  \( (6) \)

4.2. Kinematic Features (KF)

As in [43], we assume that human motion can be described by three important mechanical values: joint positions (normalized) \( \mathbf{P}^{\text{norm}} \), joint velocities \( \mathbf{V} \) and finally
Algorithm 1: Skeleton normalization at an instant $t$

**Input:** $(p_{ai}(t), p_{bi}(t))_{1 \leq i \leq C}$ represents the segment extremities ordered and $C$ represents the number of connections with $a_i$ the root extremity and $b_i$ the other extremity of the segment $i$.

**Output:** $(p_{norm}^{ai}(t), p_{norm}^{bi}(t))_{1 \leq i \leq C}$ with $a_i, b_i \in [1, n]$

1. $p_{norm}^{ai}(t) := p_{ai}(t)(p_{a1}(t) = p_{hip}(t)$ represents the position of the hip joint$)$

2. for $i \leftarrow 1$ to $C$ (C: Number of segments) do
3. $S_i := p_{ai}(t) - p_{bi}(t)$
4. $s'_i := S_i / \text{distance}(p_{ai}(t), p_{bi}(t))$
5. $p_{norm}^{bi}(t) := s'_i + p_{norm}^{ai}(t)$
6. end

Joint accelerations $A$. These values are concatenated to obtain what we call Kinematic Features (KF), noted KF in Equation (7).

$$\text{KF}(t) = [P_{norm}(t), V(t), A(t)]$$  \hspace{1cm} (7)

In this subsection, we describe how velocity (8) and acceleration (9) are numerically computed from the discrete data of joint positions as in [43]. In reality, the skeleton is composed of a skeleton sequence of $N$ frames. $k \in [1, N]$ denotes the frame index and $t_k$ represents its associated instant.

$$V(t_k) = P_{norm}(t_{k+1}) - P_{norm}(t_{k-1})$$  \hspace{1cm} (8)

$$A(t_k) = P_{norm}(t_{k+2}) + P_{norm}(t_{k-2}) - 2 \times P_{norm}(t_k)$$  \hspace{1cm} (9)

The dimension of the KF extracted from each frame is equal to $M = 9 \times n$. We recall that $n$ is the number of joints.
4.3. Time Variable Replacement (TVR): a new approach for Temporal Normalization (TN)

Temporal variability is principally caused by execution rate variability (the temporal differences that exist when a subject repeats a same action or when the different subject performs a same action), which implies changeable action duration and different distribution of motion. This means that actions are not performed in the same time slice as illustrated on the top panel of the Figure 3. Consequently, recognizing actions with features varying in different time slices proves to be difficult. For this reason, Temporal Normalization (T.N.) is needed to improve the efficiency of our method. We propose to interpolate the components of the features, according to a novel variable called Normalized Action Time (NAT), instead of time. This change of variable is done thanks to a function TVRF which places the actions in a space that is invariant to execution rate variability as shown in Figure 3. Therefore, the KF can be expressed as a variable depending on NAT which is rate-invariant (10).

\[
\text{KF}(\text{NAT}) = [P_{\text{norm}}(\text{NAT}), V(\text{NAT}), A(\text{NAT})]
\] (10)

The choice of the function TVFR is crucial for the good functioning of the normalization.

1) First, this function should have a physical meaning which makes features invariant to the execution rate variability.

2) Second, the used function should be increasing and have to realize a one-to-one correspondence with time.

3) Finally, to compare actions with different temporal length, the latter function should vary in a fixed range independently from the length of the skeleton sequence as described by Figure 4.

In this way, let consider the TVRF_{instance} (instance represents the index of the action instance) as an increasing one-to-one correspondence between the variable interval of time and a fixed interval where NAT varies:

\[
\forall \text{instance}, TVRF_{\text{instance}} : [0, N_{\text{instance}}] \rightarrow [a, b] \\
\quad t \mapsto TVRF_{\text{instance}}(t) = \text{NAT}
\]
Figure 3: Example of the effect of temporal normalization on a joint component trajectory $f(t)$. In this example, $f(t)$ refers to the x-coordinates of a joint. We consider two instances of the same type of action (Instance1 and Instance2). Top: the trajectories are plotted as functions of time. We can observe that the time slices of the two trajectories are different ($t_{N1} \neq t_{N2}$). Bottom: After the substitution of time by a NAT, we can observe that the trajectories vary in the same range $[a,b]$. An important remark can also be made: the two trajectories representing the same action type are more similar.

$a, b$ represent constant values such as $[a, b]$ is the range where varies NAT and $N_{instance}$ is the length of the skeleton sequence instance. This TVR algorithm is expected to improve the accuracy of recognition of our method, since the time-variable features are expressed in a same interval by replacing the time variable by a rate-invariant NAT variable. Thus, the good functioning of this approach is deeply related to the choice of NAT, and consequently to the choice of the TVRF. We present in this paper two different TVRF respecting the mentioned conditions: the Normalized Accumulated kinetic Energy (NAE) of the skeleton and the Normalized Pose Motion Signal Energy (NPMSE).

4.3.1. Normalized Accumulated kinetic Energy of the skeleton (NAE) as a Time Replacement Variable Function (TVRF)

The Normalized Accumulated kinetic Energy (NAE) of the skeleton is proposed as a Time Replacement Variable Function (TVRF). At an instant $t$ and for each instant
Figure 4: Let Instance$_1$, Instance$_2$ and Instance$_3$ be three skeleton sequences with a temporal length respectively equal to $N_1$, $N_2$ and $N_3$. This figure shows how the TVR allows the expression of different instances with different temporal range in a same fixed range $[a, b]$.

*instance*, NAE refers to the ratio $NAE(t)$ between the kinetic energy $E^{\text{kinetic}}_{\text{acc}}(t)$ consumed by the human body until $t$ and the total kinetic energy $E^{\text{kinetic}}_{\text{total}}$ consumed by the human body on the whole skeleton sequence composed of $N$ frames. Equation (11) describes this new term where $E(t)$ represents the kinetic energy consumed by the human body at an instant $t$.

\begin{equation}
    NAT = TVRF_{\text{inst}}(t) = NAE(t) = \frac{E^{\text{kinetic}}_{\text{acc}}(t)}{E^{\text{kinetic}}_{\text{total}}} \tag{11}
\end{equation}

Since the data structure is discrete. For each punctual instant $t_k$, NAE is calculated as follows in Equation (12). We recall that $N$ represents the number of frames.
contained in the skeleton sequence.

\[ NAT = TVRF_{\text{inst}}(t_k) = NAE(t_k) = \frac{E_{\text{acc}}^{\text{kinetic}}(t_k)}{E_{\text{total}}^{\text{kinetic}}} = \frac{\sum_{i=1}^{n} E_{\text{kinetic}}^{\text{acc}}(c_1)}{\sum_{c_2=1}^{N} E_{\text{kinetic}}^{\text{total}}(c_2)} \]  \hspace{1cm} (12)

Indeed, the NAE variable increases when the velocity of joints increases and consequently when the displacement quantity increases as well. If there is no motion, NAE does not increase. We use NAE for two essential reasons. First, all actions must be expressed in the same space which is guaranteed by the normalization of the energy (varying between 0 and 1). Secondly, to perform a coherent interpolation, a growing variable is necessary. This is why accumulation is used.

**Kinetic Energy Calculation:** Instead of considering the skeleton as a body, it can be assimilated to a set of \( n \) points where each one represents a skeleton joint. In many earlier papers [45, 46, 47], the kinetic energy of the human skeleton \( E_{\text{kinetic}}^{\text{total}}(t_k) \), at an instant \( t_k \), is expressed by the equation (13) where \( n \) represents the number of joints, \( m_i \) and \( V_i \), respectively, the mass and the velocity of the joint \( i \). Since the skeleton joints are fictitious, we assume that they have a unitary mass \( (m_i = 1, \forall i) \).

\[ E_{\text{kinetic}}^{\text{total}}(t_k) = \sum_{i=1}^{n} \frac{1}{2} m_i V_i^2(t_k) \]  \hspace{1cm} (13)

The NAE term \( NAE(t_k) \) is calculated, thanks to the kinetic energy term \( E_{\text{kinetic}}^{\text{total}}(t_k) \) described in the previous paragraph following equation (11). After a change of variables, the KF can be expressed as a variable depending on NAE \( \text{[10]} \). Hence, Kinematic Features are expressed in the same range \([0, 1]\) and become therefore less sensitive to execution rate variability.

### 4.3.2. Normalized Pose Motion Signal Energy (NPMSE) as a Time Variable Replacement Function (TVRF)

A second TVRF is proposed to replace the time variable called Normalized Pose Motion Signal Energy (NPMSE).
Before defining the notion of Pose Motion, we need to define the rest pose. The rest pose represents the position of the spatially normalized skeleton when any gesture can be visually detected as in Figure 2.

To obtain this rest pose, a statistical model could be learnt using the training data. For the moment, since we are still working with temporally segmented data and since we know that all actions in the used datasets start with the rest pose, we can use the first skeleton of the sequence to define the rest pose.

We define the Pose Motion Signal $s(t)$ as the distance $d$ between the current pose $P_{\text{norm}}(t)$ and the rest pose $P_{\text{norm}}(\text{rest})$ (first pose in our experimental conditions)

$$s(t) = d(P_{\text{norm}}(t), P_{\text{norm}}(\text{rest}))$$

This used distance can be $l_2, l_1$, etc. More details about the nature of the distance will be given in the experimental section. Since the available data has a discrete nature, the energy of the discrete signal $s(t_k)$ at an instant $t_k$ is calculated as follows

$$E_{\text{signal}}(t_k) = \sum_{i=1}^{k} |s(t_i)|^2$$

This term is called Pose Motion Signal Energy.

It is important to specify that in this paragraph the energy calculated is the signal energy and not the kinetic one, which are two different notions.

The Pose Motion Signal Energy is a growing term, thanks to the use of the sum in the energy calculation. However, to ensure that all the actions will be expressed in the same range, a normalization of this term has to be done. For an instance instance, the TVRF is therefore the Normalized Pose Motion Signal Energy (NPMSE) which is calculated by dividing the Pose Motion Signal Energy at an instant $t$ by the Pose Motion Signal Energy at the final instant of the sequence $t_f$ as described by equation

$$NAT = TVRF_{\text{instance}}(t) = NPMSE(t) = \frac{E_{\text{signal}}(t)}{E_{\text{signal}}(t_f)}$$
Since the time data are discrete, the NPMSE at an instant \( t_k \) is calculated as follows (17).

\[
N_{AT} = TVRF_{\text{instance}}(t_k) = NPMSE(t_k) = \frac{E_{signal}(t_k)}{E_{signal}(t_N)} = \frac{\sum_{i=1}^{k} |s(t_i)|^2}{\sum_{i=1}^{N} |s(t_i)|^2}
\]

4. Relation with key poses: The idea of using the distance between the current pose and the rest pose provides from the fact that the more the poses are different from the rest state, the more they can discriminate actions. It is in a certain way related to the notion of key poses presented in many papers [48, 49, 50], where the key pose is defined as the extreme pose of an action. In [48], authors show that this kind of pose is sufficient to obtain interesting results. However, this kind of method does not include the spatio-temporal aspect which is also important. For this reason, we propose this TVRF function which exploits the notion of keypose without removing the spatio-temporal aspect.

4.4. Cubic spline interpolation of Kinematic Features (KF)

Based on the continuous nature of human actions, we assume that the kinematic values (position, velocity, acceleration) also represent continuous functions of time. To switch from a numerical space to a continuous one, we propose to interpolate KF components depending on NAT as described in Section 4.3. For the interpolation, we use the cubic spline interpolation described in Section 3. Using the discrete information of each KF component, we obtain continuous functions \( \text{KF}_{c}^{i} \) depending on a chosen TVRF, as described in equation (18), where \( \text{Spline} \) refers to the cubic spline operator. We recall that \( M \) represents the dimension of \( \text{KF} \).

\[
\text{KF}_{c}^{i}(NAT) = \text{KF}_{c}^{i}(TVRF_{\text{instance}}(t)) = \text{Spline}(\text{KF}_{i}(TVRF(t_k)))_{k \in [0,N]}, \forall i \in [1,M]
\]

4.5. Uniform sampling

To build the final descriptor KSC of an instance \( \text{instance} \), the obtained functions are uniformly sampled, choosing a fixed number of samples \( s \). The choice of \( s \) will be
In this figure, we propose the visualization of a component curve sampling, after the temporal normalization. We consider two instances of the same type of action on the top and two instances containing different actions on the bottom. These samples are used to design the final descriptor. The more the curves are similar, the more the distances $d_i$ and $d'_i$ between their samples are smaller, for $i = 0...5$ (because the number of samples $s$ is equal to 6 in this example). The classification will be based on this distance since an SVM classifier is used.

This process allows us not only to obtain same-size descriptors regardless of the sequence length but also to normalize the actions temporally and obtain values according to the same amount of NAT. The step used for the sampling is proportional to the sequence length in order to obtain a fixed size of $9 \times n \times s$ for all human motion descriptors. The final descriptor KSC used for the classification is depicted by equation (19).

$$KSC = \bigcup_{i=1..M} \bigcup_{e=0..s-1} KF_i^e(NAT(a + \frac{e(b-a)}{s-1})) \quad (19)$$

Figure 5 illustrates the interest of uniform sampling after interpolation of curves expressed as functions of a TVRF. The idea is to maximize the Euclidean distance be-
tween two feature vectors when the represented actions are different and to maximize it when they represent the same action. We summarize the different processes that allow us to compute a KSC descriptor from a skeleton sequence in Algorithm 2.

**Algorithm 2: Computation of KSC from an instance instance**

**Input:** skeleton sequence \((P_j(t_k))_{1 \leq j \leq n, 1 \leq k \leq N}\)

**Output:** \(KSC\)

1. Normalize Skeleton \((P_j^\text{norm}(t_k))_{1 \leq j \leq n, 1 \leq k \leq N}\) \((6)\)
2. Compute Kinematic Features \(KF_i(t_k)_{1 \leq i \leq M}\) \((10)\)
3. Compute \((TVRF_{\text{instance}}(t_k))_{1 \leq k \leq N}\) \((11)\)
4. for \(i \leftarrow 1 \text{ to } M\) do
   5. Interpolation: \(KF^c_i(NAT) = KF^c_i(TVRF_{\text{instance}}(t)) := Spline(KF_i(TVRF_{\text{instance}}(t_k)))_{1 \leq k \leq N}\)
6. end
7. Uniform sampling with a sampling rate \(s\):
   \[KSC := \bigcup_{i=1..M} \bigcup_{e=0..s-1} KF^c_i(NAT(a + \frac{(b-a)e}{s-1}))\]

4.6. Action recognition via linear Support Vector Machine

To perform action recognition, the KSC is used with a linear Support Vector Machine (SVM) classifier provided by the SVM library LibSVM \[51\]. The multi-class SVM proposed by \[52\] is carried out with a cost which is equal to 10. The main advantage of the linear kernel classifier is its low computational latency compared to non-linear kernel ones \[53\].

5. Experimental evaluation

In this section, we propose to evaluate the proposed method for action recognition on five benchmarks: MSRAction3D \[5\], UTKinect \[13\], MSRC12 \[14\], Multiview3D Action dataset \[15\] and NTU RGB+D dataset \[16\].

**MSRAction3D dataset:** This dataset represents one of the most famous benchmarks captured by a RGB-D camera and contains segmented human actions. This
benchmark is composed of 20 actions, performed by 10 different subjects, 2 or 3 times. It provides 2 modalities: skeleton joints and depth maps. The challenge of this dataset resides in its very similar actions.

**UTKinect dataset:** The UTKinect is also a well-known benchmark often used for the testing of RGB-D based human action recognition methods. It contains 3 modalities: RGB images, depth images and skeleton joints. 10 actions are performed twice by 10 subjects. This dataset is very challenging especially due to a significant intra-class variation.

**MSRC12 dataset:** This dataset is generally used for skeleton-based action detection. It contains 594 sequences including 12 different types of gestures performed by 30 subjects. In total, there are 6244 annotated gesture instances. MSRC12 only provides skeleton joints and action points which correspond to the beginning of an action. Despite the fact that MSRC12 dataset has been initially proposed for action detection, it could be very useful for the action recognition task because of its large volume.

**Multiview3D Action\(^1\) dataset:** In opposition to the two other benchmarks, Multiview3D is a very recent dataset. It also contains the three modalities captured by an RGB-D sensor. The dataset is composed of 12 actions performed by 10 actors in 3 different orientations (−30°, 0°, 30°). The challenge of this dataset is its wide body orientation variation.

**NTU RGB+D dataset:** The NTU RGB+D dataset is a very large action recognition dataset containing human skeletons. It contains a total of 56880 sequences. This dataset is composed of 60 classes performed by 40 different subjects. Each skeleton is composed of 25 joints. It contains also 80 different viewpoints.

### 5.1. Experimental Settings

In this subsection, we specify the conditions of experimentation settings chosen for the four first benchmarks. All calculations were run on the same machine, a Dell Inspiron N5010 laptop computer with Intel Core i7 processor, Windows 7 operating

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\(^1\)Multiview3D dataset can be download from the following link: [http://english.stackexchange.com/questions/55898/related-work-or-related-works](http://english.stackexchange.com/questions/55898/related-work-or-related-works)
system and 4GB RAM. To evaluate a given method in terms of computational latency, we propose to report the Mean Execution Time (MET) per descriptor. Indeed, this value which represents the average time necessary to compute a descriptor is an interesting indicator. We underline that each descriptor corresponds to the feature vector extracted from a whole action.

It could be noted that in the literature, papers generally do not report the execution time per descriptor, providing only the recognition accuracy. On the other hand, the parameters of evaluation vary greatly from one paper to another as discussed in the work of [54]. Since the goal of this work is to realize a trade-off between computational latency and accuracy, we propose to recover and to evaluate some available descriptors in terms of MET and accuracy. These latter can be divided into two main groups. The first one composed of depth-based descriptors, includes the square Histogram of Oriented Gradient (HOG2), the Histogram of Oriented Normals 4D (HON4D) and the Super Normal Vector (SNV) representations. The second one composed of skeleton-based descriptors, includes Joint Positions (JP), Relative Joint Positions (RJP), Quaternions (Q) and finally Lie Algebra Relative Pairs (LARP). These descriptors are tested on four datasets by respecting the same protocol of evaluation.

For MSRAction3D, the parameters used [5] are followed. The dataset is divided into three groups (AS1, AS2, AS3) where each one is composed of 8 actions. Hence, the classification is done on each group separately. A cross-splitting is carried out to separate the data in training and testing samples as in [9]: the data performed by the subjects 1,3,5,7,9 have been used for training and the rest has been used for testing.

For UTKinect, we used the settings given in the experimentation of [8], where the actions performed by half of the subjects were considered as training data and the rest as testing data.

For MSRC12, we followed the same protocol used in the paper of [55] where the end points of actions have been added to the dataset. Thanks to these points, it became possible to benefit from the large amount of data in order to test an action recognition method without detecting actions. Thus, a cross-splitting is done where the actions performed by half of the subjects are used for training, while the rest of data is used for testing.
<table>
<thead>
<tr>
<th>Descriptor</th>
<th>AS1(%)</th>
<th>AS2(%)</th>
<th>AS3(%)</th>
<th>Overall(%)</th>
<th>Time(s)</th>
</tr>
</thead>
<tbody>
<tr>
<td>HOG2 [6]</td>
<td>90.47</td>
<td>84.82</td>
<td>98.20</td>
<td>91.16</td>
<td>6.44</td>
</tr>
<tr>
<td>HON4D [7]</td>
<td>94.28</td>
<td>91.71</td>
<td>98.20</td>
<td>94.47</td>
<td>27.33</td>
</tr>
<tr>
<td>SNV [9]</td>
<td>95.25</td>
<td>94.69</td>
<td>96.43</td>
<td>95.46</td>
<td>146.57</td>
</tr>
<tr>
<td>JP [8]</td>
<td>82.86</td>
<td>68.75</td>
<td>83.73</td>
<td>78.44</td>
<td>0.58</td>
</tr>
<tr>
<td>RJP [8]</td>
<td>81.90</td>
<td>71.43</td>
<td>88.29</td>
<td>80.53</td>
<td>2.15</td>
</tr>
<tr>
<td>Q [8]</td>
<td>66.67</td>
<td>59.82</td>
<td>71.48</td>
<td>67.99</td>
<td>1.33</td>
</tr>
<tr>
<td>LARP [8]</td>
<td>83.81</td>
<td>84.82</td>
<td>92.73</td>
<td>87.14</td>
<td>17.61</td>
</tr>
<tr>
<td>HOPC* [35]</td>
<td>-</td>
<td>-</td>
<td>-</td>
<td>86.5</td>
<td>-</td>
</tr>
<tr>
<td>KSC-NAE (ours)</td>
<td>86.92</td>
<td>72.32</td>
<td>94.59</td>
<td>84.61</td>
<td>0.092</td>
</tr>
<tr>
<td>KSC-NPMSE-(l_1) (ours)</td>
<td>85.05</td>
<td>85.71</td>
<td>96.4</td>
<td>89.05</td>
<td>0.091</td>
</tr>
<tr>
<td>KSC-NPMSE-(l_2) (ours)</td>
<td>84.11</td>
<td>87.50</td>
<td>97.30</td>
<td>89.64</td>
<td>0.092</td>
</tr>
</tbody>
</table>

Table 1: Accuracy of recognition and execution time per descriptor(s) on MSRAAction3D: AS1, AS2 and AS3 represents the three groups proposed in the protocol experimentation of [5]. *The values have been recovered from the state-of-the-art.

For Multiview3D, we followed the experimental settings proposed in [15]. A cross-splitting is also done dividing the training and the testing samples. Then, the classification is done several times taking each time a specific orientation for the training and another specific orientation for the testing. This procedure allows us to analyze the effect of view-point changes on the accuracy of recognition.

In the experiments, the two TVRF presented in Section 4.3 are tested: the NAE and the NPMSE. When the KSC is calculated based on the temporal normalization using the NAE, our descriptor is noted KSC-NAE. To calculate NPMSE, two kind of distances are used \(l_1\) and \(l_2\). When the function NMPSE (using the distances \(l_1\) and \(l_2\)) during the temporal normalization, our descriptor is respectively noted KSC-NMPSE-\(l_1\) and KSC-NMPSE-\(l_2\).

The first benchmark allows us to test our algorithm against others in terms of accuracy and rapidity. Testing our descriptor in the other three datasets shows its robustness.
Table 2: Execution time (s) of each process per KSC-NPMSE-l descriptor on the four benchmarks

<table>
<thead>
<tr>
<th>Process</th>
<th>MSRAction3D</th>
<th>UTKinect</th>
<th>Multiview3D</th>
<th>MSRC12</th>
</tr>
</thead>
<tbody>
<tr>
<td>Spatial Normalization</td>
<td>0.022</td>
<td>0.016</td>
<td>0.016</td>
<td>0.06</td>
</tr>
<tr>
<td>Descriptor computing</td>
<td>0.07</td>
<td>0.064</td>
<td>0.073</td>
<td>0.077</td>
</tr>
<tr>
<td>Classification</td>
<td>0.008</td>
<td>0.002</td>
<td>0.010</td>
<td>0.015</td>
</tr>
<tr>
<td>Total</td>
<td>0.1</td>
<td>0.082</td>
<td>0.099</td>
<td>0.152</td>
</tr>
</tbody>
</table>

Table 3: Accuracy of recognition and MET per descriptor on UTKinect dataset. *The values have been recovered from the state-of-the-art

<table>
<thead>
<tr>
<th>Descriptor</th>
<th>Accuracy (%)</th>
<th>MET (s)</th>
</tr>
</thead>
<tbody>
<tr>
<td>HOG2 [6]</td>
<td>74.15</td>
<td>5.03</td>
</tr>
<tr>
<td>HON4D [7]</td>
<td>90.92</td>
<td>25.39</td>
</tr>
<tr>
<td>SNV [9]</td>
<td>79.80</td>
<td>1365.33</td>
</tr>
<tr>
<td>JP [8]</td>
<td>100</td>
<td>0.43</td>
</tr>
<tr>
<td>RJP [8]</td>
<td>97.98</td>
<td>1.91</td>
</tr>
<tr>
<td>Q [8]</td>
<td>88.89</td>
<td>1.40</td>
</tr>
<tr>
<td>LARP [8]</td>
<td>97.08</td>
<td>42.00</td>
</tr>
<tr>
<td>Random Forrest* [56]</td>
<td>87.90</td>
<td>-</td>
</tr>
<tr>
<td>ST-LSTM* [21]</td>
<td>95</td>
<td>-</td>
</tr>
<tr>
<td>KSC-NAE (ours)</td>
<td>84.00</td>
<td>0.08</td>
</tr>
<tr>
<td>KSC-NPMSE-l1 (ours)</td>
<td>94.00</td>
<td>0.09</td>
</tr>
<tr>
<td>KSC-NPMSE-l2 (ours)</td>
<td>96.00</td>
<td>0.10</td>
</tr>
</tbody>
</table>

Table 4: Accuracy of recognition and MET per descriptor on MSRC12 dataset. *The values have been recovered from the state-of-the-art

<table>
<thead>
<tr>
<th>Descriptor</th>
<th>Accuracy (%)</th>
<th>MET (s)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Logistic Regression* [12]</td>
<td>91.2</td>
<td>-</td>
</tr>
<tr>
<td>Covariance descriptor* [55]</td>
<td>91.7</td>
<td>-</td>
</tr>
<tr>
<td>KSC-NAE (ours)</td>
<td>84.00</td>
<td>0.137</td>
</tr>
<tr>
<td>KSC-NPMSE-l1 (ours)</td>
<td>93.22</td>
<td>0.134</td>
</tr>
<tr>
<td>KSC-NPMSE-l2 (ours)</td>
<td>94.27</td>
<td>0.134</td>
</tr>
</tbody>
</table>
### Table 5: Accuracy of recognition and MET per descriptor on Multiview3D dataset.

*The values have been recovered from the state-of-the-art

<table>
<thead>
<tr>
<th>Descriptor</th>
<th>Same view (%)</th>
<th>Different view (%)</th>
<th>MET (s)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Actionlet* [19]</td>
<td>87.1</td>
<td>69.7</td>
<td>-</td>
</tr>
<tr>
<td>HOG2 [6]</td>
<td>87.8</td>
<td>74.2</td>
<td>9.06</td>
</tr>
<tr>
<td>HON4D [7]</td>
<td>89.3</td>
<td>76.6</td>
<td>17.51</td>
</tr>
<tr>
<td>SNV [5]</td>
<td>94.27</td>
<td>76.65</td>
<td>271.72</td>
</tr>
<tr>
<td>JP [8]</td>
<td>96.00</td>
<td>88.10</td>
<td>1.22</td>
</tr>
<tr>
<td>RJP [5]</td>
<td>97.70</td>
<td>92.7</td>
<td>4.58</td>
</tr>
<tr>
<td>Q [8]</td>
<td>91.30</td>
<td>72.10</td>
<td>2.52</td>
</tr>
<tr>
<td>LARP [8]</td>
<td>96.00</td>
<td>88.1</td>
<td>10.51</td>
</tr>
<tr>
<td>KSC-NAE (ours)</td>
<td>82.12</td>
<td>79.43</td>
<td>0.09</td>
</tr>
<tr>
<td>KSC-NPMSE-l1 (ours)</td>
<td><strong>90.63</strong></td>
<td>89.67</td>
<td>0.091</td>
</tr>
<tr>
<td>KSC-NPMSE-l2 (ours)</td>
<td><strong>90.45</strong></td>
<td><strong>90.10</strong></td>
<td>0.092</td>
</tr>
</tbody>
</table>

5.2. Results and discussion

5.2.1. Low computational latency

Table 1, Table 3, Table 4 and Table 5 compare our approach with state-of-the-art methods in terms of computational latency by reporting the MET per descriptor in respectively MSRAction3D, UTKinect, MSRC12 and Multiview3D datasets. As mentioned in [3], it has been shown that the skeleton extraction process lasts approximately 45ms/per frame with the knowledge that actions are generally contained in a window composed of 12 to 50 frames. Thus, a fair comparison of execution time would have consisted in adding a penalty of 2250 ms for skeleton methods. But, this would have no influence on the fact that our approach remains more suited to real-time applications, despite an additional extraction process. Indeed, we show that our descriptors KSC-NAE, KSC-NPMSE-l1 and KSC-NPMSE-l2 are faster in terms of computational latency with a maximum of only 0.092s of MET on MSRAction3D dataset, 0.10 on UTKinect dataset, 0.137 on MSRC12 dataset and 0.092 on Multiview3D dataset. Also, Table 2 which presents the execution time per descriptor of each process on the four benchmarks. Since some state-of-the-art methods do not provide their codes, we added an asterisk in front of their name to indicate that the accuracy has been directly re-
covered from the associated papers (the experimental conditions can be different than ours). For this reason, we could not provide the MET required for these methods.

However, in [35], the time of calculation required for each frame is reported. The authors mention that the calculation of their descriptor takes about 2 seconds per frame (between 30 seconds and 100 seconds for a whole video of the MSRAction3D dataset). Knowing that the machine used for their experiments (3.4 GHz with 24 GB RAM) is largely more powerful than our laptop, one can say that the descriptors presented in our paper require less execution time.

Thus, with these results, we can assume that the constraint of low computational latency is respected. However, it is important to notice that the computational latency also depends from a lot of parameters such as the image resolution (from the number of joints, in this case) as well as the number of classes (20 for MSRAction3D, 10 for UTKinect, 12 for MSRC12 and 12 for Multiview3D datasets) and Table 1, Table 3, Table 4 and Table 5 aim just at comparing execution time of different techniques applied to a similar situation.

5.2.2. Good accuracy and Robustness

Computational latency is an important criterion of evaluation, but is not sufficient. In fact, the accuracy of recognition must be acceptable. On the MSRAction3D, our method allows us to recognize 89.64% of the actions correctly using KSC-NPMSE-$l_2$ descriptor, which is a better score than other skeleton representations. On the other hand, even if depth-based descriptors give better results in terms of accuracy of recognition, their MET per descriptor remain too high and seem to be unsuitable for real-time applications (6.44s for HOG2, 27.33s for HON4D, 146.57s for SNV versus 0.092s for KSC). Table 3, Table 9 and Table 4 respectively report the accuracy of recognition of our method on UTKinect, MSRC12 and Multiview3D datasets and compare it to state-of-the-art methods. While on UTKinect the accuracy of recognition using KSC-NPMSE-$l_2$ descriptor is 96% (1% less than the highest score), the accuracy of our method on MSRC12 dataset outperforms recent state-of-the-art method with 94.27%. On Multiview3D dataset, the accuracy of recognition given by the descriptor KSC-NPMSE-$l_2$ is also acceptable. When the training and testing are carried out using data
Table 6: Effect of each process on the accuracy of recognition using KSC-NPMSE-$l_2$

<table>
<thead>
<tr>
<th>Deleted Process</th>
<th>MSRAction3D (%)</th>
<th>UTKinect (%)</th>
<th>Multiview3D SV (%)</th>
<th>Multiview3D DV (%)</th>
<th>MSRC12 (%)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Nothing</td>
<td>89.64</td>
<td>96.00</td>
<td>91.67</td>
<td>86.11</td>
<td>94.17</td>
</tr>
<tr>
<td>without S.N.</td>
<td>84.49</td>
<td>87.00</td>
<td>91.00</td>
<td>83.85</td>
<td>92.71</td>
</tr>
<tr>
<td>without T.N.</td>
<td>76.73</td>
<td>87.00</td>
<td>81.60</td>
<td>68.40</td>
<td>81.43</td>
</tr>
</tbody>
</table>

with the Same Viewpoint (SV), the score of accuracy is equal to 91.67% (around 4% percent less than the highest score and 4% percent better than Actionlet). And when the training and testing use data with Different Viewpoints (DV), the recognition accuracy is equal to 86.11% (versus 88.1% for LARP and 69.7% for Actionlet). As mentioned before, Table 2 shows that computational latency remains relatively low on the four datasets using our method. Thus, we can conclude that the performance of our descriptor is acceptable on the four benchmarks and that our method is robust to the dataset changing.

5.2.3. NAE vs NPMSE

Thanks to the experiments, we can conclude that the NMPSE function gives better results than the NAE function on the four datasets. Indeed, we can notice a difference of around 5% on MSRAction3D dataset, 12% of UTKinect dataset, 10% on MSRC12 dataset and 4% on Multiview3D dataset between the descriptors KSC-NAE and KSC-NPMSE-$l_2$, while the execution time per descriptor remains the same. Also, compared to the distance $l_1$, the distance $l_2$ gives slightly more accurate results. In future work, it could be interesting to compare a wider range of more sophisticated distances. By observing the shape of the two curves (NAE and NPMSE-$l_2$) as shown by Figure 6, it can be noticed that the NMPSE is smoother than NAE and that NMPSE increases importantly only in the presence of key poses, while NAE increases more uniformly. The superiority of NMPSE as a TVRF function could be explained by the fact that the notion of key frames is more exploited with the use of NMPSE. In the rest of experiments, only the KSC-NPMSE-$l_2$ will be taken into account since it gives the best results.
5.2.4. Benefits of Spatial Normalization (SN)

Table 9 reports the effect of the different processes of normalization. Each column of the table presents the obtained accuracy of recognition, after deleting one of the proposed processes contributing to spatial and temporal normalizations. We can observe that SN contributes considerably to increasing the accuracy on the three datasets. We observe an increase of around 5% for MSRAction3D, 9% for UTKinect and approximately 0.67% and around 2% for Multiview3D (for respectively SV and DV tests) and more than 1% for MSRC12, when SN is used. To explain the use of unitary Euclidean normalization instead of the use of an average skeleton as in [43], we report the results of our method combined with an average skeleton-based normalization on the four datasets used. The accuracy of recognition is very low compared with the values obtained using our spatial normalization algorithm with only 81.92% on MSRA Action3D, 84% on UTKinect and 87.5%(SV) - 79.95% (DV) on Multiview3D.
Table 7: Effect of each kinematic component on the accuracy of recognition using KSC-NPMSE-$l_2$

<table>
<thead>
<tr>
<th></th>
<th>MSRAction3D (%)</th>
<th>UTKinect (%)</th>
<th>Multiview3D SV (%)</th>
<th>Multiview3D DV (%)</th>
<th>MSRC12 (%)</th>
</tr>
</thead>
<tbody>
<tr>
<td>P+V+A</td>
<td>89.64</td>
<td>96.00</td>
<td>91.67</td>
<td>86.11</td>
<td>94.17</td>
</tr>
<tr>
<td>P+V</td>
<td>86.06</td>
<td>92.00</td>
<td>90.63</td>
<td>82.64</td>
<td>93.92</td>
</tr>
<tr>
<td>P</td>
<td>86.04</td>
<td>90.00</td>
<td>86.98</td>
<td>70.05</td>
<td>93.50</td>
</tr>
<tr>
<td>V</td>
<td>83.01</td>
<td>90.00</td>
<td>85.07</td>
<td>78.56</td>
<td>89.68</td>
</tr>
<tr>
<td>A</td>
<td>82.39</td>
<td>81.00</td>
<td>83.33</td>
<td>77.78</td>
<td>86.46</td>
</tr>
</tbody>
</table>

5.2.5. Benefits of Temporal Normalization (TN): the TVR algorithm

In Table 5, the removal of the TN process (TVR algorithm) shows its important role in our method. Indeed, without TN, the accuracy of recognition decreases from 89.64% to 76.73% on MSRAction 3D, from 96% to 87% on UTKinect, from 91.67%(SV)-86.11%(DV) to 81.60%(SV)-68.40%(DV) on Multiview3D and from 94.17% to 81.43%. These results confirm the ability of our algorithm to cope with execution rate variability. This algorithm is very useful for pre-segmented actions, since it is fast and efficient. However, to work efficiently, the video should start with a skeleton in a rest state. Indeed, the calculation of the NPMSE term, which quantifies the important phase of the motion, is based on this assumption.

5.2.6. Benefits of kinematic features

In Table 7, we evaluate the importance of each kinematic term. This table shows that position is generally the most discriminative value followed by velocity and acceleration. This may be due to the increase of the approximation error caused by the derivations. Nevertheless, the combined information of the three kinematic values give us the best amount of accuracy on the four datasets.

5.2.7. Parameter s influence

The parameter $s$, which represents the number of samples affects the accuracy of recognition. As shown in the Table 8, with varying the parameter $s$, the accuracy of recognition will also vary. The parameter $s$ is therefore fixed according to the best score obtained ($s = 15$ for MSRAction3D, UTKinect and Multiview3D and $s = 40$ for MSRC12). If $s$ is fixed too small, the accuracy decreases because of a loss of
<table>
<thead>
<tr>
<th>number of samples</th>
<th>5 (%)</th>
<th>10 (%)</th>
<th>15 (%)</th>
<th>20 (%)</th>
<th>25 (%)</th>
<th>30 (%)</th>
<th>35 (%)</th>
<th>40 (%)</th>
<th>45 (%)</th>
<th>50 (%)</th>
</tr>
</thead>
<tbody>
<tr>
<td>MSRAction3D</td>
<td>86.03</td>
<td>86.90</td>
<td><strong>89.64</strong></td>
<td>88.75</td>
<td>88.46</td>
<td>88.14</td>
<td>87.55</td>
<td>87.86</td>
<td>86.96</td>
<td>86.94</td>
</tr>
<tr>
<td>UTKinect</td>
<td>94.00</td>
<td>95.00</td>
<td><strong>96.00</strong></td>
<td>93.00</td>
<td>95.00</td>
<td>95.00</td>
<td>94.00</td>
<td>94.00</td>
<td>94.00</td>
<td>94.00</td>
</tr>
<tr>
<td>Multiview3D (SV)</td>
<td>88.54</td>
<td>90.28</td>
<td><strong>91.67</strong></td>
<td>90.45</td>
<td>89.58</td>
<td>89.76</td>
<td>90.10</td>
<td>90.10</td>
<td>90.10</td>
<td>90.10</td>
</tr>
<tr>
<td>Multiview3D (DV)</td>
<td>83.51</td>
<td>85.07</td>
<td><strong>86.11</strong></td>
<td>84.11</td>
<td>84.20</td>
<td>84.72</td>
<td>84.38</td>
<td>84.55</td>
<td>84.37</td>
<td>84.46</td>
</tr>
<tr>
<td>MSC12</td>
<td>92.20</td>
<td>92.96</td>
<td>93.91</td>
<td>93.92</td>
<td>93.69</td>
<td>94.04</td>
<td>94.11</td>
<td><strong>94.17</strong></td>
<td>94.08</td>
<td>93.98</td>
</tr>
</tbody>
</table>

Table 8: Effect of \( s \) the number of samples \( s \) on the accuracy of recognition using KSC-NPMSE-\( l_2 \)

information. On the other hand, if \( s \) is too high, the accuracy also decreases since the influence of the interpolation errors increases. Indeed, the original data is numerical and has been interpolated. Nevertheless, it is important to notice that the choice of \( s \) does not affect the results considerably. For the values tested, we observe a decrease of up to 3% compared with the highest score of accuracy for a number of samples varying between 5 and 50.

5.3. Performance on a large-scale dataset: NTU + RGB-D dataset

In this part, we propose to test our method on the recent large-scale action recognition benchmark: NTU-RGB+D dataset. Because of the important amount of data, we use for this experimentation another laptop: an i7 macbook pro with 16 Go of RAM. Since this dataset contains mutual actions involving more than one human, only the skeleton consuming more kinetic energy is considered. On the other hand, some joints are sometimes confused and have exactly the same coordinates. To overcome that, a small Gaussian noise is added to one of the two joints. We follow the same experimental protocol used in [16] and we propose to report the accuracy in Table 9 obtained for the two settings: cross-subject and cross-view. Compared to hand-crafted methods, our approach reaches the best score of accuracy while realizing the cross-subject test (with 51.12\% ) and the second best score while performing cross-view test (with 51.39\%, slightly inferior to the accuracy obtained for the Lie Group [8] representation 52.76\%). We specify that the parameter \( s \) has been fixed to 20. Despite the promising results, it can be noted in Table 9 that methods based on learned features remain more efficient on this dataset in terms of accuracy.
### Table 9: Accuracy of recognition of different methods on NTU-RGB+D

<table>
<thead>
<tr>
<th>Class of method</th>
<th>Method</th>
<th>Cross-subject (%)</th>
<th>Cross-view (%)</th>
</tr>
</thead>
<tbody>
<tr>
<td>hand-crafted</td>
<td>HOG2 [6]</td>
<td>32.24</td>
<td>22.27</td>
</tr>
<tr>
<td></td>
<td>SNV [9]</td>
<td>31.82</td>
<td>13.61</td>
</tr>
<tr>
<td></td>
<td>HON4D [7]</td>
<td>30.56</td>
<td>7.26</td>
</tr>
<tr>
<td></td>
<td>Lie Group [8]</td>
<td>50.08</td>
<td>52.76</td>
</tr>
<tr>
<td></td>
<td>Skeletal Quads [57]</td>
<td>38.62</td>
<td>41.36</td>
</tr>
<tr>
<td></td>
<td>KSC-NMPSE-L₂ (ours)</td>
<td><strong>51.12</strong></td>
<td><strong>51.39</strong></td>
</tr>
<tr>
<td>learned features</td>
<td>HBRNN-L [53]</td>
<td>59.07</td>
<td>63.97</td>
</tr>
<tr>
<td></td>
<td>ST-LSTM [21]</td>
<td>69.2</td>
<td>77.7</td>
</tr>
<tr>
<td></td>
<td>SkeletonNet [22]</td>
<td>75.94</td>
<td>81.16</td>
</tr>
<tr>
<td></td>
<td>Rahmani et al. [59]</td>
<td>75.2</td>
<td>83.1</td>
</tr>
<tr>
<td></td>
<td>Clips + CNN + MTLN [20]</td>
<td>79.57</td>
<td>84.83</td>
</tr>
</tbody>
</table>

### 6. Conclusion and future work

In this work, we have presented a novel descriptor for fast action recognition. It is based on the cubic spline interpolation of kinematic values of joints, more precisely, position, velocity and acceleration. To make our descriptor invariant to anthropometric variability and execution rate variation, we perform a skeleton normalization as well as a temporal normalization. For this reason, a novel method of temporal normalization is proposed called TVR. The proposed method have shown its efficiency in terms of accuracy and computational latency on four different datasets.

However, actions are assumed to be already segmented. In future work, the issue of temporal segmentation will be studied. Some techniques developed for dynamical switched models can be used to detect different modes in an unsegmented sequence, allowing the detection of particular points of transition from an action to another or from an action to the rest state. First attempts have been made to adapt these methods in [60] [61] [62] [23].

### References


[48] L. Miranda, T. Vieira, D. Martinez, T. Lewiner, A. W. Vieira, M. F. Campos, Real-time gesture recognition from depth data through key poses learning and


